

## *Supporting Information for Article*

# Empirical Models with Constant and Variable Activation Energy for Biomass Pyrolysis

Published in *Energy & Fuels*, **2019**, 33, 2348-2358.

DOI: 10.1021/acs.energyfuels.9b00040 (*Open access*)

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**Keywords:** Isoconversional; Model-free; Least Squares; Kinetics; Non-isothermal; Biomass; Wood; Bark; Agricultural wastes

**Scope of this document:** Models are presented for 16 different types of biomass. Their performance is illustrated by figures showing the calculated and experimental data. *Such experimental curves are shown here that had also been displayed in the figures of the original papers.* In this way the reader can compare the present fit quality to the ones obtained by other sorts of modelling.

**Notation in the Figures:** Two models are shown for each biomass: one with  $E(\alpha)$  approximated by a **third-order polynomial (red color)**, and another one **when  $E$  does not depend on  $\alpha$  (blue color)**. This coloring scheme was applied to the plots of  $E(\alpha)$  and  $\tilde{A}(\alpha)f(\alpha)$  as well as to the figures illustrating the fit quality. In the latter figures the experimental mass loss rate curves ( $-dm/dt$ ) were denoted by **thick gray lines**, while the temperature – time dependences ( $T(t)$ ), when present, were represented by **thin dashed green lines**.

Each section starts with a figure on the 4 – 9 temperature programs that were employed for the given set of experiments; the selection of the colors in these figures is arbitrary (it aimed only at the discernibility of the 4 – 9  $T(t)$  curves).

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## About the Employed Models

Herewith the model is repeated from the article and a few relations are added:

The employed empirical model:

$$d\alpha/dt = A(\alpha)f(\alpha) \exp(-E(\alpha)/RT) \quad (S1)$$

where  $\alpha$  is the reacted fraction (dimensionless), while  $[A(\alpha)f(\alpha)]/s^{-1}$  and  $E(\alpha)/kJmol^{-1}$  are empirical functions.

In a rearranged form:

$$d\alpha/dt = \tilde{A}(\alpha)(1-\alpha) \exp(-E(\alpha)/RT) \quad (S2)$$

where the term  $(1-\alpha)$  ensures that  $d\alpha/dt$  would be 0 at  $\alpha=1$ .  $\tilde{A}(\alpha)=A(\alpha)f(\alpha)/(1-\alpha)$  when  $\alpha<1$ . (Obviously, the division by  $(1-\alpha)$  is not possible at the  $\alpha=1$  point. There, however,  $\tilde{A}(\alpha)$  may have any finite value so that  $\tilde{A}(\alpha)(1-\alpha)$  would be zero at  $\alpha=1$ .)

A further rearrangement yields:

$$d\alpha/dt = (1-\alpha) \exp(\ln \tilde{A}(\alpha)-E(\alpha)/RT) \quad (S3)$$

To obtain flexible approximations with limited numbers of unknowns,  $\ln \tilde{A}(\alpha)$  and  $E(\alpha)$  are approximated by polynomials. For this purpose, the variable  $x=2\alpha-1$  is introduced which varies from -1 till +1 as  $\alpha$  varies from 0 to 1 and the results will be presented as the following example shows:

$$E(x) = 177.269618 - 37.801456 x + 26.878364 x^2 + 93.1628 x^3 \quad (S4)$$

Each model will also be expressed by Chebyshev polynomials of the first kind ( $T_0, T_1(x), T_2(x), \dots$ ) because they have favorable properties for actual calculations. For example, the above polynomial is also expressed as

$$E(x) = 190.7088 T_0(x) + 32.070644 T_1(x) + 13.439182 T_2(x) + 23.2907 T_3(x) \quad (S5)$$

*The user is kindly asked to select whichever form he/she likes better.*

Pls note that the calculation with the by Chebyshev polynomials of the first kind are fast and simple. There is no need for the actual form of these polynomials because their values can be calculated by a simple recurrence relationship at any  $x$ . In our case it means the insertion of a few simple program lines in the source code. For example:

```
T0 = 1;
T1 = x;
T2 = 2*x*T1 - T0;
T3 = 2*x*T2 - T1;
E = a[0] + a[1]*T1 + a[2]*T2 + a[3]*T3;
```

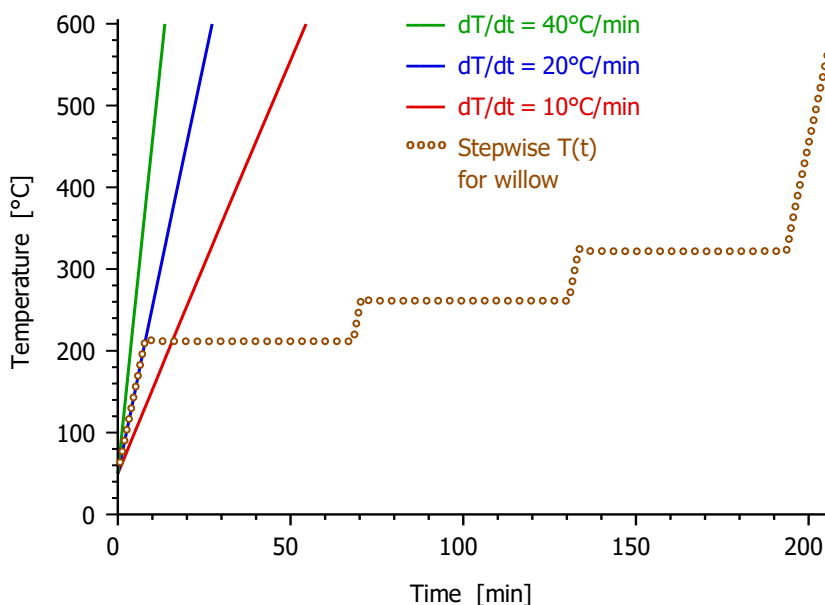
where array **a** contains the coefficients of a polynomial of type eq S5 and the program lines are written in C (C++/C#/Java) notation.

## S1. Wood shoots from an energy plantation

Source of the data:

[S1] Mészáros, E.; Várhegyi, G.; Jakab, E.; Marosvölgyi, B.: Thermogravimetric and reaction kinetic analysis of biomass samples from an energy plantation. *Energy Fuels* **2004**, *18*, 497-507. doi: [10.1021/ef034030%2B](https://doi.org/10.1021/ef034030%2B) [Repository](#)

Four TGA experiments were available for each sample. The figure below shows the corresponding temperature programs. It is a redrawn/rearranged version of Figure 1 of the cited paper. Please note that the stepwise programs differed for the different samples; the one in Figure S2.1 was used for the willow shoots.



**Figure S1.1:** Temperature programs used for the TGA experiments of this section.

## S1.1. Black locust shoots (*Robinia pseudoacacia*)

### Model with constant E:

Input file: "B\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 201.39157$$

$$\log_{10}\tilde{A}(x)= 14.767721 - .837505x + .7874086x^2 + .175056x^3 + .0748392x^4 - .806736x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 15.18949T_0(x) - 1.210423T_1(x) + .4311239T_2(x) - .208341T_3(x) + .0093549T_4(x) - .050421T_5(x)$$

### Model with third order E( $\alpha$ ):

Input file: "B\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

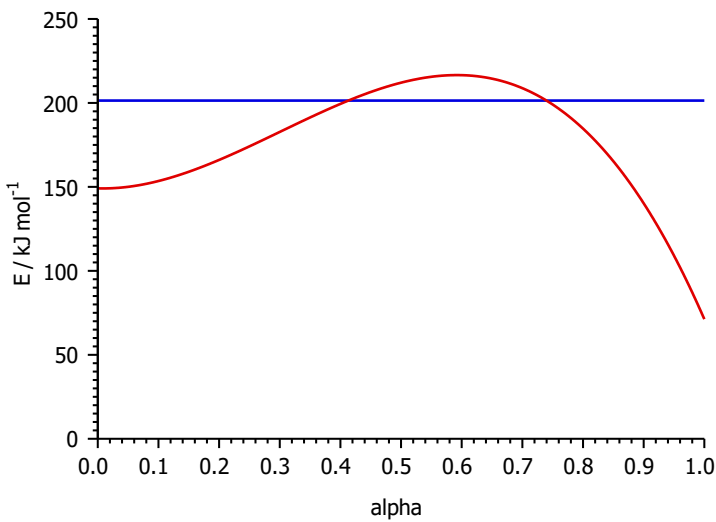
$$E(x)= 212.05679 + 46.19796x - 101.87136x^2 - 85.14972x^3$$

$$\log_{10}\tilde{A}(x)= 15.543158 + 2.883188x - 7.763372x^2 - 5.756672x^3 - .703496x^4 - 1.915872x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 161.12111T_0(x) - 17.66433T_1(x) - 50.93568T_2(x) - 21.28743T_3(x)$$

$$\log_{10}\tilde{A}(x)= 11.397661T_0(x) - 2.631736T_1(x) - 4.233434T_2(x) - 2.037878T_3(x) - .087937T_4(x) - .119742T_5(x)$$



#### E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)

Parameter file: B\_0,5\_oneC.PAR

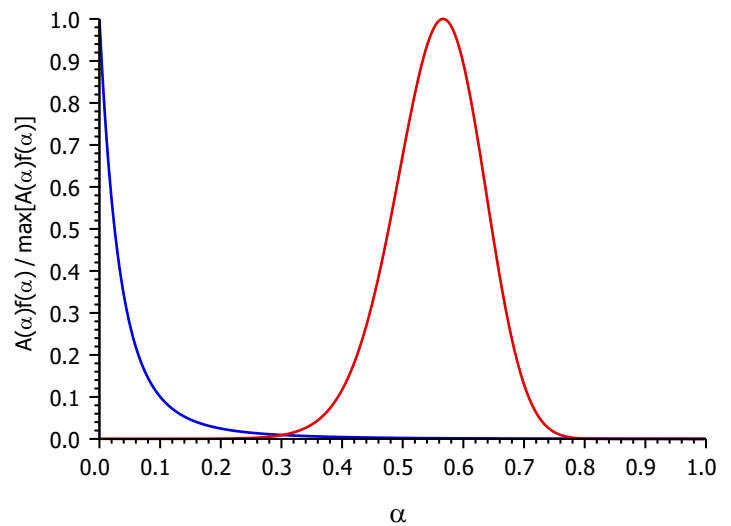
$$\log_{10}\tilde{A}(0)= 17.10 \quad E(0)= 201.4 \quad \log_{10}\tilde{A}(1)= 14.16 \quad E(1)= 201.4$$

$$\text{mean } \log_{10}\tilde{A}= 15.05 \quad \text{mean } E= 201.4$$

Parameter file: B\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 11.87 \quad E(0)= 149.1 \quad \log_{10}\tilde{A}(1)= 2.29 \quad E(1)= 71.2$$

$$\text{mean } \log_{10}\tilde{A}= 12.81 \quad \text{mean } E= 178.1$$



#### Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]

Parameter file: B\_0,5\_oneC.PAR

$$A(0)f(0)= 1.256E+17 \quad E(0)= 201.4 \quad A(1)f(1)= 0.00 \quad E(1)= 201.4$$

$$\text{mean } A(\alpha)f(\alpha)= 5.498E+15 \quad \text{mean } E= 201.4$$

$$\text{max } A(\alpha)f(\alpha)= 1.256E+17 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 201.4$$

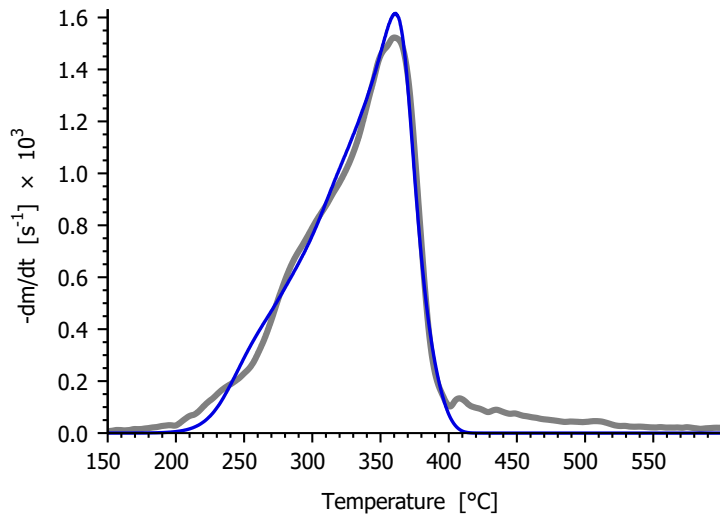
Parameter file: B\_3,5\_oneC.PAR

$$A(0)f(0)= 7.339E+11 \quad E(0)= 149.1 \quad A(1)f(1)= 0.00 \quad E(1)= 71.2$$

$$\text{mean } A(\alpha)f(\alpha)= 4.718E+14 \quad \text{mean } E= 178.1$$

$$\text{max } A(\alpha)f(\alpha)= 2.585E+15 \quad \text{at } \alpha= 0.567 \quad \text{and } E= 216.2$$

Figures illustrating the fit quality (cf. Figure 10 in reference [S1])



**Black locust shoots, 10°C/min**

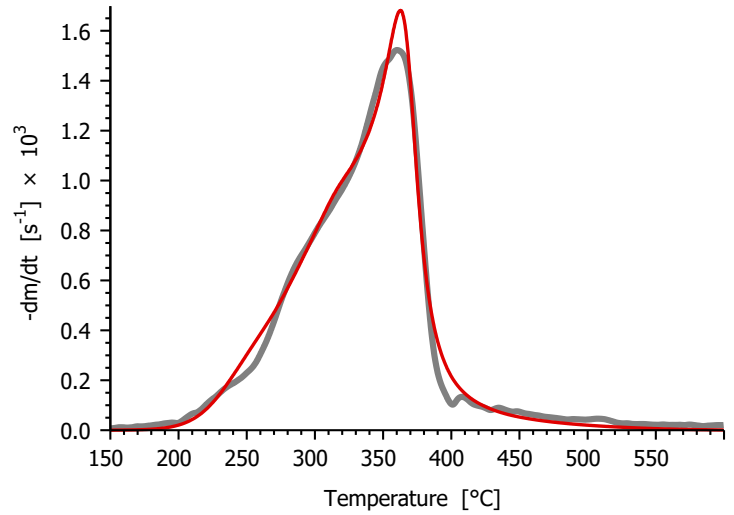
Relative deviation: 3.32%, Deviation: 0.20 µg/s  
rms rel. dev. of 4 experiments: 3.11%

Model:  $x=2\alpha-1$

$E(x) = 201.39$

$\log_{10} \tilde{A}(x) = 15.189T_0(x) - 1.21T_1(x) + .431T_2(x) - .208T_3(x) + .009T_4(x) - .05T_5(x)$

$c = 0.788$



**Black locust shoots, 10°C/min**

Relative deviation: 2.82%, Deviation: 0.17 µg/s  
rms rel. dev. of 4 experiments: 2.65%

Model:  $x=2\alpha-1$

$E(x) = 161.12T_0(x) - 17.66T_1(x) - 50.94T_2(x) - 21.29T_3(x)$

$\log_{10} \tilde{A}(x) = 11.398T_0(x) - 2.632T_1(x) - 4.233T_2(x) - 2.038T_3(x) - .088T_4(x) - .12T_5(x)$

$c = 0.851$

## S1.2. Poplar shoots

### Model with constant E:

Input file: "P\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 207.00457$$

$$\log_{10}\tilde{A}(x)= 15.09038 - .657046x + 1.360278x^2 - .238448x^3 - 2.281232x^4 - 2.317552x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 14.915057T_0(x) - 2.284352T_1(x) - .460477T_2(x) - .783847T_3(x) - .285154T_4(x) - .144847T_5(x)$$

### Model with third order E( $\alpha$ ):

Input file: "P\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

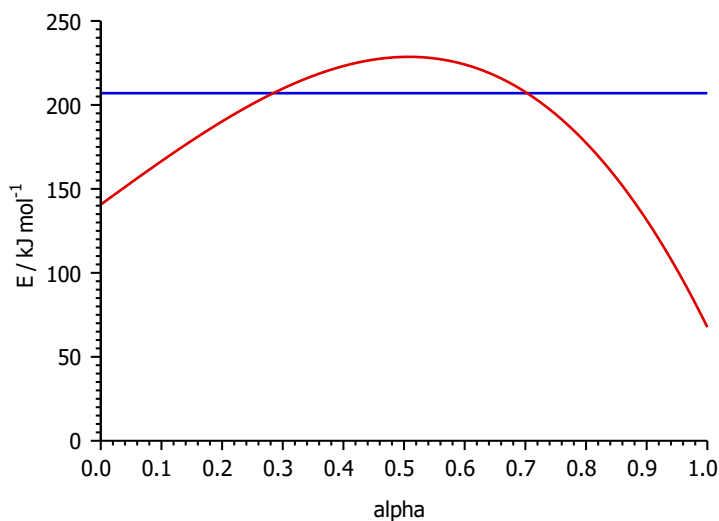
$$E(x)= 228.59258 + 3.95597x - 124.41916x^2 - 40.45308x^3$$

$$\log_{10}\tilde{A}(x)= 16.905634 - .453547x - 9.157212x^2 - 3.179244x^3 - 2.015672x^4 - 1.364736x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 166.383T_0(x) - 26.38384T_1(x) - 62.20958T_2(x) - 10.11327T_3(x)$$

$$\log_{10}\tilde{A}(x)= 11.571151T_0(x) - 3.69094T_1(x) - 5.586442T_2(x) - 1.221291T_3(x) - .251959T_4(x) - .085296T_5(x)$$



**E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)**

Parameter file: P\_0,5\_oneC.PAR

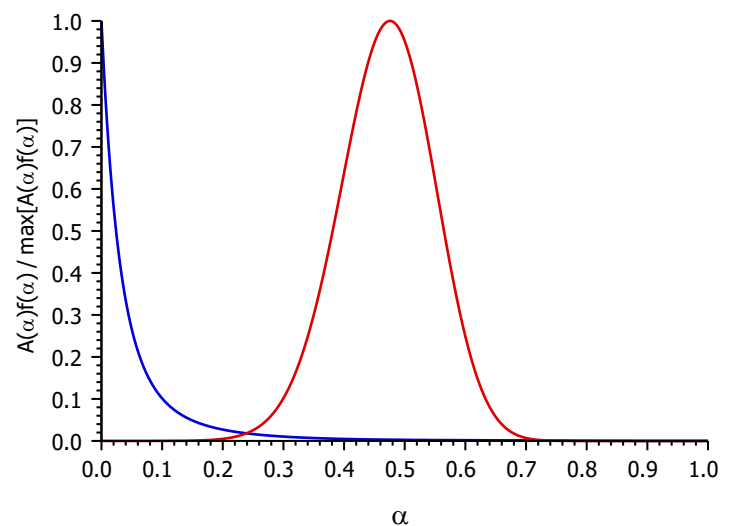
$$\log_{10}\tilde{A}(0)= 17.38 \quad E(0)= 207.0 \quad \log_{10}\tilde{A}(1)= 10.96 \quad E(1)= 207.0$$

$$\text{mean } \log_{10}\tilde{A}= 15.09 \quad \text{mean } E= 207.0$$

Parameter file: P\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 10.73 \quad E(0)= 140.7 \quad \log_{10}\tilde{A}(1)= 0.74 \quad E(1)= 67.7$$

$$\text{mean } \log_{10}\tilde{A}= 13.45 \quad \text{mean } E= 187.1$$



**Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]**

Parameter file: P\_0,5\_oneC.PAR

$$A(0)f(0)= 2.413E+17 \quad E(0)= 207.0 \quad A(1)f(1)= 0.00 \quad E(1)= 207.0$$

$$\text{mean } A(\alpha)f(\alpha)= 1.053E+16 \quad \text{mean } E= 207.0$$

$$\text{max } A(\alpha)f(\alpha)= 2.413E+17 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 207.0$$

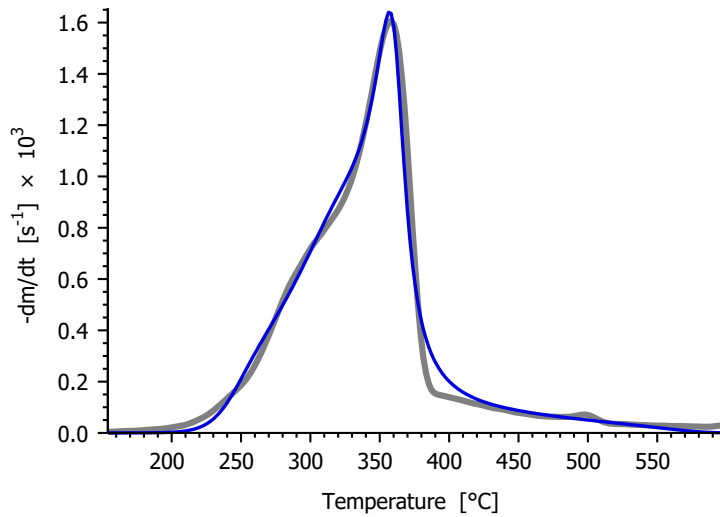
Parameter file: P\_3,5\_oneC.PAR

$$A(0)f(0)= 5.374E+10 \quad E(0)= 140.7 \quad A(1)f(1)= 0.00 \quad E(1)= 67.7$$

$$\text{mean } A(\alpha)f(\alpha)= 8.250E+15 \quad \text{mean } E= 187.1$$

$$\text{max } A(\alpha)f(\alpha)= 4.227E+16 \quad \text{at } \alpha= 0.476 \quad \text{and } E= 228.1$$

Figures illustrating the fit quality (cf. Figure 10 in reference [S1])



**Poplar shoots, 10°C/min**

Relative deviation: 2.95%, Deviation: 0.18 µg/s

rms rel. dev. of 4 experiments: 3.78%

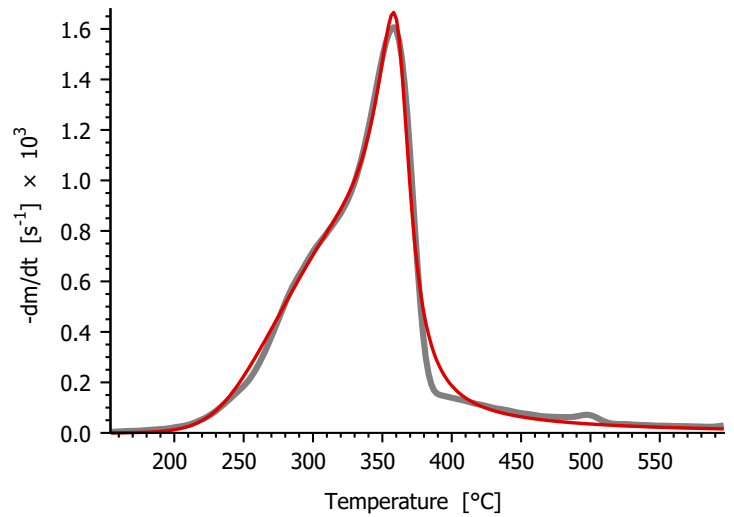
Model:  $x=2\alpha-1$

$E(x) = 207.0$

$\log_{10} \tilde{A}(x) = 14.915T_0(x) - 2.284T_1(x) - .46T_2(x) - .784T_3(x)$

$- .285T_4(x) - .145T_5(x)$

$c = 0.791$



**Poplar shoots, 10°C/min**

Relative deviation: 2.24%, Deviation: 0.14 µg/s

rms rel. dev. of 4 experiments: 3.13%

Model:  $x=2\alpha-1$

$E(x) = 166.38T_0(x) - 26.38T_1(x) - 62.21T_2(x) - 10.11T_3(x)$

$\log_{10} \tilde{A}(x) = 11.571T_0(x) - 3.691T_1(x) - 5.586T_2(x) - 1.221T_3(x)$

$- .252T_4(x) - .085T_5(x)$

$c = 0.804$



### S1.3. Willow shoots

#### Model with constant E:

Input file: "W\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 192.30365$$

$$\log_{10}\tilde{A}(x)= 13.872239 - .914686x + 1.330912x^2 + .955792x^3 - 1.563432x^4 - 2.8156x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 13.951408T_0(x) - 1.957592T_1(x) - .11626T_2(x) - .640927T_3(x) - .195429T_4(x) - .175975T_5(x)$$

#### Model with third order E( $\alpha$ ):

Input file: "W\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

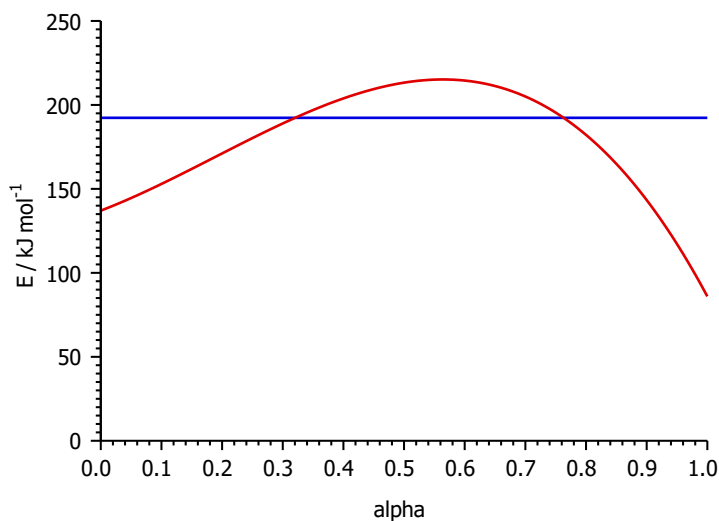
$$E(x)= 213.26372 + 28.74274x - 101.7404x^2 - 54.27984x^3$$

$$\log_{10}\tilde{A}(x)= 15.633178 + 1.380063x - 7.413694x^2 - 3.175292x^3 - 1.403592x^4 - 2.098592x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 162.39352T_0(x) - 11.96714T_1(x) - 50.8702T_2(x) - 13.56996T_3(x)$$

$$\log_{10}\tilde{A}(x)= 11.399984T_0(x) - 2.313026T_1(x) - 4.408643T_2(x) - 1.449633T_3(x) - .175449T_4(x) - .131162T_5(x)$$



#### E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)

Parameter file: W\_0,5\_oneC.PAR

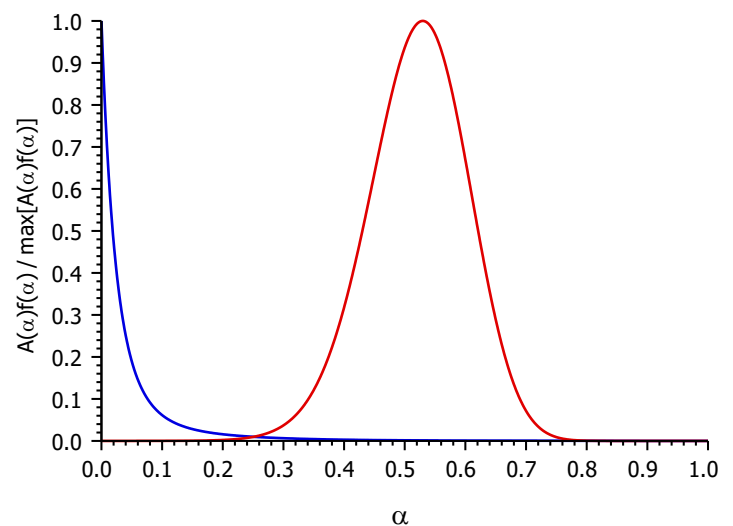
$$\log_{10}\tilde{A}(0)= 16.41 \quad E(0)= 192.3 \quad \log_{10}\tilde{A}(1)= 10.87 \quad E(1)= 192.3$$

$$\text{mean } \log_{10}\tilde{A}= 14.00 \quad \text{mean } E= 192.3$$

Parameter file: W\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 10.71 \quad E(0)= 137.1 \quad \log_{10}\tilde{A}(1)= 2.92 \quad E(1)= 86.0$$

$$\text{mean } \log_{10}\tilde{A}= 12.88 \quad \text{mean } E= 179.3$$



#### Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]

Parameter file: W\_0,5\_oneC.PAR

$$A(0)f(0)= 2.595E+16 \quad E(0)= 192.3 \quad A(1)f(1)= 0.00 \quad E(1)= 192.3$$

$$\text{mean } A(\alpha)f(\alpha)= 8.746E+14 \quad \text{mean } E= 192.3$$

$$\text{max } A(\alpha)f(\alpha)= 2.595E+16 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 192.3$$

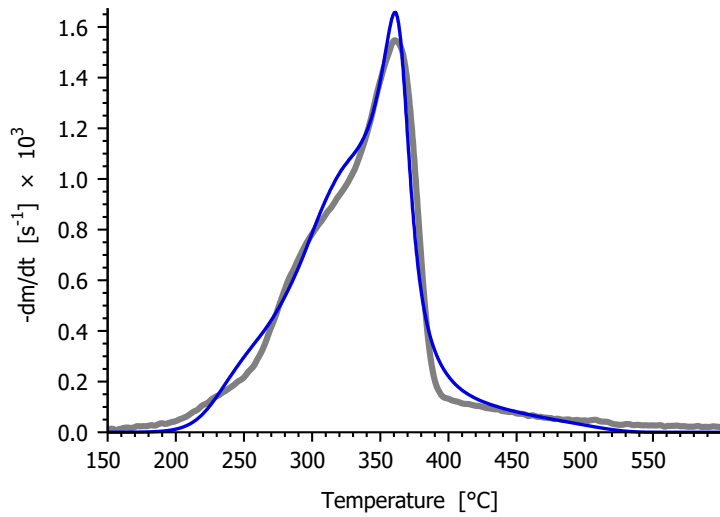
Parameter file: W\_3,5\_oneC.PAR

$$A(0)f(0)= 5.125E+10 \quad E(0)= 137.1 \quad A(1)f(1)= 0.00 \quad E(1)= 86.0$$

$$\text{mean } A(\alpha)f(\alpha)= 4.668E+14 \quad \text{mean } E= 179.3$$

$$\text{max } A(\alpha)f(\alpha)= 2.294E+15 \quad \text{at } \alpha= 0.530 \quad \text{and } E= 214.6$$

Figures illustrating the fit quality (cf. Figure 10 in reference [S1])



**Willow shoots, 10°C/min**

Relative deviation: 3.66%, Deviation: 0.23 µg/s

rms rel. dev. of 4 experiments: 3.42%

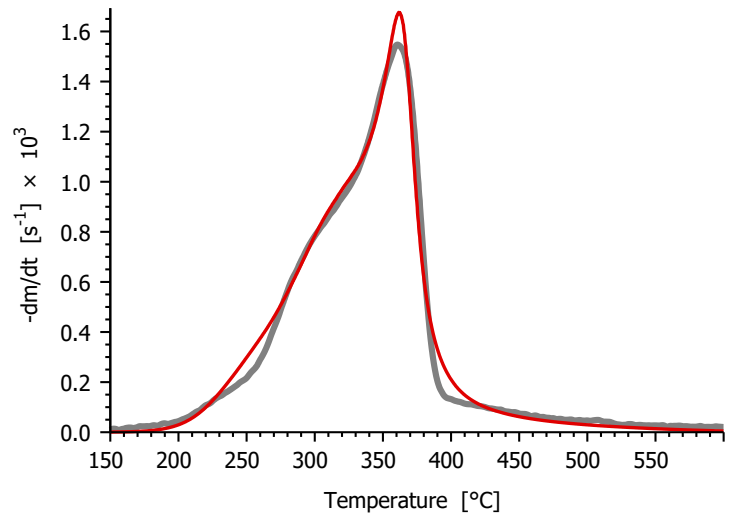
Model:  $x=2\alpha-1$

$E(x) = 192.3$

$\log_{10} \tilde{A}(x) = 13.951T_0(x) - 1.958T_1(x) - .116T_2(x) - .641T_3(x)$

$-.195T_4(x) - .176T_5(x)$

$c = 0.831$



**Willow shoots, 10°C/min**

Relative deviation: 2.72%, Deviation: 0.17 µg/s

rms rel. dev. of 4 experiments: 2.74%

Model:  $x=2\alpha-1$

$E(x) = 162.39T_0(x) - 11.97T_1(x) - 50.87T_2(x) - 13.57T_3(x)$

$\log_{10} \tilde{A}(x) = 11.4T_0(x) - 2.313T_1(x) - 4.409T_2(x) - 1.45T_3(x)$

$-.175T_4(x) - .131T_5(x)$

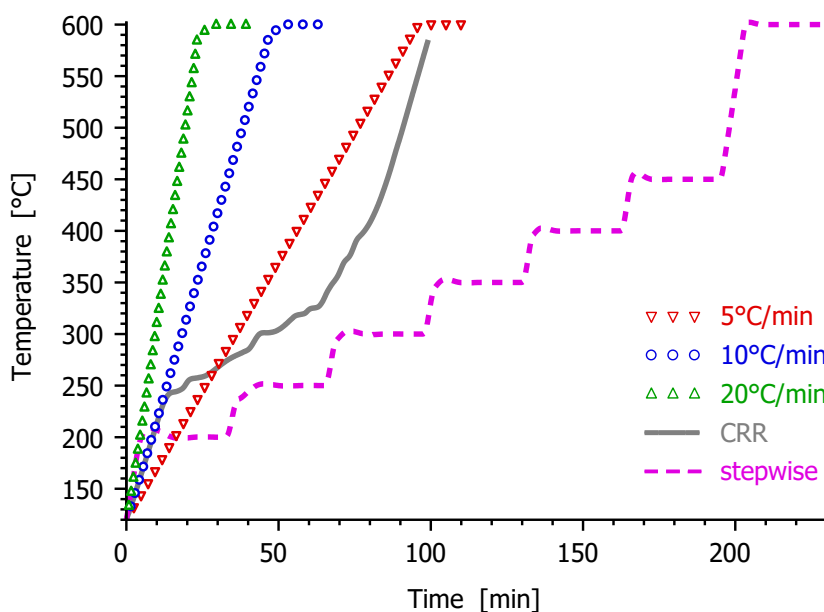
$c = 0.841$

## S2. Industrial Biomass Wastes

Source of the data:

[S2] Becidan, M.; Várhegyi, G.; Hustad, J. E.; Skreiberg, Ø.: Thermal decomposition of biomass wastes. A kinetic study. *Ind. Eng. Chem. Res.* **2007**, *46*, 2428-2437. doi: [10.1021/ie061468z](https://doi.org/10.1021/ie061468z) [Repository](#)

Five TGA experiments were available for each sample. The figure below shows the corresponding temperature programs. It is a redrawn/rearranged version of Figure 1 of the cited paper. Please note that the CRR (“constant reaction rate”) programs were determined by the apparatus separately for each sample. The one in Figure S2.1 belongs to the brewer spent grains.



**Figure S2.1:** Temperature programs used for the TGA experiments of this section.

## S2.1. Brewer spent grains

### Model with constant E:

Input file: "B\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 205.49138$$

$$\log_{10}\tilde{A}(x)= 15.480744 -1.943698x +.876088x^2 +.930456x^3 -2.606512x^4 -3.164768x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 14.941346T_0(x) -3.223836T_1(x) -.865212T_2(x) -.756376T_3(x) -.325814T_4(x) -.197798T_5(x)$$

### Model with third order E( $\alpha$ ):

Input file: "B\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

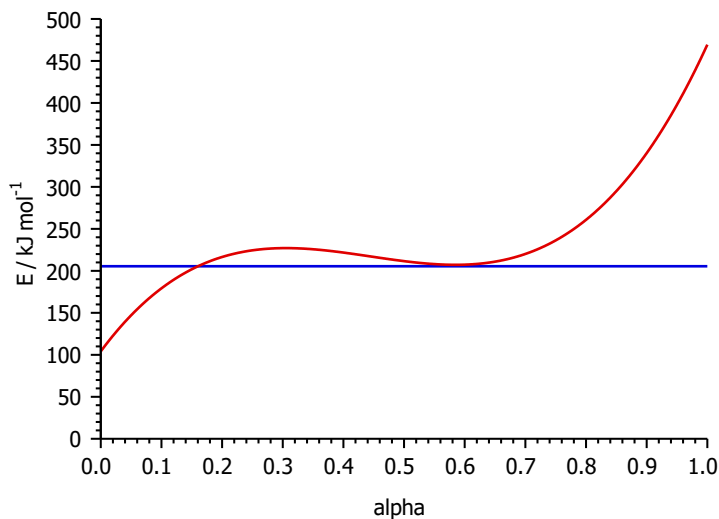
$$E(x)= 211.563722 -45.096816x +75.199396x^2 +227.735488x^3$$

$$\log_{10}\tilde{A}(x)= 16.038065 -6.0397905x +8.675692x^2 +20.7184024x^3 -6.172224x^4 -3.687408x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 249.16342T_0(x) +125.7048T_1(x) +37.599698T_2(x) +56.933872T_3(x)$$

$$\log_{10}\tilde{A}(x)= 18.061327T_0(x) +7.1943813T_1(x) +1.251734T_2(x) +4.0272856T_3(x) -.771528T_4(x) -.230463T_5(x)$$



#### E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)

Parameter file: B\_0,5\_oneC.PAR

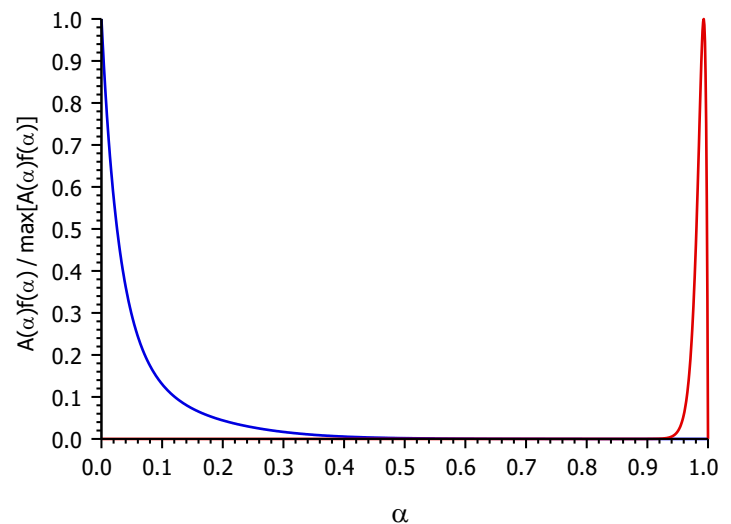
$$\log_{10}\tilde{A}(0)= 17.93 \quad E(0)= 205.5 \quad \log_{10}\tilde{A}(1)= 9.57 \quad E(1)= 205.5$$

$$\text{mean } \log_{10}\tilde{A}= 15.25 \quad \text{mean } E= 205.5$$

Parameter file: B\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 7.55 \quad E(0)= 104.1 \quad \log_{10}\tilde{A}(1)= 29.53 \quad E(1)= 469.4$$

$$\text{mean } \log_{10}\tilde{A}= 17.70 \quad \text{mean } E= 236.6$$



#### Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]

Parameter file: B\_0,5\_oneC.PAR

$$A(0)f(0)= 8.479E+17 \quad E(0)= 205.5 \quad A(1)f(1)= 0.00 \quad E(1)= 205.5$$

$$\text{mean } A(\alpha)f(\alpha)= 4.205E+16 \quad \text{mean } E= 205.5$$

$$\text{max } A(\alpha)f(\alpha)= 8.479E+17 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 205.5$$

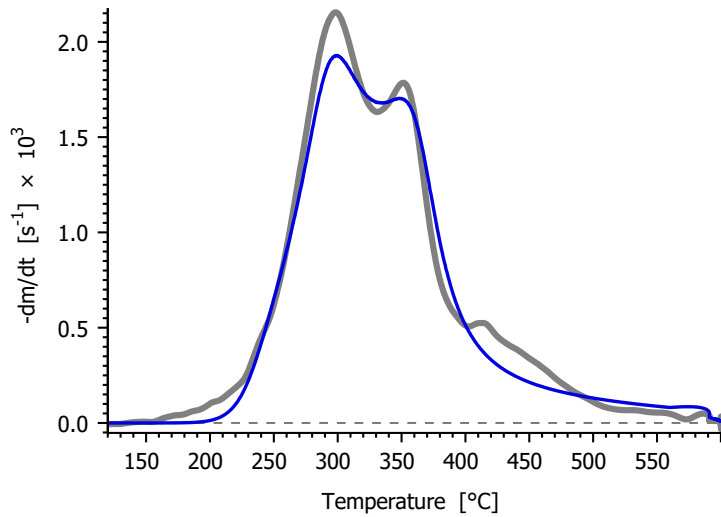
Parameter file: B\_3,5\_oneC.PAR

$$A(0)f(0)= 3.551E+07 \quad E(0)= 104.1 \quad A(1)f(1)= 0.00 \quad E(1)= 469.4$$

$$\text{mean } A(\alpha)f(\alpha)= 1.742E+25 \quad \text{mean } E= 236.6$$

$$\text{max } A(\alpha)f(\alpha)= 8.967E+26 \quad \text{at } \alpha= 0.993 \quad \text{and } E= 458.4$$

Figures illustrating the fit quality (cf. Figure 4 in reference [S2])



**Brewer spent grains, 20°C/min**

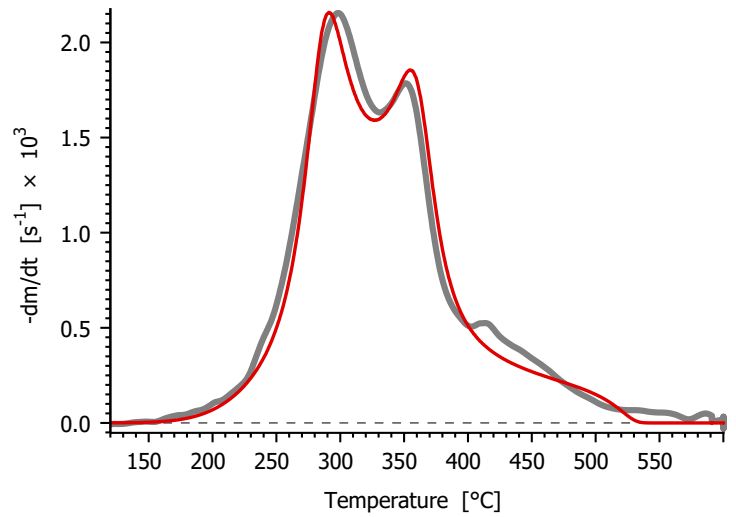
Relative deviation: 3.22%, Deviation: 0.18 µg/s  
rms rel. dev. of 5 experiments: 5.28%

Model:  $x=2\alpha-1$

$E(x) = 205.49$

$\log_{10} \tilde{A}(x) = 14.941T_0(x) - 3.224T_1(x) - 0.865T_2(x) - 0.756T_3(x) - 0.326T_4(x) - 0.198T_5(x)$

$c = 0.759$



**Brewer spent grains, 20°C/min**

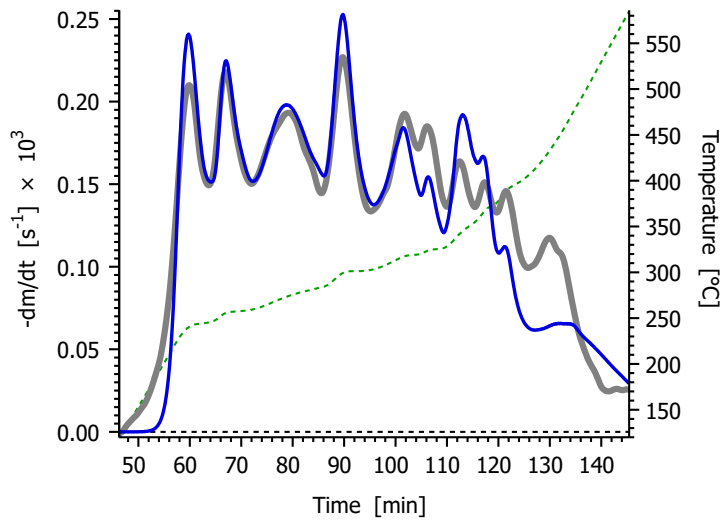
Relative deviation: 3.01%, Deviation: 0.17 µg/s  
rms rel. dev. of 5 experiments: 3.94%

Model:  $x=2\alpha-1$

$E(x) = 249.16T_0(x) + 125.7T_1(x) + 37.6T_2(x) + 56.93T_3(x)$

$\log_{10} \tilde{A}(x) = 18.061T_0(x) + 7.194T_1(x) + 1.252T_2(x) + 4.027T_3(x) - 0.772T_4(x) - 0.23T_5(x)$

$c = 0.758$



**Brewer spent grains, "constant reaction rate" (CRR)**

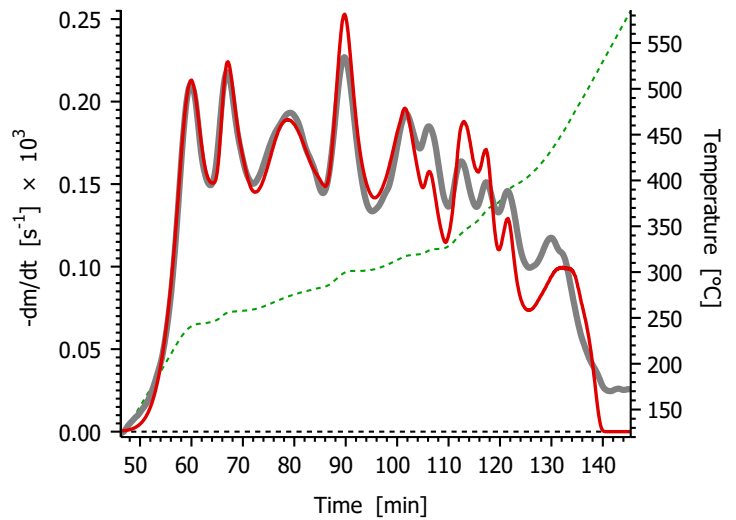
Relative deviation: 9.64%, Deviation: 0.10 µg/s  
rms rel. dev. of 5 experiments: 5.28%

Model:  $x=2\alpha-1$

$E(x) = 205.49$

$\log_{10} \tilde{A}(x) = 14.941T_0(x) - 3.224T_1(x) - 0.865T_2(x) - 0.756T_3(x) - 0.326T_4(x) - 0.198T_5(x)$

$c = 0.759$



**Brewer spent grains, "constant reaction rate" (CRR)**

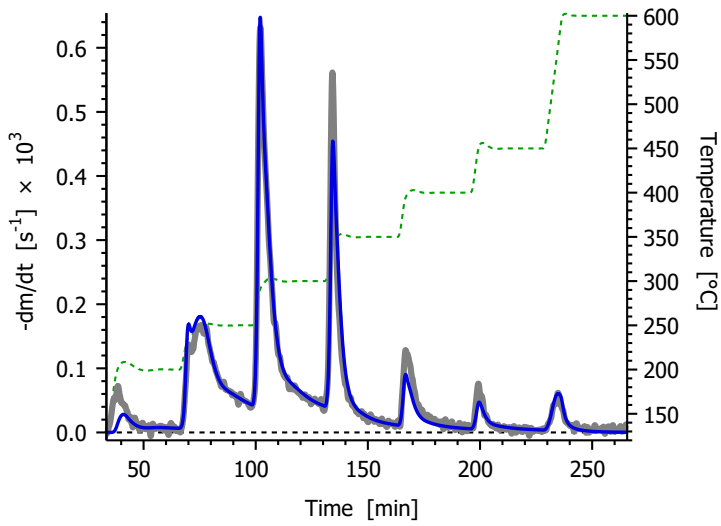
Relative deviation: 6.87%, Deviation: 0.073 µg/s  
rms rel. dev. of 5 experiments: 3.94%

Model:  $x=2\alpha-1$

$E(x) = 249.16T_0(x) + 125.7T_1(x) + 37.6T_2(x) + 56.93T_3(x)$

$\log_{10} \tilde{A}(x) = 18.061T_0(x) + 7.194T_1(x) + 1.252T_2(x) + 4.027T_3(x) - 0.772T_4(x) - 0.23T_5(x)$

$c = 0.758$


**Brewer spent grains, Stepwise T(t)**

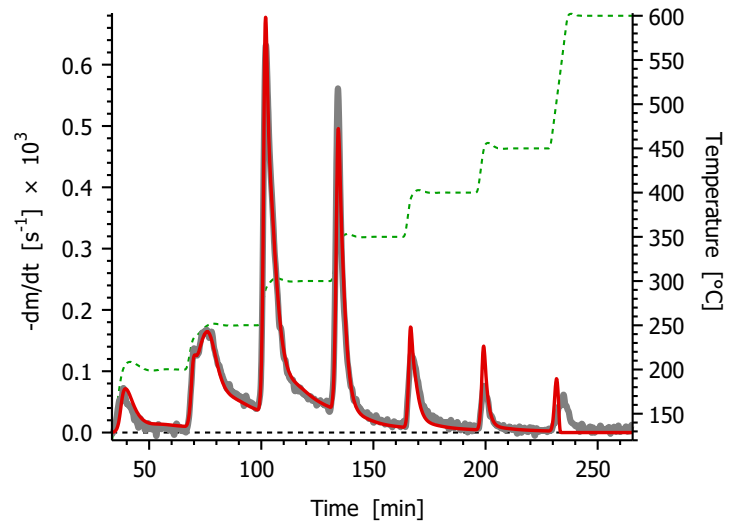
Relative deviation: 2.55%, Deviation: 0.078  $\mu\text{g/s}$   
 rms rel. dev. of 5 experiments: 5.28%

Model:  $x=2\alpha-1$

$E(x) = 205.49$

$\log_{10} \tilde{A}(x) = 14.941T_0(x) - 3.224T_1(x) - .865T_2(x) - .756T_3(x)$   
 $- .326T_4(x) - .198T_5(x)$

$c = 0.759$


**Brewer spent grains, Stepwise T(t)**

Relative deviation: 2.44%, Deviation: 0.075  $\mu\text{g/s}$   
 rms rel. dev. of 5 experiments: 3.94%

Model:  $x=2\alpha-1$

$E(x) = 249.16T_0(x) + 125.7T_1(x) + 37.6T_2(x) + 56.93T_3(x)$

$\log_{10} \tilde{A}(x) = 18.061T_0(x) + 7.194T_1(x) + 1.252T_2(x) + 4.027T_3(x)$   
 $- .772T_4(x) - .23T_5(x)$

$c = 0.758$

## S2.2. Coffee waste

### Model with constant E:

Input file: "C\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 206.20704$$

$$\log_{10}\tilde{A}(x)= 15.69215 -1.090325x - .199498x^2 -3.290896x^3 -1.54684x^4 - .204288x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 15.012336T_0(x) -3.686177T_1(x) - .873169T_2(x) - .886564T_3(x) - .193355T_4(x) - .012768T_5(x)$$

### Model with third order E( $\alpha$ ):

Input file: "C\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

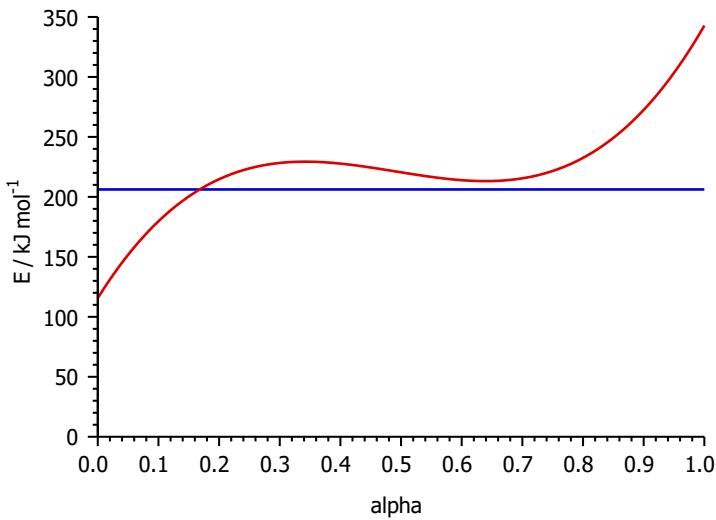
$$E(x)= 220.4857005 -40.704909x +8.731879x^2 +154.29576x^3$$

$$\log_{10}\tilde{A}(x)= 17.015448 -4.8389645x +1.855026x^2 +10.371016x^3 -4.78824x^4 - .356224x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 224.85164T_0(x) +75.016911T_1(x) +4.3659395T_2(x) +38.57394T_3(x)$$

$$\log_{10}\tilde{A}(x)= 16.147371T_0(x) +2.7166575T_1(x) -1.466607T_2(x) +2.481434T_3(x) - .59853T_4(x) - .022264T_5(x)$$



#### E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)

Parameter file: C\_0,5\_oneC.PAR

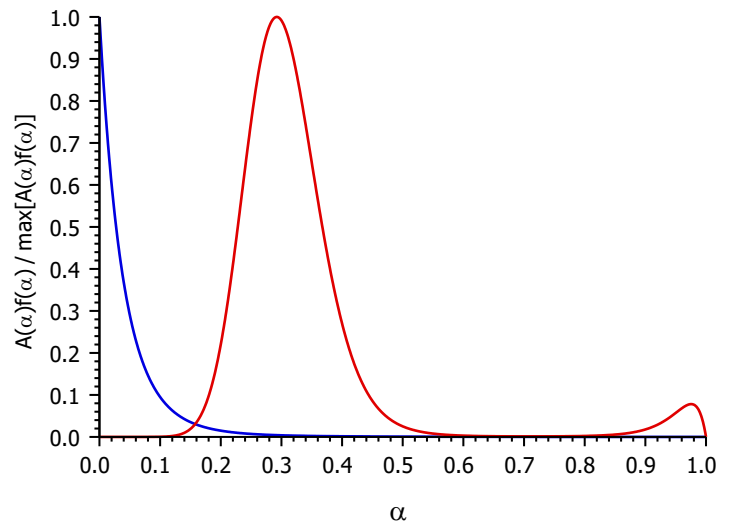
$$\log_{10}\tilde{A}(0)= 18.53 \quad E(0)= 206.2 \quad \log_{10}\tilde{A}(1)= 9.36 \quad E(1)= 206.2$$

$$\text{mean } \log_{10}\tilde{A}= 15.32 \quad \text{mean } E= 206.2$$

Parameter file: C\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 8.91 \quad E(0)= 115.6 \quad \log_{10}\tilde{A}(1)= 19.26 \quad E(1)= 342.8$$

$$\text{mean } \log_{10}\tilde{A}= 16.68 \quad \text{mean } E= 223.4$$



#### Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]

Parameter file: C\_0,5\_oneC.PAR

$$A(0)f(0)= 3.399E+18 \quad E(0)= 206.2 \quad A(1)f(1)= 0.00 \quad E(1)= 206.2$$

$$\text{mean } A(\alpha)f(\alpha)= 1.444E+17 \quad \text{mean } E= 206.2$$

$$\text{max } A(\alpha)f(\alpha)= 3.399E+18 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 206.2$$

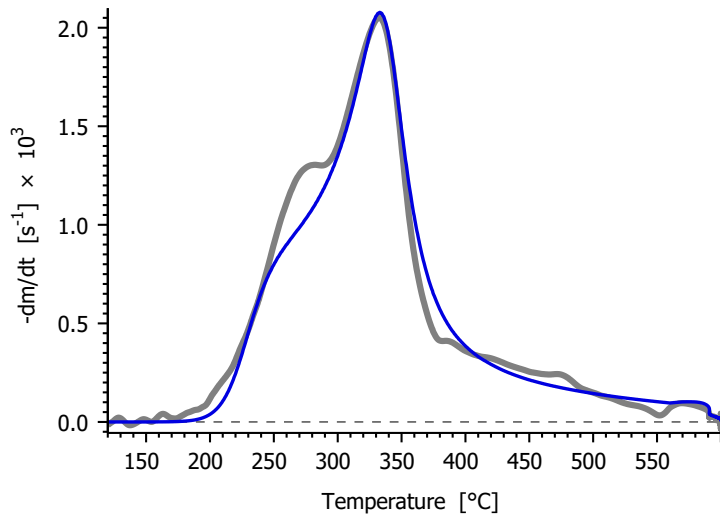
Parameter file: C\_3,5\_oneC.PAR

$$A(0)f(0)= 8.061E+08 \quad E(0)= 115.6 \quad A(1)f(1)= 0.00 \quad E(1)= 342.8$$

$$\text{mean } A(\alpha)f(\alpha)= 3.238E+17 \quad \text{mean } E= 223.4$$

$$\text{max } A(\alpha)f(\alpha)= 2.060E+18 \quad \text{at } \alpha= 0.292 \quad \text{and } E= 227.8$$

Figures illustrating the fit quality (cf. Figure 5 in reference [S2])


**Coffee waste, 20°C/min**

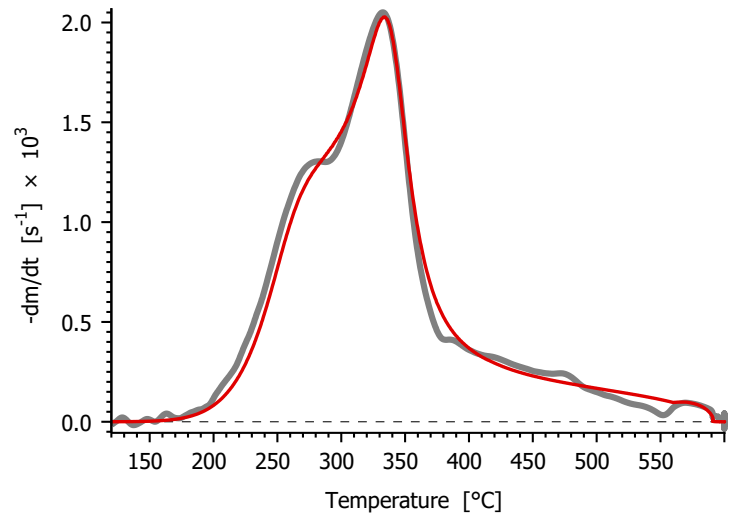
Relative deviation: 3.22%, Deviation: 0.16 µg/s  
rms rel. dev. of 5 experiments: 3.76%

Model:  $x=2\alpha-1$

$E(x) = 206.21$

$\log_{10} \ddot{A}(x) = 15.012T_0(x) - 3.686T_1(x) - .873T_2(x) - .887T_3(x) - .193T_4(x) - .013T_5(x)$

$c = 0.689$


**Coffee waste, 20°C/min**

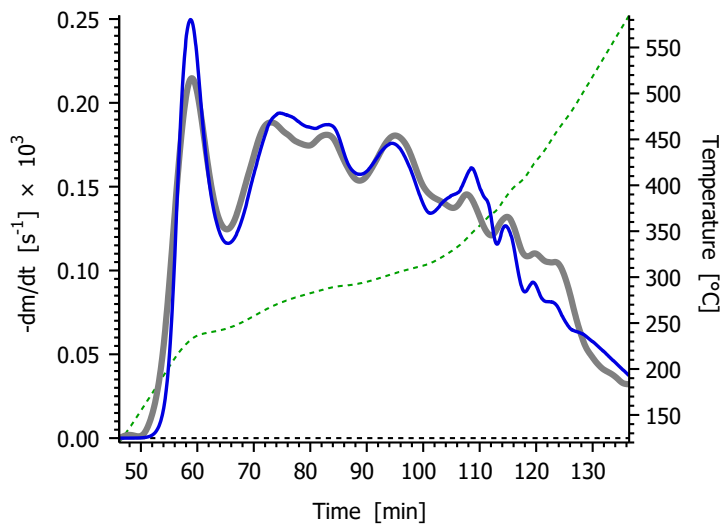
Relative deviation: 2.22%, Deviation: 0.11 µg/s  
rms rel. dev. of 5 experiments: 2.65%

Model:  $x=2\alpha-1$

$E(x) = 224.85T_0(x) + 75.02T_1(x) + 4.37T_2(x) + 38.57T_3(x)$

$\log_{10} \ddot{A}(x) = 16.147T_0(x) + 2.717T_1(x) - 1.467T_2(x) + 2.481T_3(x) - .599T_4(x) - .022T_5(x)$

$c = 0.687$


**Coffee waste, "constant reaction rate" (CRR)**

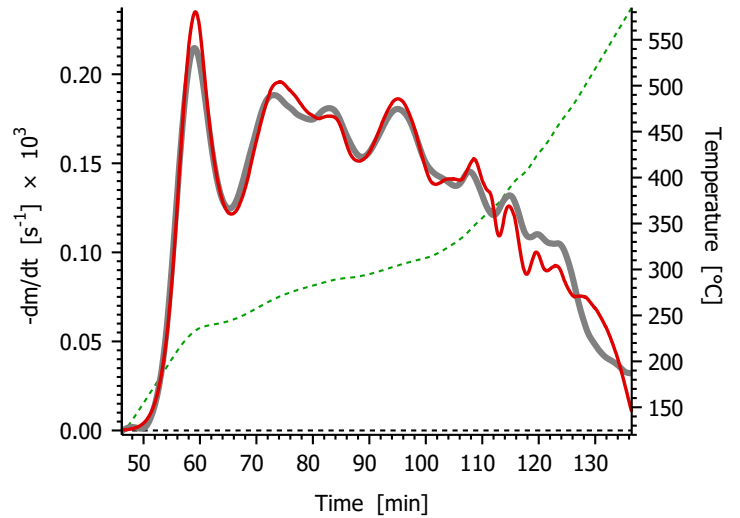
Relative deviation: 6.57%, Deviation: 0.069 µg/s  
rms rel. dev. of 5 experiments: 3.76%

Model:  $x=2\alpha-1$

$E(x) = 206.21$

$\log_{10} \ddot{A}(x) = 15.012T_0(x) - 3.686T_1(x) - .873T_2(x) - .887T_3(x) - .193T_4(x) - .013T_5(x)$

$c = 0.689$


**Coffee waste, "constant reaction rate" (CRR)**

Relative deviation: 4.24%, Deviation: 0.045 µg/s  
rms rel. dev. of 5 experiments: 2.65%

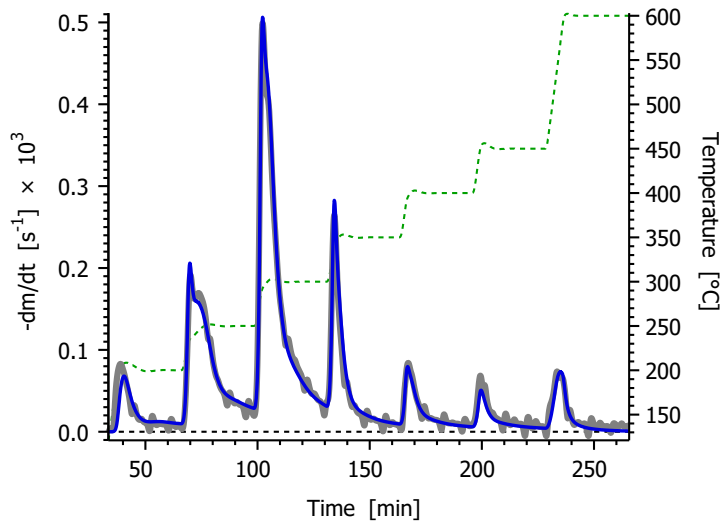
Model:  $x=2\alpha-1$

$E(x) = 224.85T_0(x) + 75.02T_1(x) + 4.37T_2(x) + 38.57T_3(x)$

$\log_{10} \ddot{A}(x) = 16.147T_0(x) + 2.717T_1(x) - 1.467T_2(x) + 2.481T_3(x) - .599T_4(x) - .022T_5(x)$

$c = 0.687$





**Coffee waste, Stepwise T(t)**

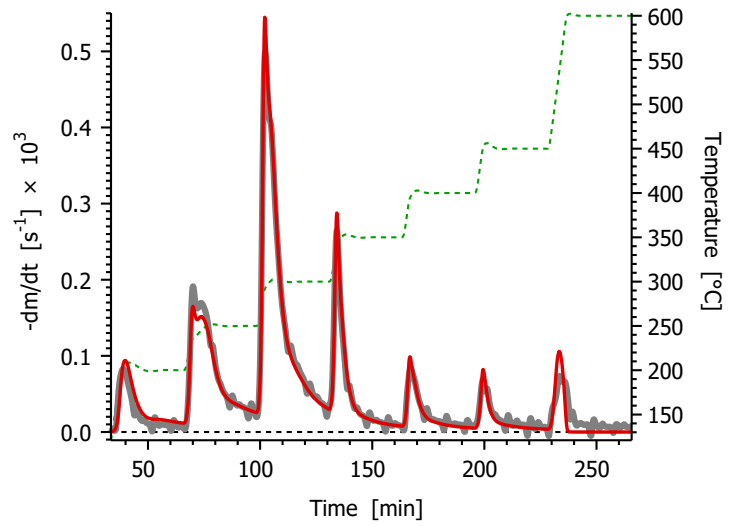
Relative deviation: 2.03%, Deviation: 0.050 µg/s  
rms rel. dev. of 5 experiments: 3.76%

Model:  $x=2\alpha-1$

$E(x) = 206.21$

$\log_{10} \tilde{A}(x) = 15.012T_0(x) - 3.686T_1(x) - .873T_2(x) - .887T_3(x)$   
 $- .193T_4(x) - .013T_5(x)$

$c = 0.689$



**Coffee waste, Stepwise T(t)**

Relative deviation: 2.17%, Deviation: 0.053 µg/s  
rms rel. dev. of 5 experiments: 2.65%

Model:  $x=2\alpha-1$

$E(x) = 224.85T_0(x) + 75.02T_1(x) + 4.37T_2(x) + 38.57T_3(x)$

$\log_{10} \tilde{A}(x) = 16.147T_0(x) + 2.717T_1(x) - 1.467T_2(x) + 2.481T_3(x)$   
 $- .599T_4(x) - .022T_5(x)$

$c = 0.687$

### S2.3. Medium density fiberboard

#### Model with constant E:

Input file: "F\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 178.76916$$

$$\log_{10}\tilde{A}(x)= 12.799454 - .925107x + 1.25016x^2 + 1.629328x^3 - 1.983728x^4 - 4.327232x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 12.680636T_0(x) - 2.407631T_1(x) - .366784T_2(x) - .944928T_3(x) - .247966T_4(x) - .270452T_5(x)$$

#### Model with third order E(α):

Input file: "F\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

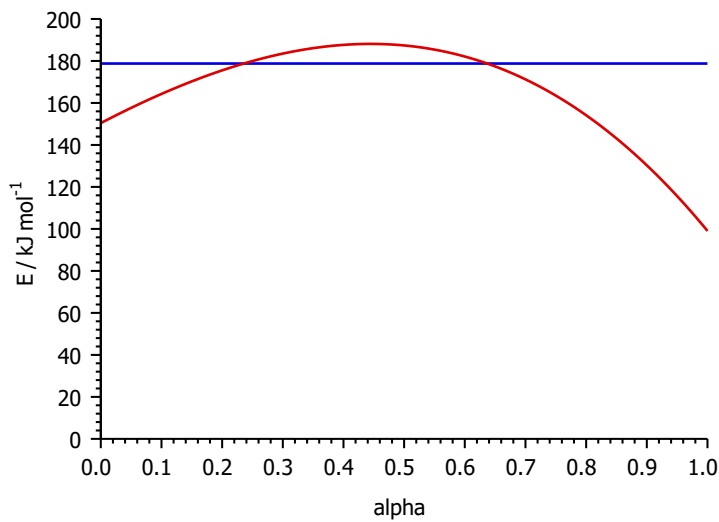
$$E(x)= 187.38753 - 13.38397x - 62.65204x^2 - 12.29512x^3$$

$$\log_{10}\tilde{A}(x)= 13.555281 - 2.124616x - 4.26881x^2 + .462856x^3 - 1.82284x^4 - 3.499696x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 156.06151T_0(x) - 22.60531T_1(x) - 31.32602T_2(x) - 3.07378T_3(x)$$

$$\log_{10}\tilde{A}(x)= 10.737311T_0(x) - 3.964784T_1(x) - 3.045825T_2(x) - .977941T_3(x) - .227855T_4(x) - .218731T_5(x)$$



#### E(α) = polynomial of (2α-1)

Parameter file: F\_0,5\_oneC.PAR

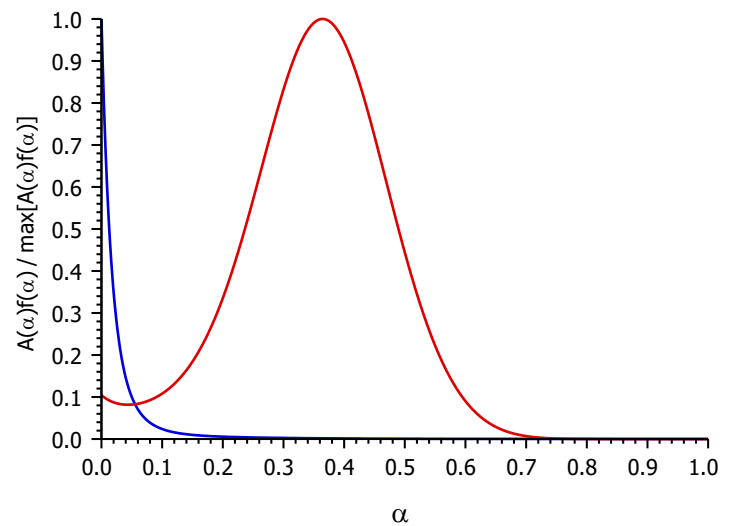
$$\log_{10}\tilde{A}(0)= 15.69 \quad E(0)= 178.8 \quad \log_{10}\tilde{A}(1)= 8.44 \quad E(1)= 178.8$$

$$\text{mean } \log_{10}\tilde{A}= 12.82 \quad \text{mean } E= 178.8$$

Parameter file: F\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 12.63 \quad E(0)= 150.4 \quad \log_{10}\tilde{A}(1)= 2.30 \quad E(1)= 99.1$$

$$\text{mean } \log_{10}\tilde{A}= 11.77 \quad \text{mean } E= 166.5$$



#### Plot of A(α)f(α) / max[A(α)f(α)]

Parameter file: F\_0,5\_oneC.PAR

$$A(0)f(0)= 4.885E+15 \quad E(0)= 178.8 \quad A(1)f(1)= 0.00 \quad E(1)= 178.8$$

$$\text{mean } A(\alpha)f(\alpha)= 1.097E+14 \quad \text{mean } E= 178.8$$

$$\text{max } A(\alpha)f(\alpha)= 4.885E+15 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 178.8$$

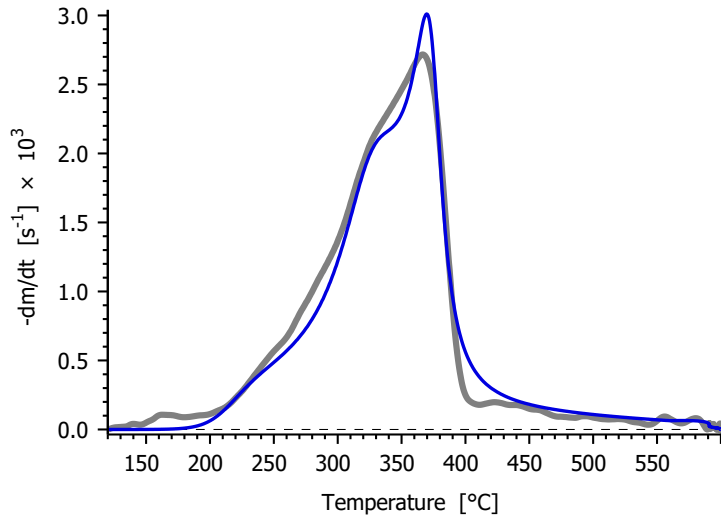
Parameter file: F\_3,5\_oneC.PAR

$$A(0)f(0)= 4.218E+12 \quad E(0)= 150.4 \quad A(1)f(1)= 0.00 \quad E(1)= 99.1$$

$$\text{mean } A(\alpha)f(\alpha)= 1.134E+13 \quad \text{mean } E= 166.5$$

$$\text{max } A(\alpha)f(\alpha)= 4.043E+13 \quad \text{at } \alpha= 0.364 \quad \text{and } E= 186.7$$

Figures illustrating the fit quality (cf. Figure 6 in reference [S2])



**Fiberboard, 20°C/min**

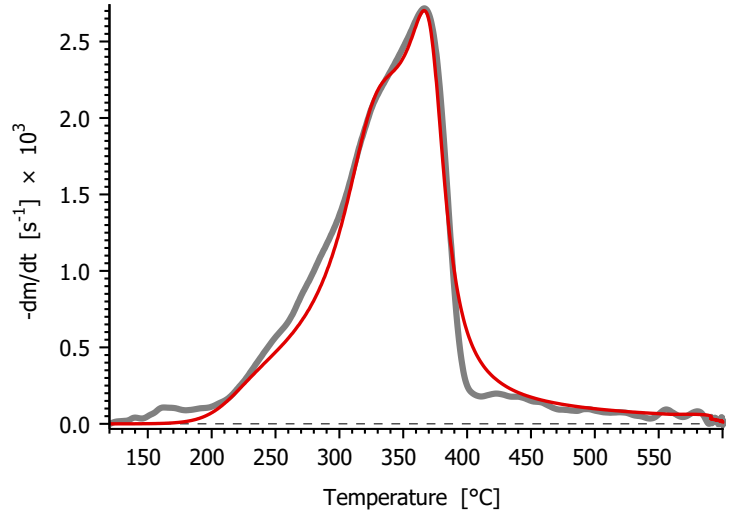
Relative deviation: 2.93%, Deviation: 0.20 µg/s  
rms rel. dev. of 5 experiments: 3.56%

Model:  $x=2\alpha-1$

$E(x) = 178.77$

$\log_{10} \tilde{A}(x) = 12.681T_0(x) - 2.408T_1(x) - .367T_2(x) - .945T_3(x) - .248T_4(x) - .27T_5(x)$

$c = 0.813$



**Fiberboard, 20°C/min**

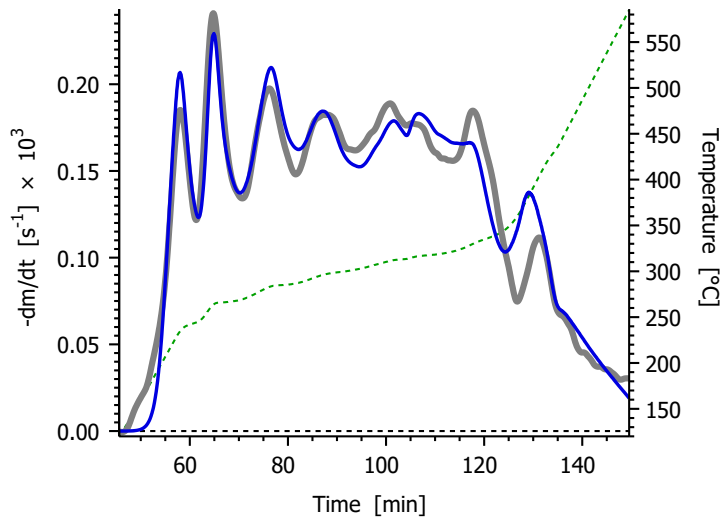
Relative deviation: 2.71%, Deviation: 0.18 µg/s  
rms rel. dev. of 5 experiments: 3.08%

Model:  $x=2\alpha-1$

$E(x) = 156.06T_0(x) - 22.61T_1(x) - 31.33T_2(x) - 3.07T_3(x)$

$\log_{10} \tilde{A}(x) = 10.737T_0(x) - 3.965T_1(x) - 3.046T_2(x) - .978T_3(x) - .228T_4(x) - .219T_5(x)$

$c = 0.827$



**Fiberboard, "constant reaction rate" (CRR)**

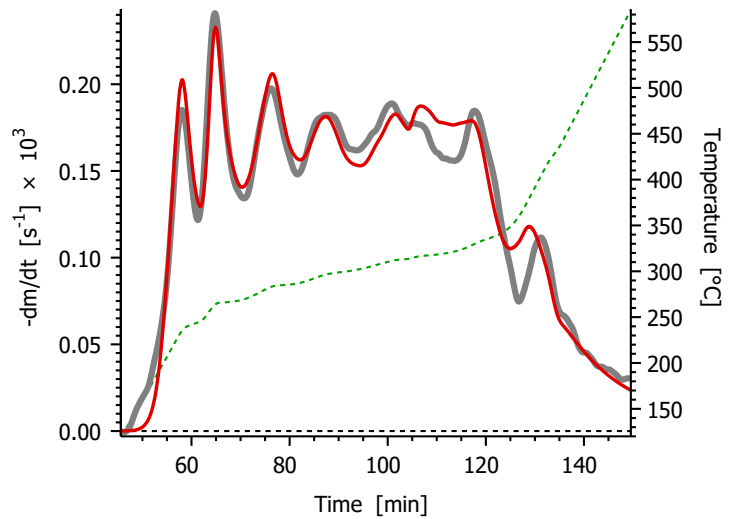
Relative deviation: 5.93%, Deviation: 0.067 µg/s  
rms rel. dev. of 5 experiments: 3.56%

Model:  $x=2\alpha-1$

$E(x) = 178.77$

$\log_{10} \tilde{A}(x) = 12.681T_0(x) - 2.408T_1(x) - .367T_2(x) - .945T_3(x) - .248T_4(x) - .27T_5(x)$

$c = 0.813$



**Fiberboard, "constant reaction rate" (CRR)**

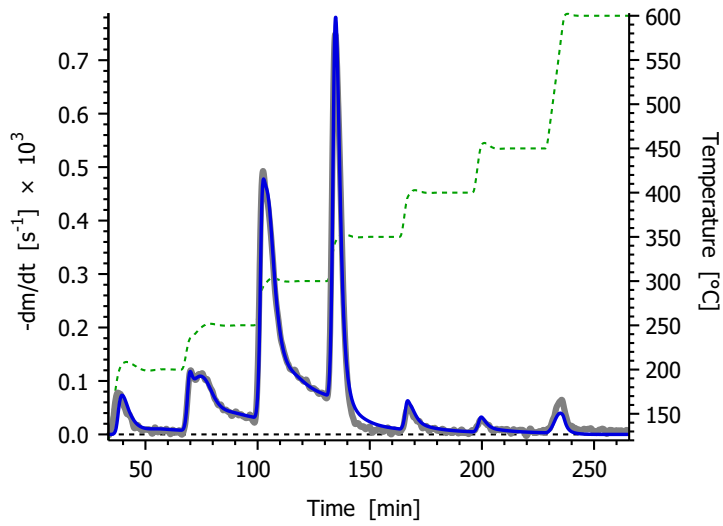
Relative deviation: 4.77%, Deviation: 0.054 µg/s  
rms rel. dev. of 5 experiments: 3.08%

Model:  $x=2\alpha-1$

$E(x) = 156.06T_0(x) - 22.61T_1(x) - 31.33T_2(x) - 3.07T_3(x)$

$\log_{10} \tilde{A}(x) = 10.737T_0(x) - 3.965T_1(x) - 3.046T_2(x) - .978T_3(x) - .228T_4(x) - .219T_5(x)$

$c = 0.827$



**Fiberboard, stepwise T(t)**

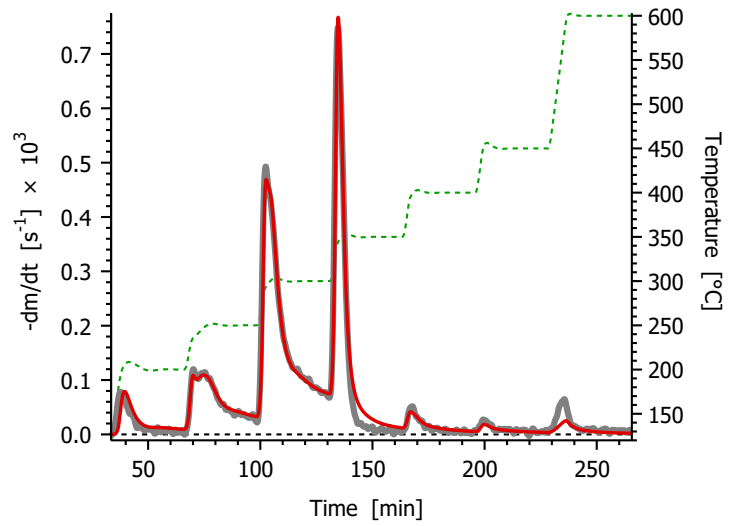
Relative deviation: 2.02%, Deviation: 0.073 µg/s  
rms rel. dev. of 5 experiments: 3.56%

Model:  $x=2\alpha-1$

$E(x) = 178.77$

$\log_{10} \tilde{A}(x) = 12.681T_0(x) - 2.408T_1(x) - .367T_2(x) - .945T_3(x) - .248T_4(x) - .27T_5(x)$

$c = 0.813$



**Fiberboard, stepwise T(t)**

Relative deviation: 2.09%, Deviation: 0.076 µg/s  
rms rel. dev. of 5 experiments: 3.08%

Model:  $x=2\alpha-1$

$E(x) = 156.06T_0(x) - 22.61T_1(x) - 31.33T_2(x) - 3.07T_3(x)$

$\log_{10} \tilde{A}(x) = 10.737T_0(x) - 3.965T_1(x) - 3.046T_2(x) - .978T_3(x) - .228T_4(x) - .219T_5(x)$

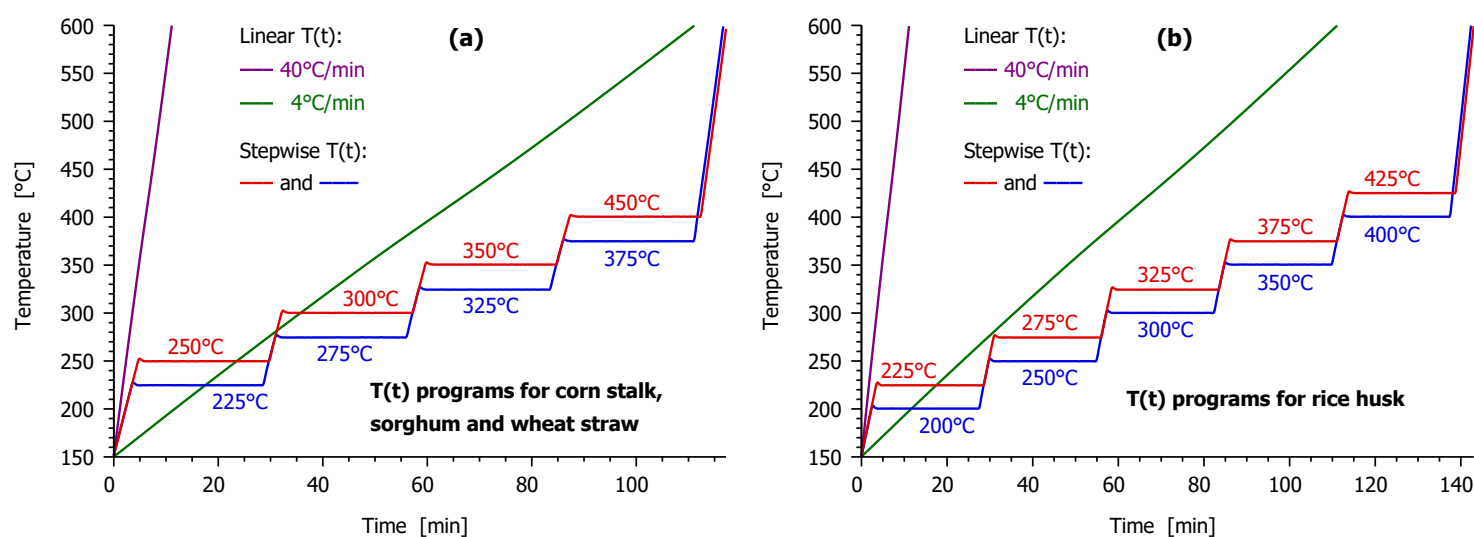
$c = 0.827$

### S3. Four Agricultural Residues

Source of the data:

[S3] Várhegyi, G.; Bobály, B.; Jakab, E.; Chen, H.: Thermogravimetric study of biomass pyrolysis kinetics. A distributed activation energy model with prediction tests. *Energy Fuels* **2011**, *25*, 24-32. doi: [10.1021/ef101079r](https://doi.org/10.1021/ef101079r)  
[Supporting Info](#) [Repository](#)

Four TGA experiments were available for each sample. The figures below show the corresponding temperature programs. It is a redrawn/rearranged version of Figure 2 of the cited paper. The Supporting Information of the cited paper contains all the experimental curves with different evaluations. (It is available free-of-charge at the internet links given in the above reference.)



**Figure S3.1:** Temperature programs used for the TGA experiments of this section.

### S3.1. Corn stalk

#### Model with constant E:

Input file: "C\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 187.97731$$

$$\log_{10}\tilde{A}(x)= 13.775727 -0.36308x +0.381556x^2 -3.726592x^3 -4.469088x^4 -3.221648x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 12.290597T_0(x) -5.171554T_1(x) -2.043766T_2(x) -1.938413T_3(x) -0.558636T_4(x) -0.201353T_5(x)$$

#### Model with third order E(α):

Input file: "C\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

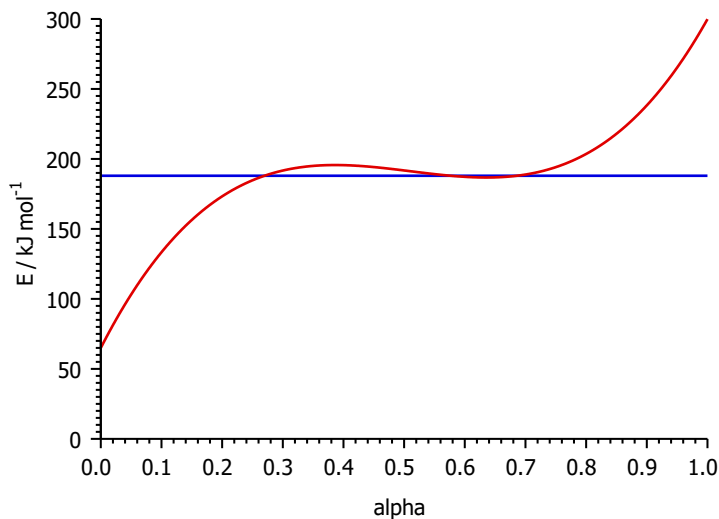
$$E(x)= 191.764335 -26.613237x -9.33327x^2 +144.055868x^3$$

$$\log_{10}\tilde{A}(x)= 14.190545 -2.7887559x +1.070722x^2 +10.1355028x^3 -5.115208x^4 -1.183872x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 187.0977T_0(x) +81.428664T_1(x) -4.666635T_2(x) +36.013967T_3(x)$$

$$\log_{10}\tilde{A}(x)= 12.807703T_0(x) +4.0729512T_1(x) -2.022243T_2(x) +2.1639157T_3(x) -0.639401T_4(x) -0.073992T_5(x)$$



#### E(α) = polynomial of (2α-1)

Parameter file: C\_0,5\_oneC.PAR

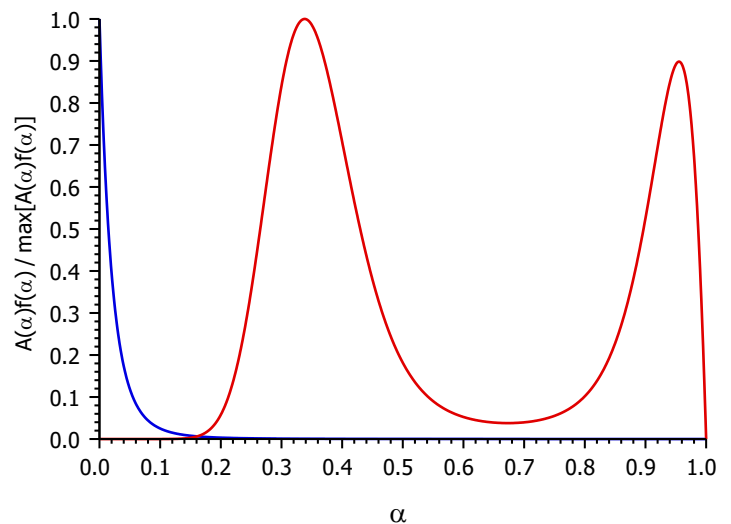
$$\log_{10}\tilde{A}(0)= 17.00 \quad E(0)= 188.0 \quad \log_{10}\tilde{A}(1)= 2.38 \quad E(1)= 188.0$$

$$\text{mean } \log_{10}\tilde{A}= 13.01 \quad \text{mean } E= 188.0$$

Parameter file: C\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 3.98 \quad E(0)= 65.0 \quad \log_{10}\tilde{A}(1)= 16.31 \quad E(1)= 299.9$$

$$\text{mean } \log_{10}\tilde{A}= 13.52 \quad \text{mean } E= 188.7$$



#### Plot of A(α)f(α) / max[A(α)f(α)]

Parameter file: C\_0,5\_oneC.PAR

$$A(0)f(0)= 9.989E+16 \quad E(0)= 188.0 \quad A(1)f(1)= 0.00 \quad E(1)= 188.0$$

$$\text{mean } A(\alpha)f(\alpha)= 2.389E+15 \quad \text{mean } E= 188.0$$

$$\text{max } A(\alpha)f(\alpha)= 9.989E+16 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 188.0$$

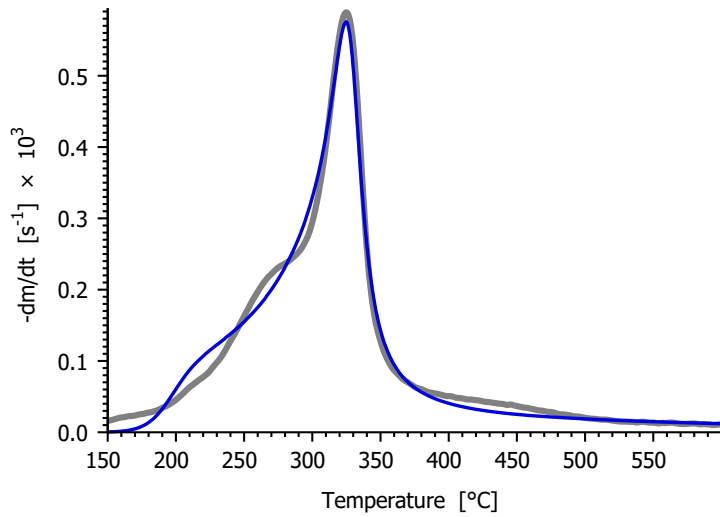
Parameter file: C\_3,5\_oneC.PAR

$$A(0)f(0)= 9.620E+03 \quad E(0)= 65.0 \quad A(1)f(1)= 0.00 \quad E(1)= 299.9$$

$$\text{mean } A(\alpha)f(\alpha)= 1.223E+14 \quad \text{mean } E= 188.7$$

$$\text{max } A(\alpha)f(\alpha)= 4.271E+14 \quad \text{at } \alpha= 0.338 \quad \text{and } E= 194.5$$

Figures illustrating the fit quality (cf. Figure S1 in the Supporting Information of reference [S3])



**Corn stalk, 4mg, 4°C/min**

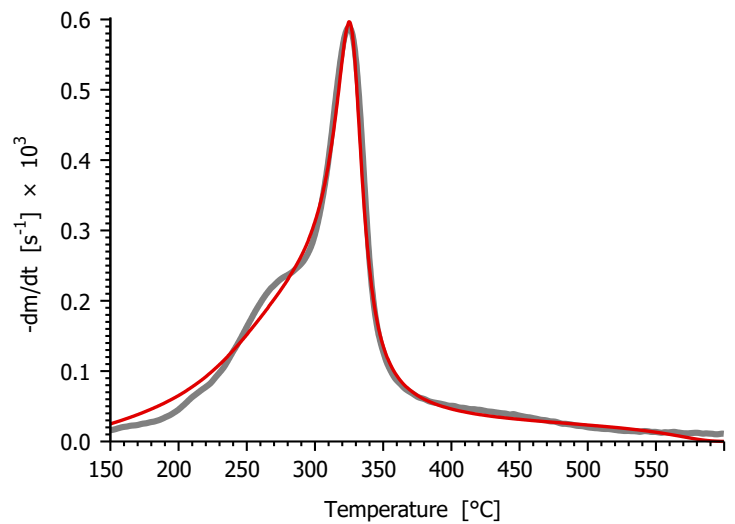
Relative deviation: 2.40%, Deviation: 0.054 µg/s  
rms rel. dev. of 4 experiments: 2.99%

Model:  $x=2\alpha-1$

$E(x) = 187.98$

$\log_{10} \tilde{A}(x) = 12.291T_0(x) - 5.172T_1(x) - 2.044T_2(x) - 1.938T_3(x) - 0.559T_4(x) - 0.201T_5(x)$

$c = 0.721$



**Corn stalk, 4mg, 4°C/min**

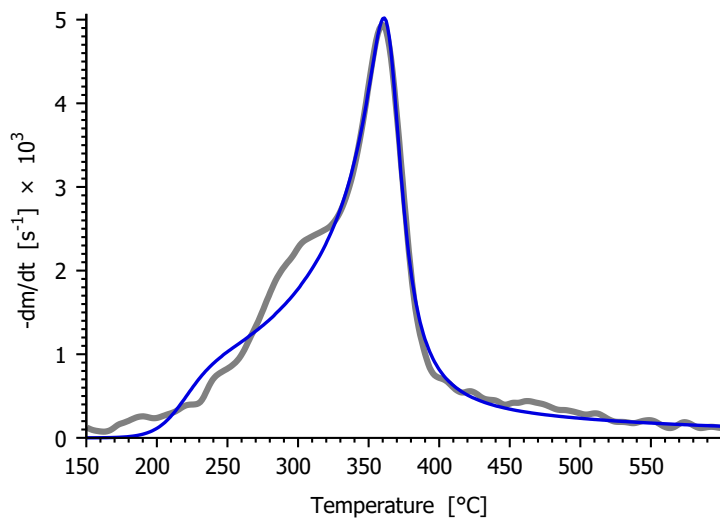
Relative deviation: 1.94%, Deviation: 0.044 µg/s  
rms rel. dev. of 4 experiments: 1.83%

Model:  $x=2\alpha-1$

$E(x) = 187.1T_0(x) + 81.43T_1(x) - 4.67T_2(x) + 36.01T_3(x)$

$\log_{10} \tilde{A}(x) = 12.808T_0(x) + 4.073T_1(x) - 2.022T_2(x) + 2.164T_3(x) - 0.639T_4(x) - 0.074T_5(x)$

$c = 0.690$



**Corn stalk, 0.5mg, 40°C/min**

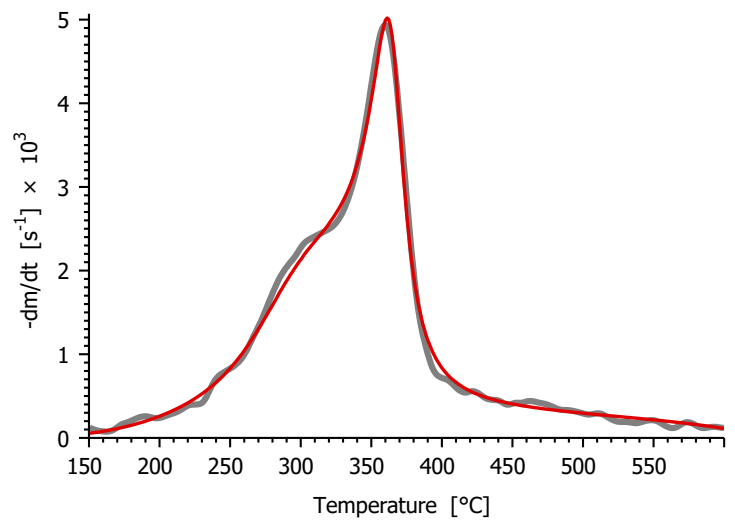
Relative deviation: 3.26%, Deviation: 0.082 µg/s  
rms rel. dev. of 4 experiments: 2.99%

Model:  $x=2\alpha-1$

$E(x) = 187.98$

$\log_{10} \tilde{A}(x) = 12.291T_0(x) - 5.172T_1(x) - 2.044T_2(x) - 1.938T_3(x) - 0.559T_4(x) - 0.201T_5(x)$

$c = 0.721$



**Corn stalk, 0.5mg, 40°C/min**

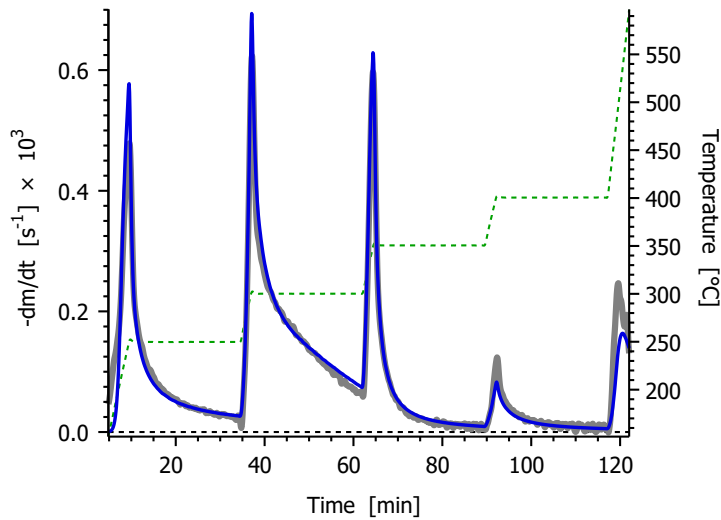
Relative deviation: 1.53%, Deviation: 0.039 µg/s  
rms rel. dev. of 4 experiments: 1.83%

Model:  $x=2\alpha-1$

$E(x) = 187.1T_0(x) + 81.43T_1(x) - 4.67T_2(x) + 36.01T_3(x)$

$\log_{10} \tilde{A}(x) = 12.808T_0(x) + 4.073T_1(x) - 2.022T_2(x) + 2.164T_3(x) - 0.639T_4(x) - 0.074T_5(x)$

$c = 0.690$



**Corn stalk, 2mg, steps: 250 - 400°C**

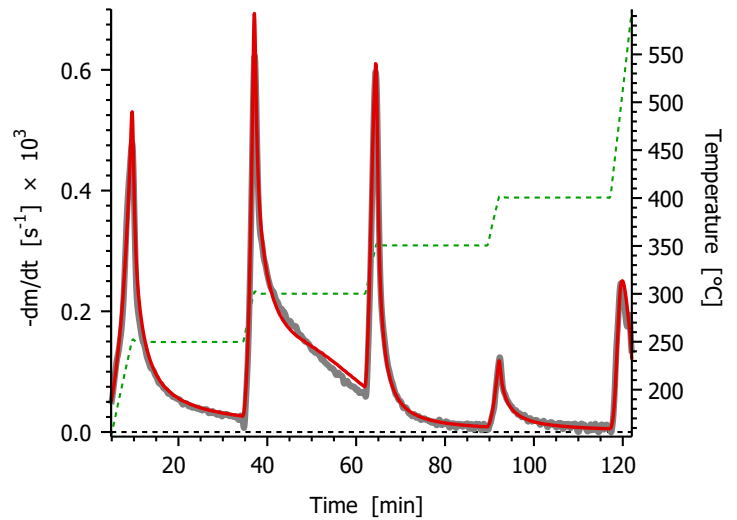
Relative deviation: 3.69%, Deviation: 0.045 µg/s  
rms rel. dev. of 4 experiments: 2.99%

Model:  $x=2\alpha-1$

$E(x) = 187.98$

$\log_{10} \tilde{A}(x) = 12.291T_0(x) - 5.172T_1(x) - 2.044T_2(x) - 1.938T_3(x) - 0.559T_4(x) - 0.201T_5(x)$

$c = 0.721$



**Corn stalk, 2mg, steps: 250 - 400°C**

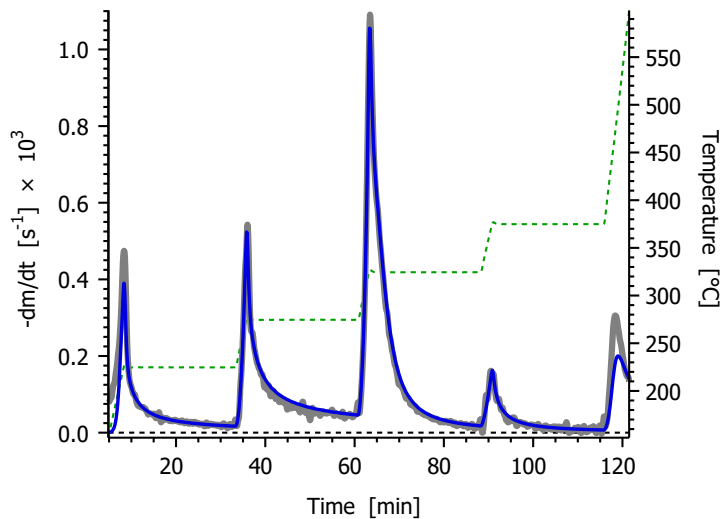
Relative deviation: 1.98%, Deviation: 0.024 µg/s  
rms rel. dev. of 4 experiments: 1.83%

Model:  $x=2\alpha-1$

$E(x) = 187.1T_0(x) + 81.43T_1(x) - 4.67T_2(x) + 36.01T_3(x)$

$\log_{10} \tilde{A}(x) = 12.808T_0(x) + 4.073T_1(x) - 2.022T_2(x) + 2.164T_3(x) - 0.639T_4(x) - 0.074T_5(x)$

$c = 0.690$



**Corn stalk, 2mg, steps: 225 - 375°C**

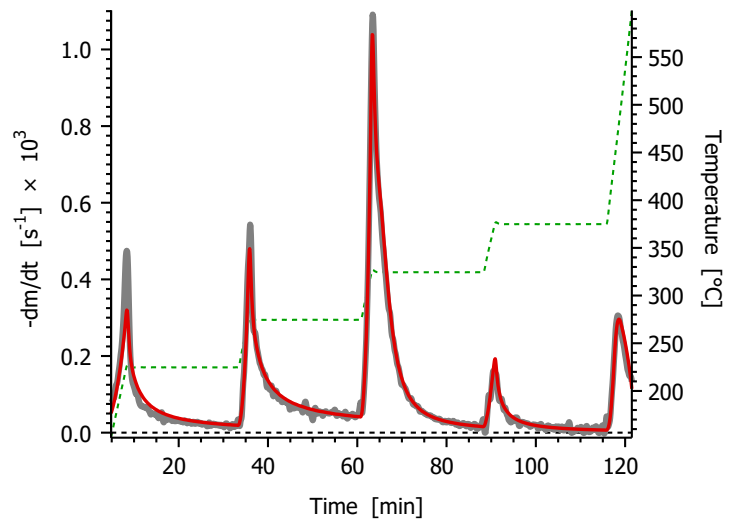
Relative deviation: 2.40%, Deviation: 0.051 µg/s  
rms rel. dev. of 4 experiments: 2.99%

Model:  $x=2\alpha-1$

$E(x) = 187.98$

$\log_{10} \tilde{A}(x) = 12.291T_0(x) - 5.172T_1(x) - 2.044T_2(x) - 1.938T_3(x) - 0.559T_4(x) - 0.201T_5(x)$

$c = 0.721$



**Corn stalk, 2mg, steps: 225 - 375°C**

Relative deviation: 1.85%, Deviation: 0.040 µg/s  
rms rel. dev. of 4 experiments: 1.83%

Model:  $x=2\alpha-1$

$E(x) = 187.1T_0(x) + 81.43T_1(x) - 4.67T_2(x) + 36.01T_3(x)$

$\log_{10} \tilde{A}(x) = 12.808T_0(x) + 4.073T_1(x) - 2.022T_2(x) + 2.164T_3(x) - 0.639T_4(x) - 0.074T_5(x)$

$c = 0.690$



### S3.2. Rice husk

#### Model with constant E:

Input file: "R\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 181.0715$$

$$\log_{10}\tilde{A}(x)= 13.079498 - .763766x + 1.471146x^2 - .472292x^3 - 6.014304x^4 - 7.5068x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 11.559707T_0(x) - 5.809735T_1(x) - 2.271579T_2(x) - 2.463948T_3(x) - .751788T_4(x) - .469175T_5(x)$$

#### Model with third order E(α):

Input file: "R\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

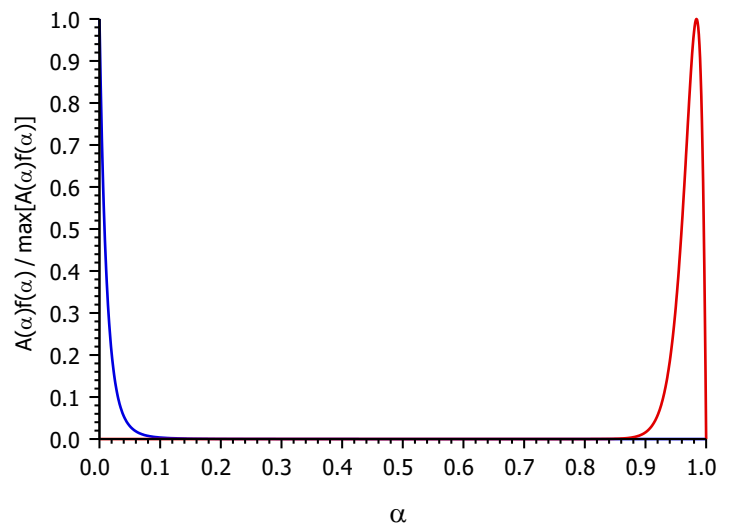
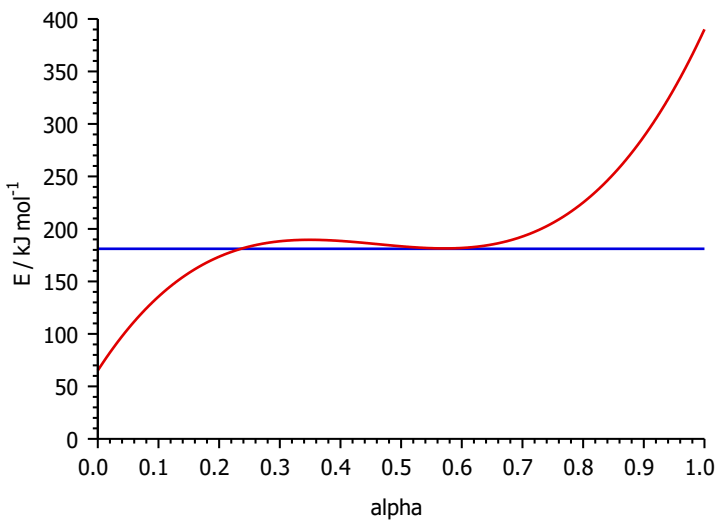
$$E(x)= 183.434091 - 24.200095x + 44.197618x^2 + 186.6883x^3$$

$$\log_{10}\tilde{A}(x)= 13.361836 - 2.8951496x + 5.813892x^2 + 15.4994652x^3 - 5.885848x^4 - 3.849584x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 205.5329T_0(x) + 115.81613T_1(x) + 22.098809T_2(x) + 46.672075T_3(x)$$

$$\log_{10}\tilde{A}(x)= 14.061589T_0(x) + 6.3234593T_1(x) - .035978T_2(x) + 2.6718713T_3(x) - .735731T_4(x) - .240599T_5(x)$$



#### E(α) = polynomial of (2α-1)

Parameter file: R\_0,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 17.28 \quad E(0)= 181.1 \quad \log_{10}\tilde{A}(1)= -0.21 \quad E(1)= 181.1$$

$$\text{mean } \log_{10}\tilde{A}= 12.37 \quad \text{mean } E= 181.1$$

Parameter file: R\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 4.54 \quad E(0)= 65.1 \quad \log_{10}\tilde{A}(1)= 22.04 \quad E(1)= 390.1$$

$$\text{mean } \log_{10}\tilde{A}= 14.12 \quad \text{mean } E= 198.2$$

#### Plot of A(α)f(α) / max[A(α)f(α)]

Parameter file: R\_0,5\_oneC.PAR

$$A(0)f(0)= 1.902E+17 \quad E(0)= 181.1 \quad A(1)f(1)= 0.00 \quad E(1)= 181.1$$

$$\text{mean } A(\alpha)f(\alpha)= 2.516E+15 \quad \text{mean } E= 181.1$$

$$\text{max } A(\alpha)f(\alpha)= 1.902E+17 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 181.1$$

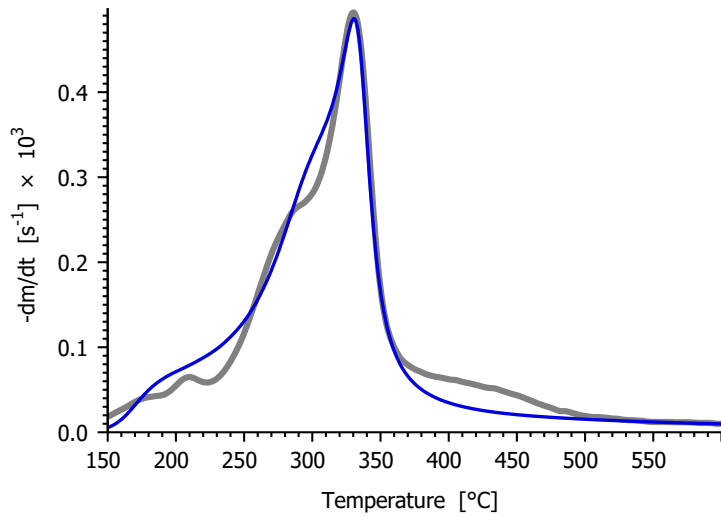
Parameter file: R\_3,5\_oneC.PAR

$$A(0)f(0)= 3.429E+04 \quad E(0)= 65.1 \quad A(1)f(1)= 0.00 \quad E(1)= 390.1$$

$$\text{mean } A(\alpha)f(\alpha)= 2.702E+18 \quad \text{mean } E= 198.2$$

$$\text{max } A(\alpha)f(\alpha)= 6.763E+19 \quad \text{at } \alpha= 0.984 \quad \text{and } E= 370.9$$

Figures illustrating the fit quality (cf. Figure S1 in the Supporting Information of reference [S3])



**Rice husk, 4mg, 4°C/min**

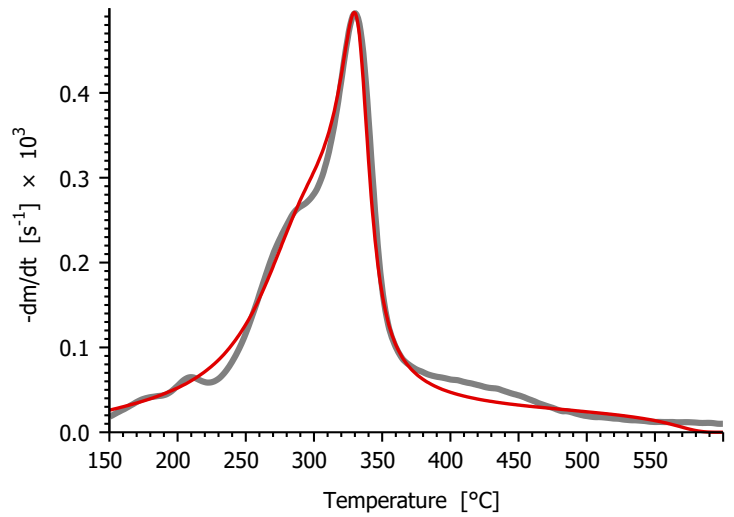
Relative deviation: 3.79%, Deviation: 0.074 µg/s  
rms rel. dev. of 4 experiments: 3.54%

Model:  $x=2\alpha-1$

$E(x) = 181.07$

$\log_{10} \tilde{A}(x) = 11.56T_0(x) - 5.81T_1(x) - 2.272T_2(x) - 2.464T_3(x) - 0.752T_4(x) - 0.469T_5(x)$

$c = 0.696$



**Rice husk, 4mg, 4°C/min**

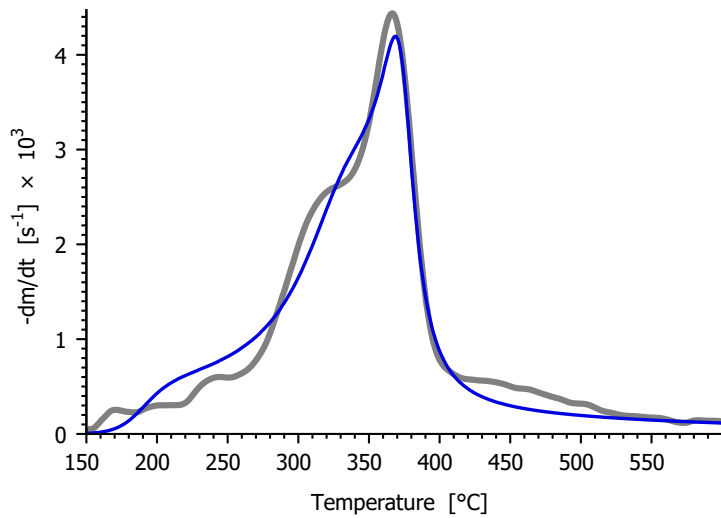
Relative deviation: 2.56%, Deviation: 0.050 µg/s  
rms rel. dev. of 4 experiments: 2.17%

Model:  $x=2\alpha-1$

$E(x) = 205.53T_0(x) + 115.82T_1(x) + 22.1T_2(x) + 46.67T_3(x)$

$\log_{10} \tilde{A}(x) = 14.062T_0(x) + 6.323T_1(x) - 0.036T_2(x) + 2.672T_3(x) - 0.736T_4(x) - 0.241T_5(x)$

$c = 0.662$



**Rice husk, 1mg, 40°C/min**

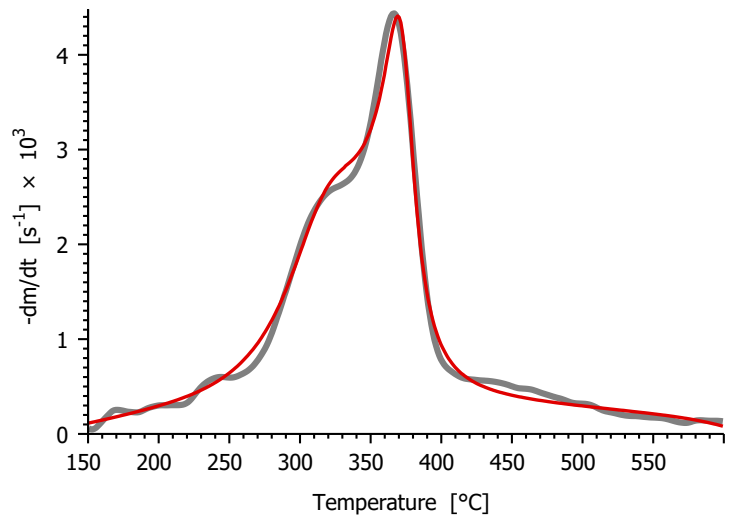
Relative deviation: 3.82%, Deviation: 0.16 µg/s  
rms rel. dev. of 4 experiments: 3.54%

Model:  $x=2\alpha-1$

$E(x) = 181.07$

$\log_{10} \tilde{A}(x) = 11.56T_0(x) - 5.81T_1(x) - 2.272T_2(x) - 2.464T_3(x) - 0.752T_4(x) - 0.469T_5(x)$

$c = 0.696$



**Rice husk, 1mg, 40°C/min**

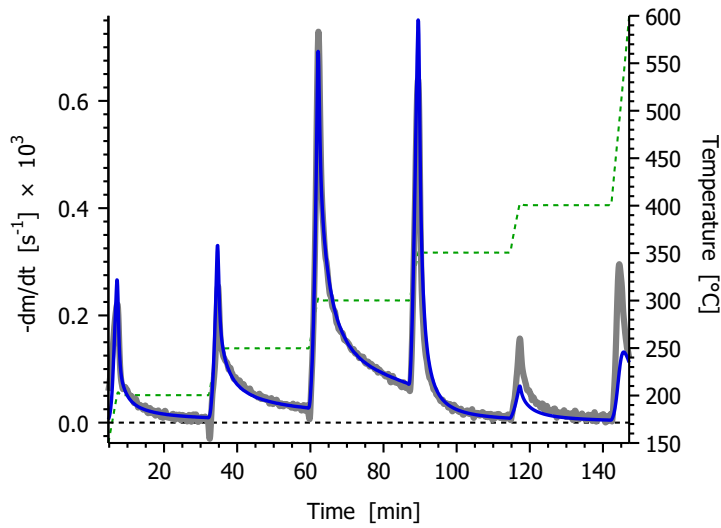
Relative deviation: 2.08%, Deviation: 0.085 µg/s  
rms rel. dev. of 4 experiments: 2.17%

Model:  $x=2\alpha-1$

$E(x) = 205.53T_0(x) + 115.82T_1(x) + 22.1T_2(x) + 46.67T_3(x)$

$\log_{10} \tilde{A}(x) = 14.062T_0(x) + 6.323T_1(x) - 0.036T_2(x) + 2.672T_3(x) - 0.736T_4(x) - 0.241T_5(x)$

$c = 0.662$



**Rice husk, 2mg, steps: 200 - 400°C**

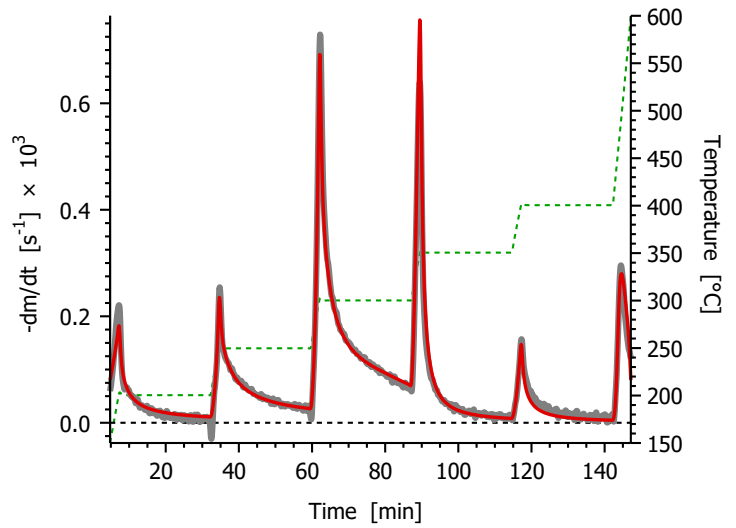
Relative deviation: 3.79%, Deviation: 0.055 µg/s  
rms rel. dev. of 4 experiments: 3.54%

Model:  $x=2\alpha-1$

$E(x) = 181.07$

$\log_{10} \tilde{A}(x) = 11.56T_0(x) - 5.81T_1(x) - 2.272T_2(x) - 2.464T_3(x) - 0.752T_4(x) - 0.469T_5(x)$

$c = 0.696$



**Rice husk, 2mg, steps: 200 - 400°C**

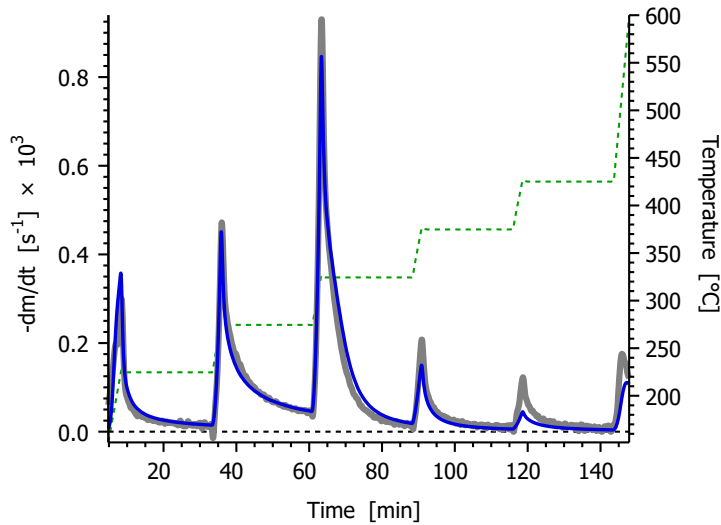
Relative deviation: 1.97%, Deviation: 0.028 µg/s  
rms rel. dev. of 4 experiments: 2.17%

Model:  $x=2\alpha-1$

$E(x) = 205.53T_0(x) + 115.82T_1(x) + 22.1T_2(x) + 46.67T_3(x)$

$\log_{10} \tilde{A}(x) = 14.062T_0(x) + 6.323T_1(x) - 0.036T_2(x) + 2.672T_3(x) - 0.736T_4(x) - 0.241T_5(x)$

$c = 0.662$



**Rice husk, 2mg, steps: 225 - 425°C**

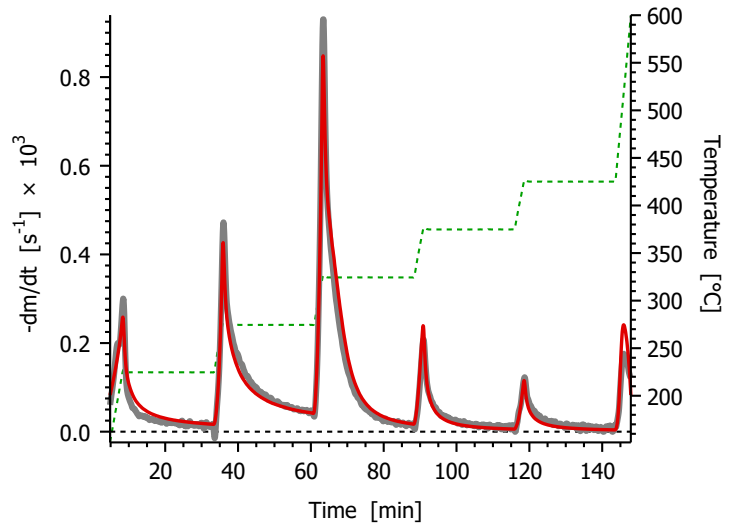
Relative deviation: 2.63%, Deviation: 0.048 µg/s  
rms rel. dev. of 4 experiments: 3.54%

Model:  $x=2\alpha-1$

$E(x) = 181.07$

$\log_{10} \tilde{A}(x) = 11.56T_0(x) - 5.81T_1(x) - 2.272T_2(x) - 2.464T_3(x) - 0.752T_4(x) - 0.469T_5(x)$

$c = 0.696$



**Rice husk, 2mg, steps: 225 - 425°C**

Relative deviation: 2.02%, Deviation: 0.037 µg/s  
rms rel. dev. of 4 experiments: 2.17%

Model:  $x=2\alpha-1$

$E(x) = 205.53T_0(x) + 115.82T_1(x) + 22.1T_2(x) + 46.67T_3(x)$

$\log_{10} \tilde{A}(x) = 14.062T_0(x) + 6.323T_1(x) - 0.036T_2(x) + 2.672T_3(x) - 0.736T_4(x) - 0.241T_5(x)$

$c = 0.662$

### S3.3. Sorghum

#### Model with constant E:

Input file: "S\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 188.21119$$

$$\log_{10}\tilde{A}(x)= 13.536254 - .570222x - .819662x^2 - 3.352008x^3 - 3.716208x^4 - 2.973456x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 11.732845T_0(x) - 4.942638T_1(x) - 2.267935T_2(x) - 1.767207T_3(x) - .464526T_4(x) - .185841T_5(x)$$

#### Model with third order E( $\alpha$ ):

Input file: "S\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

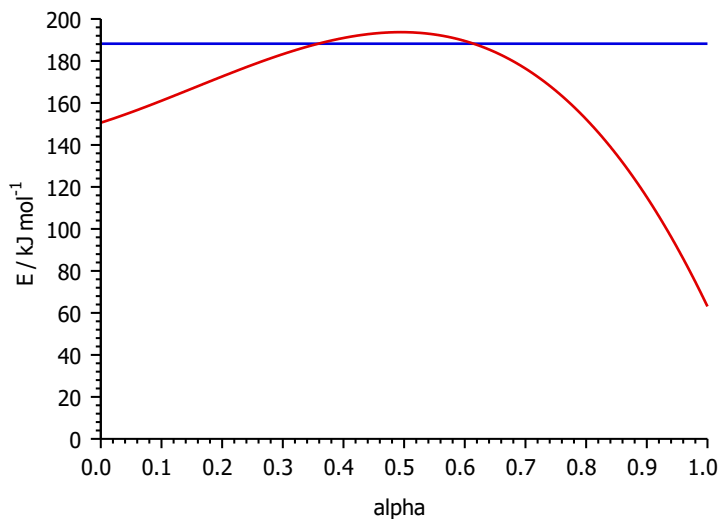
$$E(x)= 193.70388 - 1.86176x - 86.8737x^2 - 41.89796x^3$$

$$\log_{10}\tilde{A}(x)= 13.9385846 - .966972x - 9.080428x^2 - 7.695572x^3 - 3.409552x^4 - 1.814272x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 150.26703T_0(x) - 33.28523T_1(x) - 43.43685T_2(x) - 10.47449T_3(x)$$

$$\log_{10}\tilde{A}(x)= 8.1197886T_0(x) - 7.872571T_1(x) - 6.24499T_2(x) - 2.490853T_3(x) - .426194T_4(x) - .113392T_5(x)$$



#### E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)

Parameter file: S\_0,5\_oneC.PAR

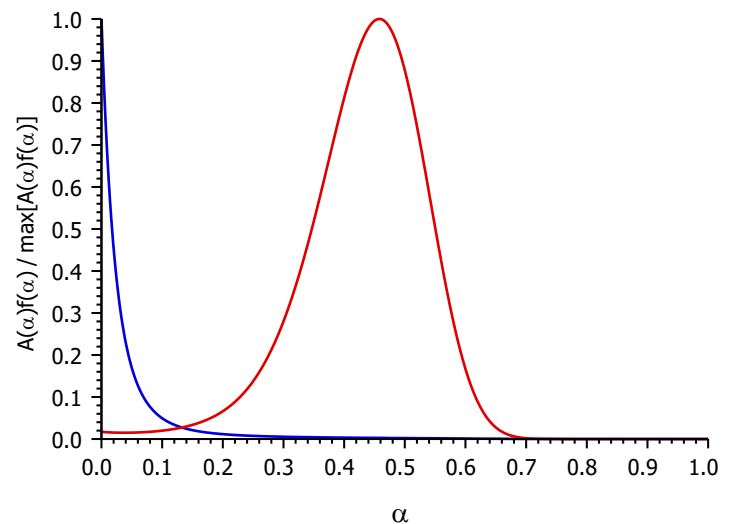
$$\log_{10}\tilde{A}(0)= 15.90 \quad E(0)= 188.2 \quad \log_{10}\tilde{A}(1)= 2.10 \quad E(1)= 188.2$$

$$\text{mean } \log_{10}\tilde{A}= 12.52 \quad \text{mean } E= 188.2$$

Parameter file: S\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 11.93 \quad E(0)= 150.6 \quad \log_{10}\tilde{A}(1)= -9.03 \quad E(1)= 63.1$$

$$\text{mean } \log_{10}\tilde{A}= 10.23 \quad \text{mean } E= 164.7$$



#### Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]

Parameter file: S\_0,5\_oneC.PAR

$$A(0)f(0)= 7.872E+15 \quad E(0)= 188.2 \quad A(1)f(1)= 0.00 \quad E(1)= 188.2$$

$$\text{mean } A(\alpha)f(\alpha)= 2.445E+14 \quad \text{mean } E= 188.2$$

$$\text{max } A(\alpha)f(\alpha)= 7.872E+15 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 188.2$$

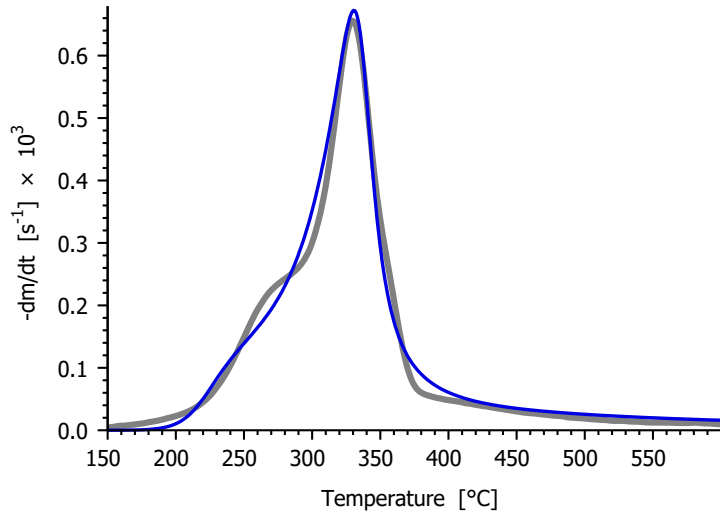
Parameter file: S\_3,5\_oneC.PAR

$$A(0)f(0)= 8.422E+11 \quad E(0)= 150.6 \quad A(1)f(1)= 0.00 \quad E(1)= 63.1$$

$$\text{mean } A(\alpha)f(\alpha)= 1.104E+13 \quad \text{mean } E= 164.7$$

$$\text{max } A(\alpha)f(\alpha)= 4.945E+13 \quad \text{at } \alpha= 0.458 \quad \text{and } E= 193.3$$

Figures illustrating the fit quality (cf. Figure S1 in the Supporting Information of reference [S3])



**Sorghum, 4mg, 4°C/min**

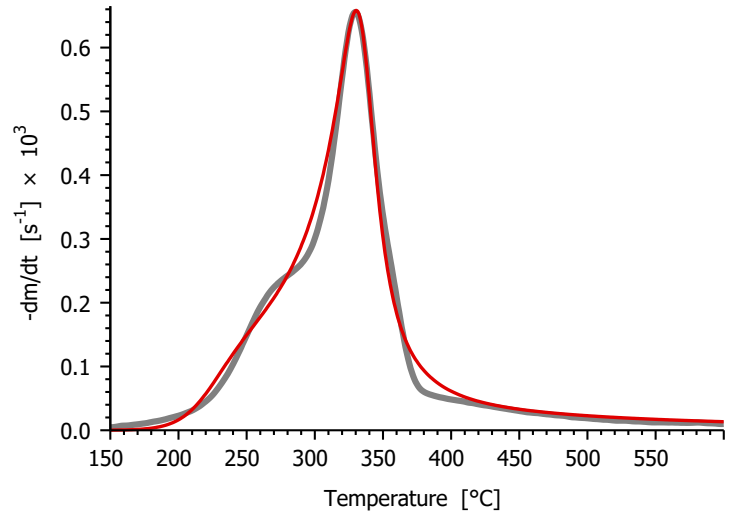
Relative deviation: 2.86%, Deviation: 0.074  $\mu\text{g/s}$   
rms rel. dev. of 4 experiments: 2.49%

Model:  $x=2\alpha-1$

$E(x) = 188.21$

$\log_{10} \tilde{A}(x) = 11.733T_0(x) - 4.943T_1(x) - 2.268T_2(x) - 1.767T_3(x) - 0.465T_4(x) - 0.186T_5(x)$

$c = 0.851$



**Sorghum, 4mg, 4°C/min**

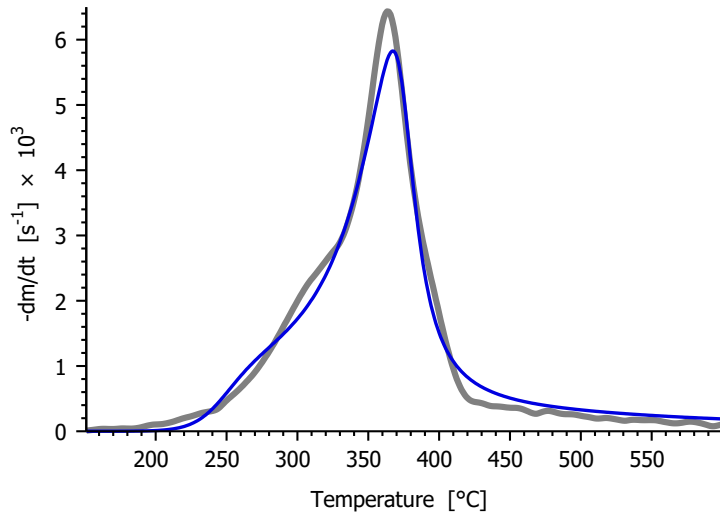
Relative deviation: 2.50%, Deviation: 0.065  $\mu\text{g/s}$   
rms rel. dev. of 4 experiments: 2.23%

Model:  $x=2\alpha-1$

$E(x) = 150.27T_0(x) - 33.29T_1(x) - 43.44T_2(x) - 10.47T_3(x)$

$\log_{10} \tilde{A}(x) = 8.12T_0(x) - 7.873T_1(x) - 6.245T_2(x) - 2.491T_3(x) - 0.426T_4(x) - 0.113T_5(x)$

$c = 0.902$



**Sorghum, 1mg, 40°C/min**

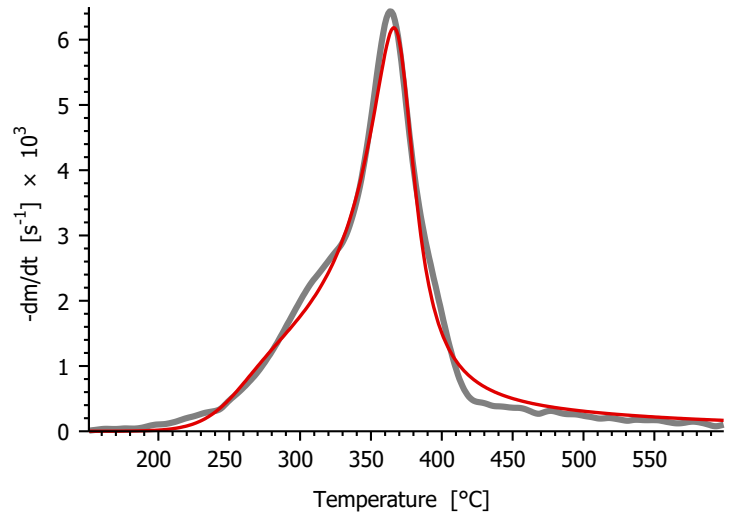
Relative deviation: 3.16%, Deviation: 0.19  $\mu\text{g/s}$   
rms rel. dev. of 4 experiments: 2.49%

Model:  $x=2\alpha-1$

$E(x) = 188.21$

$\log_{10} \tilde{A}(x) = 11.733T_0(x) - 4.943T_1(x) - 2.268T_2(x) - 1.767T_3(x) - 0.465T_4(x) - 0.186T_5(x)$

$c = 0.851$



**Sorghum, 1mg, 40°C/min**

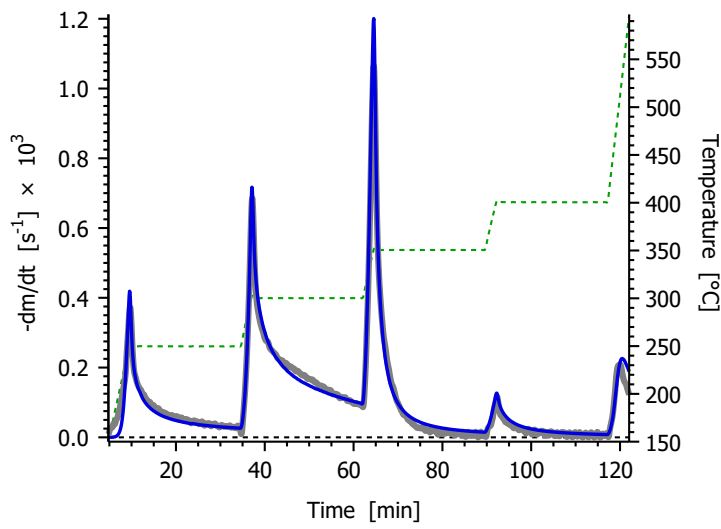
Relative deviation: 2.46%, Deviation: 0.14  $\mu\text{g/s}$   
rms rel. dev. of 4 experiments: 2.23%

Model:  $x=2\alpha-1$

$E(x) = 150.27T_0(x) - 33.29T_1(x) - 43.44T_2(x) - 10.47T_3(x)$

$\log_{10} \tilde{A}(x) = 8.12T_0(x) - 7.873T_1(x) - 6.245T_2(x) - 2.491T_3(x) - 0.426T_4(x) - 0.113T_5(x)$

$c = 0.902$



**Sorghum, 2mg, steps: 250 - 400°C**

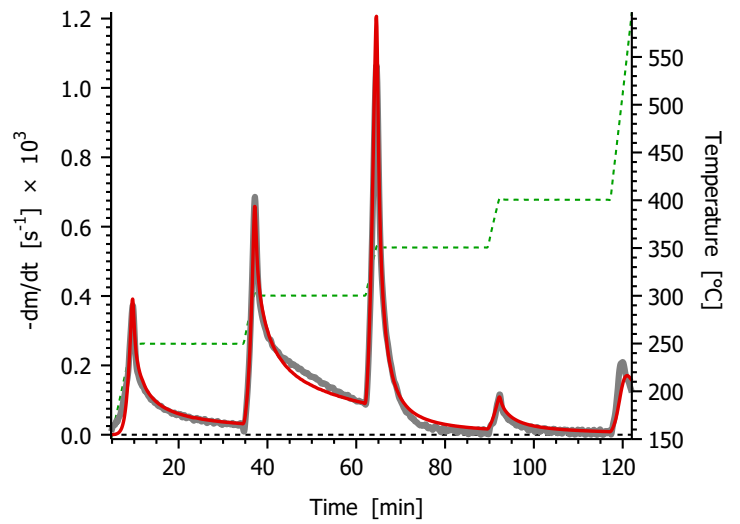
Relative deviation: 1.89%, Deviation: 0.040 µg/s  
rms rel. dev. of 4 experiments: 2.49%

Model:  $x=2\alpha-1$

$E(x) = 188.21$

$\log_{10} \tilde{A}(x) = 11.733T_0(x) - 4.943T_1(x) - 2.268T_2(x) - 1.767T_3(x) - 0.465T_4(x) - 0.186T_5(x)$

$c = 0.851$



**Sorghum, 2mg, steps: 250 - 400°C**

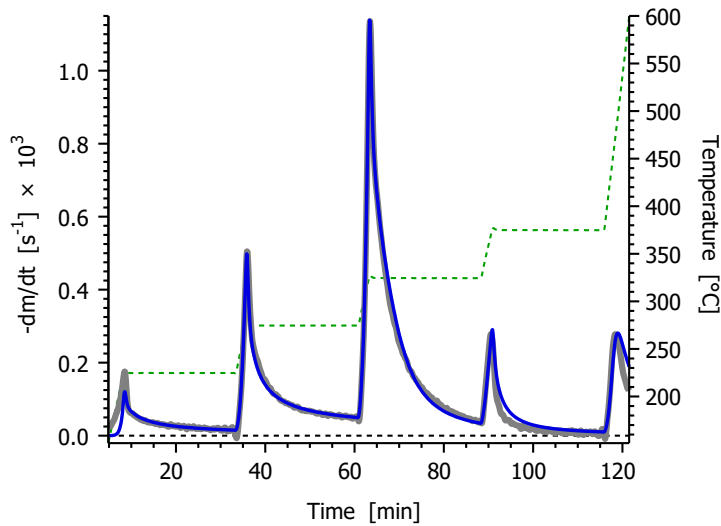
Relative deviation: 1.99%, Deviation: 0.043 µg/s  
rms rel. dev. of 4 experiments: 2.23%

Model:  $x=2\alpha-1$

$E(x) = 150.27T_0(x) - 33.29T_1(x) - 43.44T_2(x) - 10.47T_3(x)$

$\log_{10} \tilde{A}(x) = 8.12T_0(x) - 7.873T_1(x) - 6.245T_2(x) - 2.491T_3(x) - 0.426T_4(x) - 0.113T_5(x)$

$c = 0.902$



**Sorghum, 2mg, steps: 225-375°C**

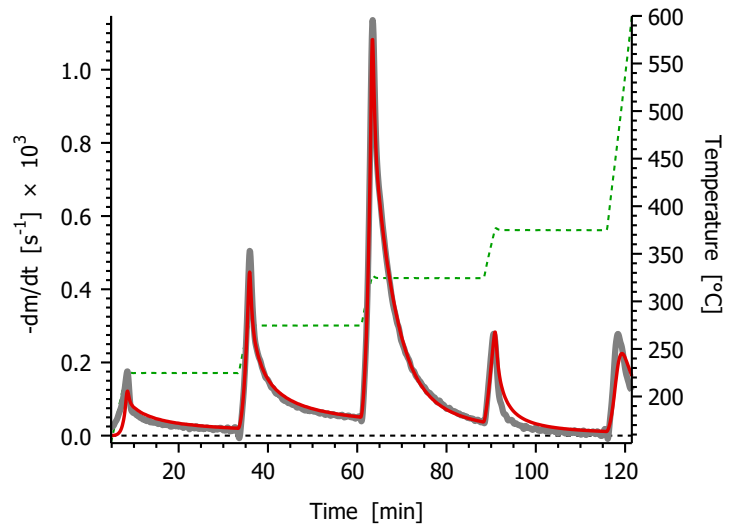
Relative deviation: 1.72%, Deviation: 0.039 µg/s  
rms rel. dev. of 4 experiments: 2.49%

Model:  $x=2\alpha-1$

$E(x) = 188.21$

$\log_{10} \tilde{A}(x) = 11.733T_0(x) - 4.943T_1(x) - 2.268T_2(x) - 1.767T_3(x) - 0.465T_4(x) - 0.186T_5(x)$

$c = 0.851$



**Sorghum, 2mg, steps: 225-375°C**

Relative deviation: 1.92%, Deviation: 0.043 µg/s  
rms rel. dev. of 4 experiments: 2.23%

Model:  $x=2\alpha-1$

$E(x) = 150.27T_0(x) - 33.29T_1(x) - 43.44T_2(x) - 10.47T_3(x)$

$\log_{10} \tilde{A}(x) = 8.12T_0(x) - 7.873T_1(x) - 6.245T_2(x) - 2.491T_3(x) - 0.426T_4(x) - 0.113T_5(x)$

$c = 0.902$

### S3.4. Wheat straw

#### Model with constant E:

Input file: "W\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 187.61656$$

$$\log_{10}\tilde{A}(x)= 13.748554 -.519708x +.056052x^2 -1.713088x^3 -4.838784x^4 -4.340992x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 11.962036T_0(x) -4.517644T_1(x) -2.391366T_2(x) -1.784832T_3(x) -.604848T_4(x) -.271312T_5(x)$$

#### Model with third order E( $\alpha$ ):

Input file: "W\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

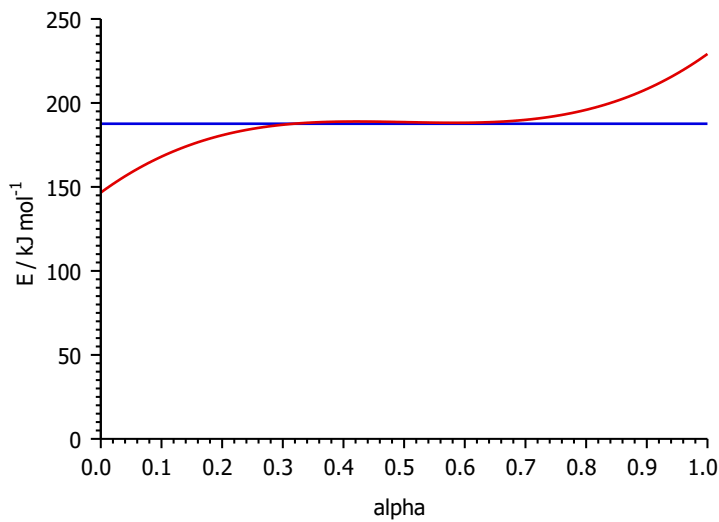
$$E(x)= 188.588694 -3.516947x -.681028x^2 +44.79034x^3$$

$$\log_{10}\tilde{A}(x)= 13.838112 -.797866x +.118542x^2 +1.97342x^3 -5.190192x^4 -3.850752x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 188.24818T_0(x) +30.075808T_1(x) -.340514T_2(x) +11.197585T_3(x)$$

$$\log_{10}\tilde{A}(x)= 11.951061T_0(x) -1.724521T_1(x) -2.535825T_2(x) -.710005T_3(x) -.648774T_4(x) -.240672T_5(x)$$



#### E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)

Parameter file: W\_0,5\_oneC.PAR

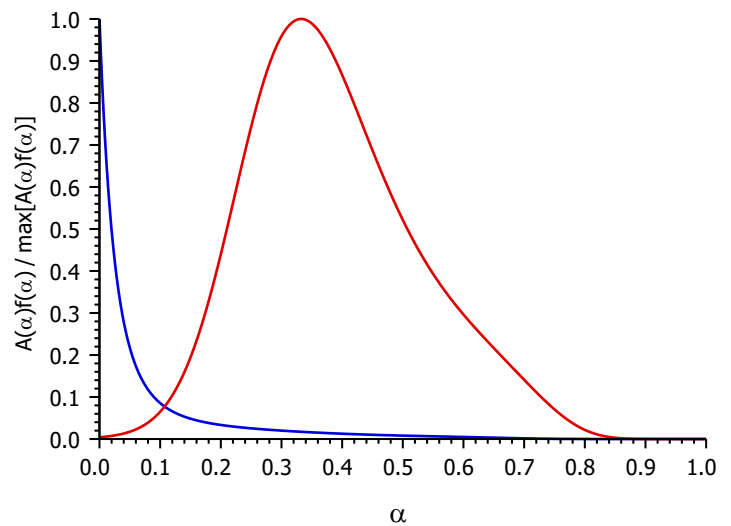
$$\log_{10}\tilde{A}(0)= 15.54 \quad E(0)= 187.6 \quad \log_{10}\tilde{A}(1)= 2.39 \quad E(1)= 187.6$$

$$\text{mean } \log_{10}\tilde{A}= 12.80 \quad \text{mean } E= 187.6$$

Parameter file: W\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 11.44 \quad E(0)= 146.6 \quad \log_{10}\tilde{A}(1)= 6.09 \quad E(1)= 229.2$$

$$\text{mean } \log_{10}\tilde{A}= 12.84 \quad \text{mean } E= 188.4$$



#### Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]

Parameter file: W\_0,5\_oneC.PAR

$$A(0)f(0)= 3.464E+15 \quad E(0)= 187.6 \quad A(1)f(1)= 0.00 \quad E(1)= 187.6$$

$$\text{mean } A(\alpha)f(\alpha)= 1.470E+14 \quad \text{mean } E= 187.6$$

$$\text{max } A(\alpha)f(\alpha)= 3.464E+15 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 187.6$$

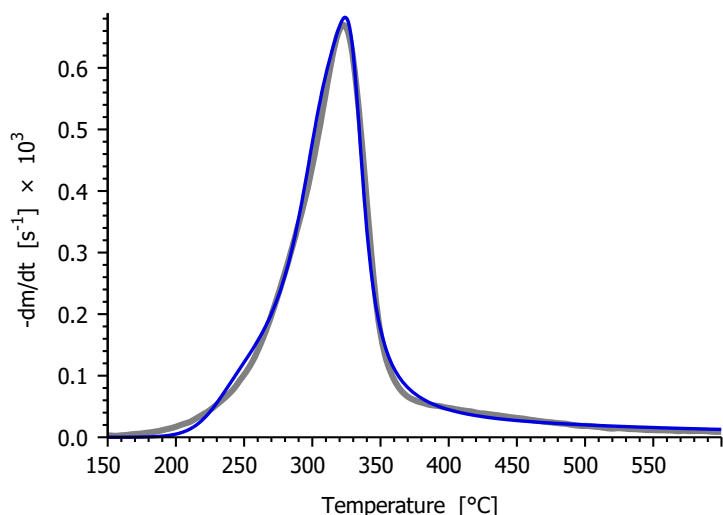
Parameter file: W\_3,5\_oneC.PAR

$$A(0)f(0)= 2.765E+11 \quad E(0)= 146.6 \quad A(1)f(1)= 0.00 \quad E(1)= 229.2$$

$$\text{mean } A(\alpha)f(\alpha)= 2.189E+13 \quad \text{mean } E= 188.4$$

$$\text{max } A(\alpha)f(\alpha)= 6.604E+13 \quad \text{at } \alpha= 0.333 \quad \text{and } E= 188.0$$

Figures illustrating the fit quality (cf. Figure S1 in the Supporting Information of reference [S3])



**Wheat straw, 4mg, 4°C/min**

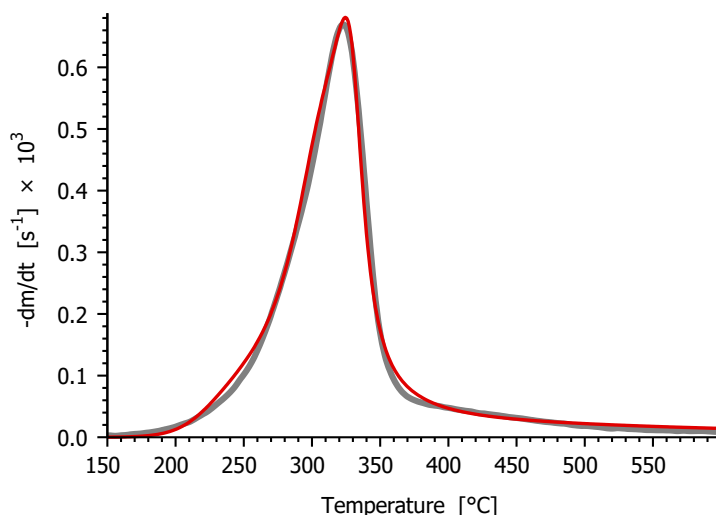
Relative deviation: 1.80%, Deviation: 0.047 µg/s  
rms rel. dev. of 4 experiments: 1.76%

Model:  $x=2\alpha-1$

$E(x) = 187.62$

$\log_{10} \tilde{A}(x) = 11.962T_0(x) - 4.518T_1(x) - 2.391T_2(x) - 1.785T_3(x) - 0.605T_4(x) - 0.271T_5(x)$

$c = 0.790$



**Wheat straw, 4mg, 4°C/min**

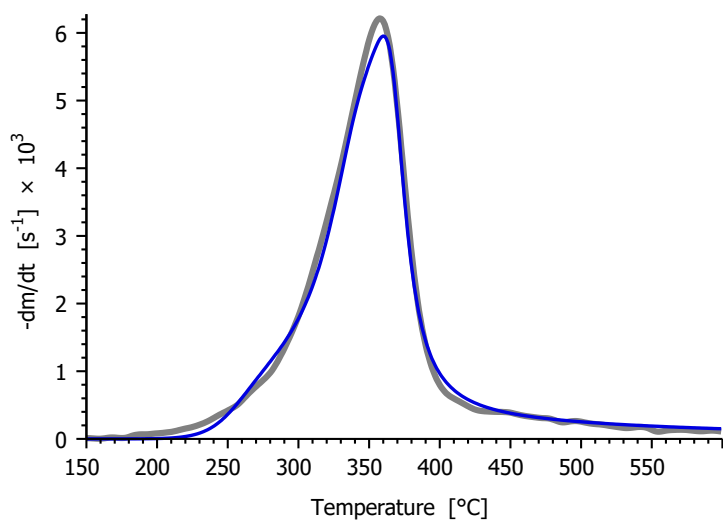
Relative deviation: 1.76%, Deviation: 0.046 µg/s  
rms rel. dev. of 4 experiments: 1.60%

Model:  $x=2\alpha-1$

$E(x) = 188.25T_0(x) + 30.08T_1(x) - 0.34T_2(x) + 11.2T_3(x)$

$\log_{10} \tilde{A}(x) = 11.951T_0(x) - 1.725T_1(x) - 2.536T_2(x) - 0.71T_3(x) - 0.649T_4(x) - 0.241T_5(x)$

$c = 0.791$



**Wheat straw, 1mg, 40°C/min**

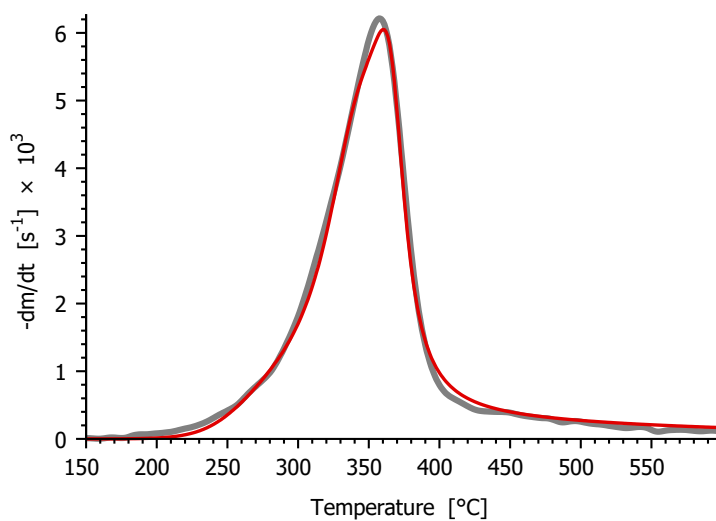
Relative deviation: 1.91%, Deviation: 0.11 µg/s  
rms rel. dev. of 4 experiments: 1.76%

Model:  $x=2\alpha-1$

$E(x) = 187.62$

$\log_{10} \tilde{A}(x) = 11.962T_0(x) - 4.518T_1(x) - 2.391T_2(x) - 1.785T_3(x) - 0.605T_4(x) - 0.271T_5(x)$

$c = 0.790$



**Wheat straw, 1mg, 40°C/min**

Relative deviation: 1.57%, Deviation: 0.089 µg/s  
rms rel. dev. of 4 experiments: 1.60%

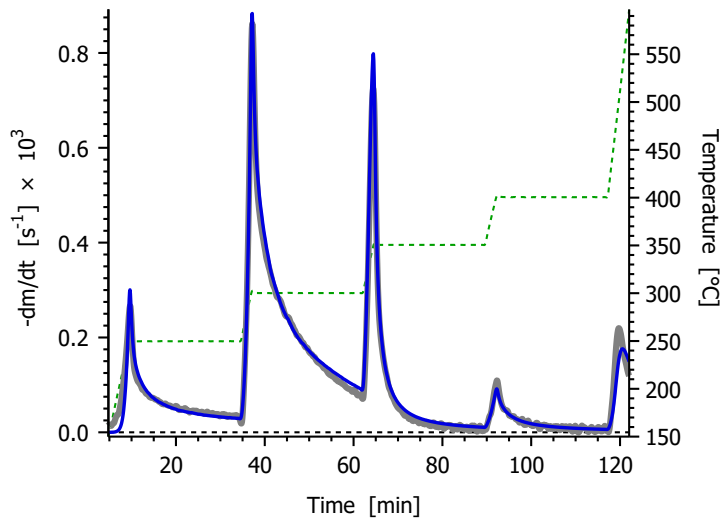
Model:  $x=2\alpha-1$

$E(x) = 188.25T_0(x) + 30.08T_1(x) - 0.34T_2(x) + 11.2T_3(x)$

$\log_{10} \tilde{A}(x) = 11.951T_0(x) - 1.725T_1(x) - 2.536T_2(x) - 0.71T_3(x) - 0.649T_4(x) - 0.241T_5(x)$

$c = 0.791$





**Wheat straw, 2mg, steps: 250 - 400°C**

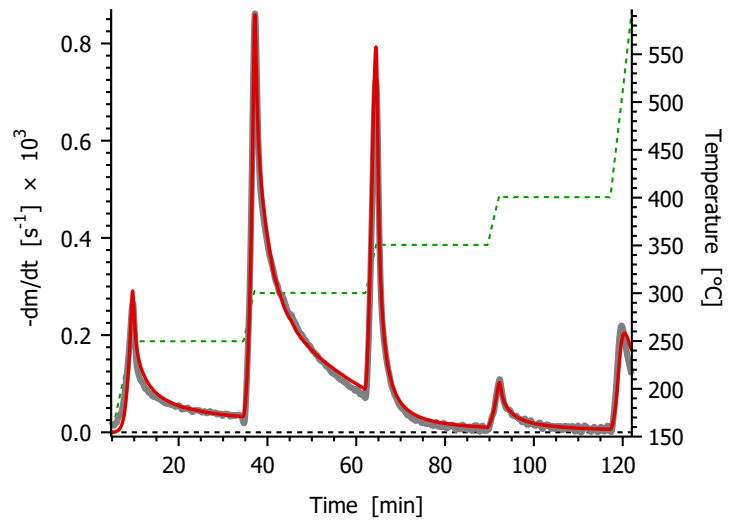
Relative deviation: 1.88%, Deviation: 0.032 µg/s  
rms rel. dev. of 4 experiments: 1.76%

Model:  $x=2\alpha-1$

$E(x) = 187.62$

$\log_{10} \tilde{A}(x) = 11.962T_0(x) - 4.518T_1(x) - 2.391T_2(x) - 1.785T_3(x) - 0.605T_4(x) - 0.271T_5(x)$

$c = 0.790$



**Wheat straw, 2mg, steps: 250 - 400°C**

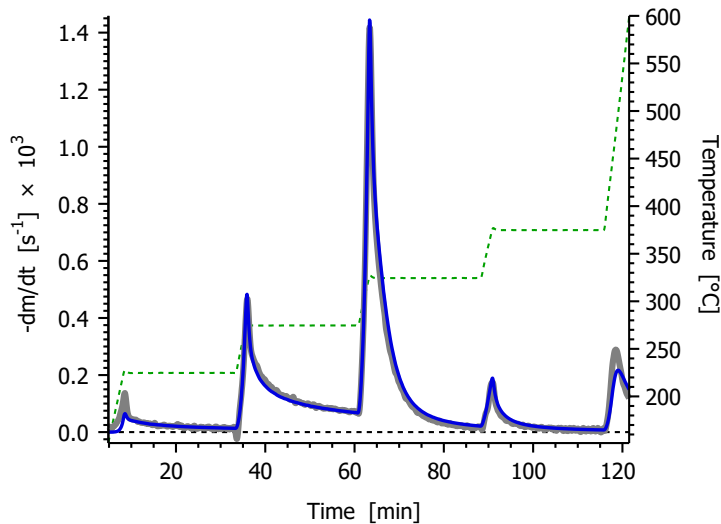
Relative deviation: 1.71%, Deviation: 0.029 µg/s  
rms rel. dev. of 4 experiments: 1.60%

Model:  $x=2\alpha-1$

$E(x) = 188.25T_0(x) + 30.08T_1(x) - 0.34T_2(x) + 11.2T_3(x)$

$\log_{10} \tilde{A}(x) = 11.951T_0(x) - 1.725T_1(x) - 2.536T_2(x) - 0.71T_3(x) - 0.649T_4(x) - 0.241T_5(x)$

$c = 0.791$



**Wheat straw, 2mg, steps: 225 - 375°C**

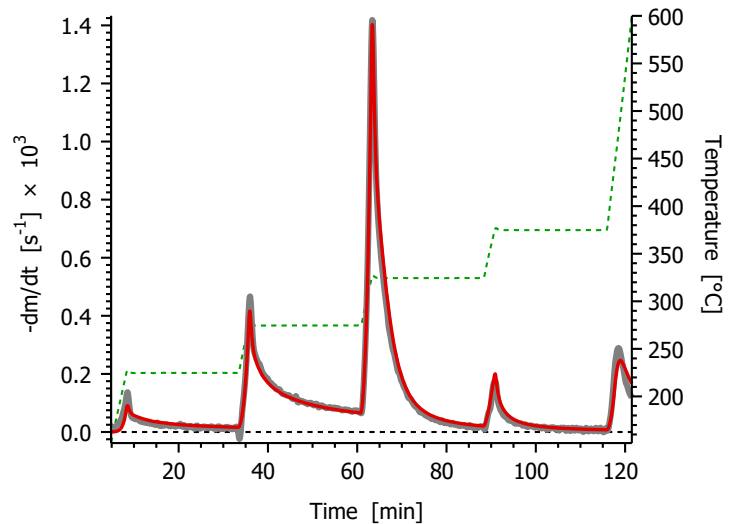
Relative deviation: 1.42%, Deviation: 0.040 µg/s  
rms rel. dev. of 4 experiments: 1.76%

Model:  $x=2\alpha-1$

$E(x) = 187.62$

$\log_{10} \tilde{A}(x) = 11.962T_0(x) - 4.518T_1(x) - 2.391T_2(x) - 1.785T_3(x) - 0.605T_4(x) - 0.271T_5(x)$

$c = 0.790$



**Wheat straw, 2mg, steps: 225 - 375°C**

Relative deviation: 1.33%, Deviation: 0.038 µg/s  
rms rel. dev. of 4 experiments: 1.60%

Model:  $x=2\alpha-1$

$E(x) = 188.25T_0(x) + 30.08T_1(x) - 0.34T_2(x) + 11.2T_3(x)$

$\log_{10} \tilde{A}(x) = 11.951T_0(x) - 1.725T_1(x) - 2.536T_2(x) - 0.71T_3(x) - 0.649T_4(x) - 0.241T_5(x)$

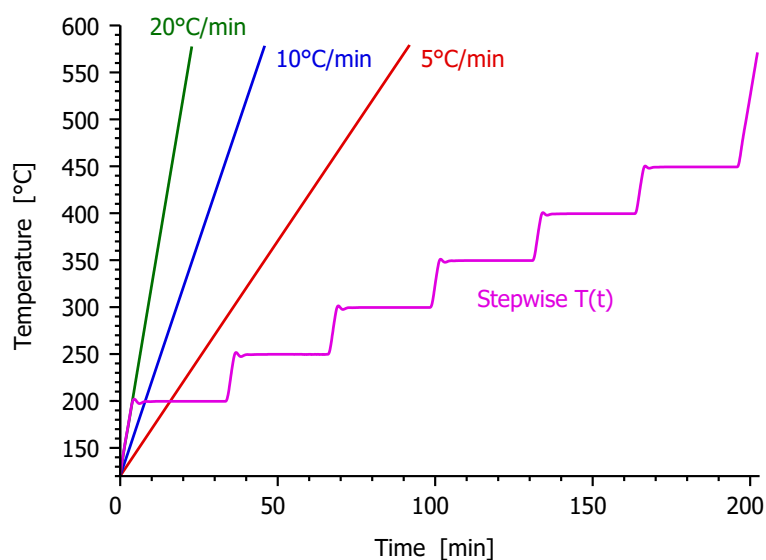
$c = 0.791$

## S4. Two Corncob Samples

Source of the data:

[S4] Trninić, M.; Wang, L.; Várhegyi, G.; Grønli, M.; Skreiberg, Ø.: Kinetics of corncob pyrolysis. *Energy Fuels* **2012**, 26, 2005-2013. doi: [10.1021/ef3002668](https://doi.org/10.1021/ef3002668) [Repository](#)

Four TGA experiments were available for each sample. The figure below shows the corresponding temperature programs. It is a redrawn/rearranged version of Figure 1 of the cited paper.



**Figure S4.1:** Temperature programs used for the TGA experiments of this section.

### S4.1. A corncob sample from Oahu, Hawaii

#### Model with constant E:

Input file: "P\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 184.58533$$

$$\log_{10}\tilde{A}(x)= 13.791489 -1.424139x +2.858664x^2 +2.334976x^3 -6.331752x^4 -7.615808x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 12.846414T_0(x) -4.432787T_1(x) -1.736544T_2(x) -1.796196T_3(x) -.791469T_4(x) -.475988T_5(x)$$

#### Model with third order E(α):

Input file: "P\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

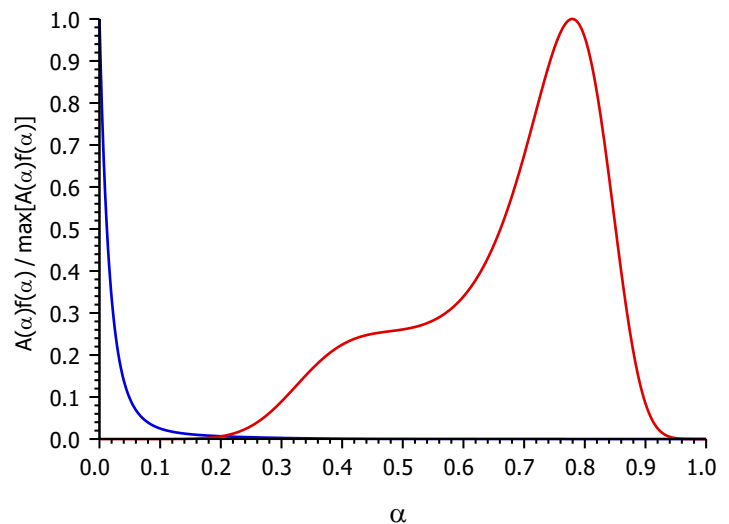
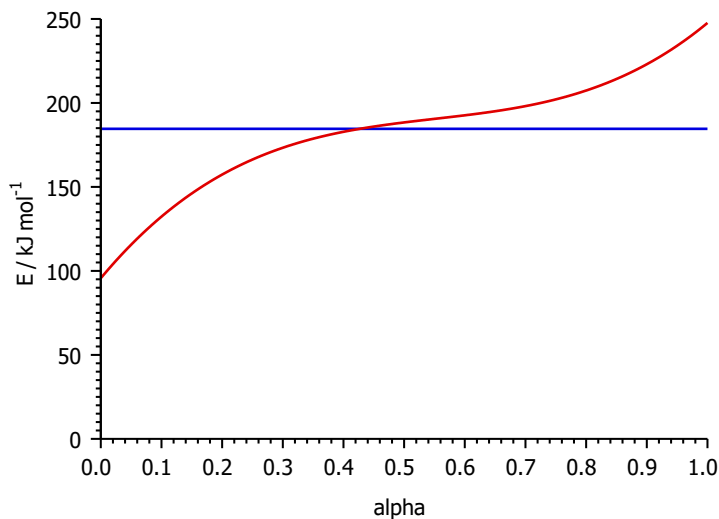
$$E(x)= 188.396709 +22.413672x -16.740878x^2 +53.57418x^3$$

$$\log_{10}\tilde{A}(x)= 14.144895 +.6288517x +1.089066x^2 +6.700328x^3 -6.351632x^4 -5.549744x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 180.02627T_0(x) +62.594307T_1(x) -8.370439T_2(x) +13.393545T_3(x)$$

$$\log_{10}\tilde{A}(x)= 12.307566T_0(x) +2.1855077T_1(x) -2.631283T_2(x) -.059213T_3(x) -.793954T_4(x) -.346859T_5(x)$$



#### E(α) = polynomial of (2α-1)

Parameter file: P\_0,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 17.02 \quad E(0)= 184.6 \quad \log_{10}\tilde{A}(1)= 3.61 \quad E(1)= 184.6$$

$$\text{mean } \log_{10}\tilde{A}= 13.48 \quad \text{mean } E= 184.6$$

Parameter file: P\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 7.10 \quad E(0)= 95.7 \quad \log_{10}\tilde{A}(1)= 10.66 \quad E(1)= 247.6$$

$$\text{mean } \log_{10}\tilde{A}= 13.24 \quad \text{mean } E= 182.8$$

#### Plot of A(α)f(α) / max[A(α)f(α)]

Parameter file: P\_0,5\_oneC.PAR

$$A(0)f(0)= 1.055E+17 \quad E(0)= 184.6 \quad A(1)f(1)= 0.00 \quad E(1)= 184.6$$

$$\text{mean } A(\alpha)f(\alpha)= 2.323E+15 \quad \text{mean } E= 184.6$$

$$\text{max } A(\alpha)f(\alpha)= 1.055E+17 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 184.6$$

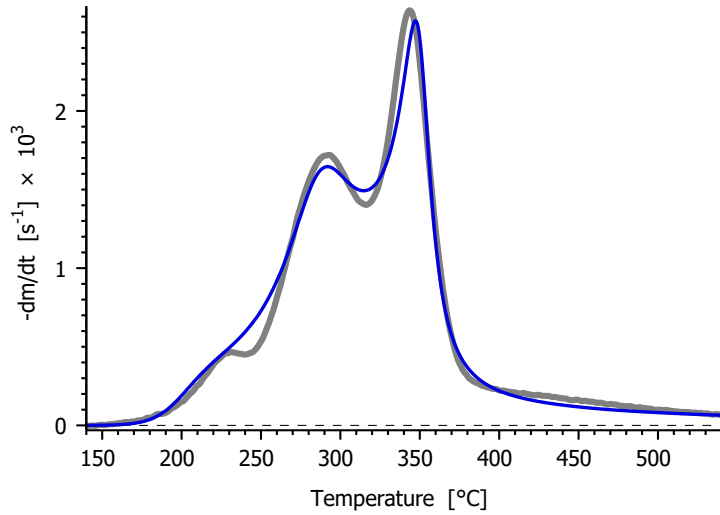
Parameter file: P\_3,5\_oneC.PAR

$$A(0)f(0)= 1.267E+07 \quad E(0)= 95.7 \quad A(1)f(1)= 0.00 \quad E(1)= 247.6$$

$$\text{mean } A(\alpha)f(\alpha)= 7.053E+13 \quad \text{mean } E= 182.8$$

$$\text{max } A(\alpha)f(\alpha)= 2.676E+14 \quad \text{at } \alpha= 0.779 \quad \text{and } E= 205.0$$

Figures illustrating the fit quality (cf. Figure 4 in reference [S4])



**Corncob (Pioneer Hi-Bred, Oahu), 20°C/min**

Relative deviation: 2.98%, Deviation: 0.40 µg/s

rms rel. dev. of 4 experiments: 3.09%

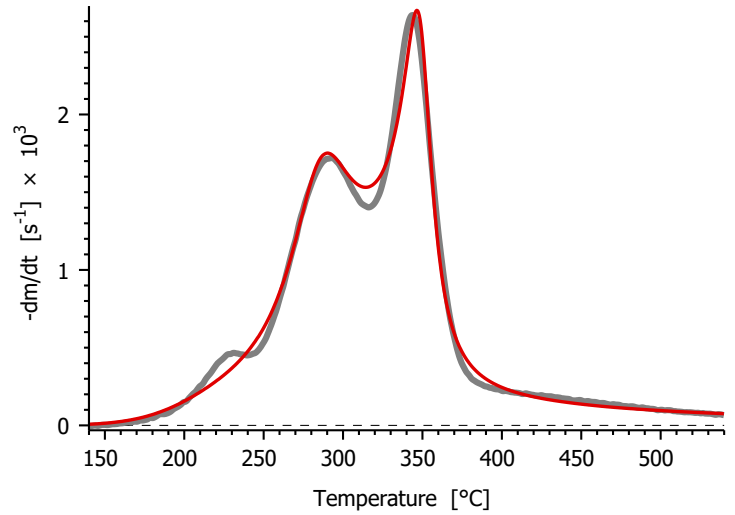
Model:  $x=2\alpha-1$

$E(x) = 184.59$

$\log_{10} \tilde{A}(x) = 12.846T_0(x) - 4.433T_1(x) - 1.737T_2(x) - 1.796T_3(x)$

$-0.791T_4(x) - 0.476T_5(x)$

$c = 0.741$



**Corncob (Pioneer Hi-Bred, Oahu), 20°C/min**

Relative deviation: 2.21%, Deviation: 0.30 µg/s

rms rel. dev. of 4 experiments: 2.44%

Model:  $x=2\alpha-1$

$E(x) = 180.03T_0(x) + 62.59T_1(x) - 8.37T_2(x) + 13.39T_3(x)$

$\log_{10} \tilde{A}(x) = 12.308T_0(x) + 2.186T_1(x) - 2.631T_2(x) - 0.059T_3(x)$

$-0.794T_4(x) - 0.347T_5(x)$

$c = 0.730$

## S4.2. A corncob sample from Serbia

### Model with constant E:

Input file: "S\_0,5\_oneC.PAR"

The model:

$$x=2\alpha-1$$

$$E= 186.56647$$

$$\log_{10}\tilde{A}(x)= 13.85819 - .8057x + 1.842452x^2 + .374848x^3 - 3.729488x^4 - 3.0152x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 13.380858T_0(x) - 2.409064T_1(x) - .943518T_2(x) - .848538T_3(x) - .466186T_4(x) - .18845T_5(x)$$

### Model with third order E( $\alpha$ ):

Input file: "S\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

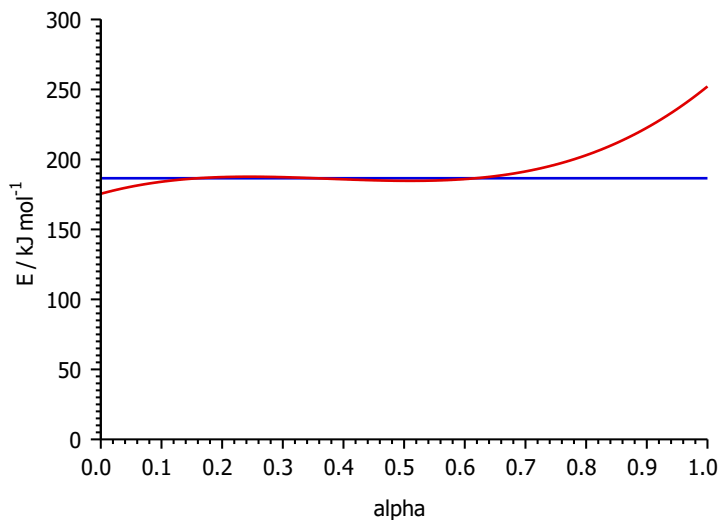
$$E(x)= 184.718266 - 1.2145034x + 29.088348x^2 + 39.5551832x^3$$

$$\log_{10}\tilde{A}(x)= 13.626923 - .81002x + 4.619062x^2 + 2.860636x^3 - 5.76796x^4 - 3.881776x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 199.26244T_0(x) + 28.451884T_1(x) + 14.544174T_2(x) + 9.8887958T_3(x)$$

$$\log_{10}\tilde{A}(x)= 13.773469T_0(x) - 1.090653T_1(x) - .574449T_2(x) - .497896T_3(x) - .720995T_4(x) - .242611T_5(x)$$



#### E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)

Parameter file: S\_0,5\_oneC.PAR

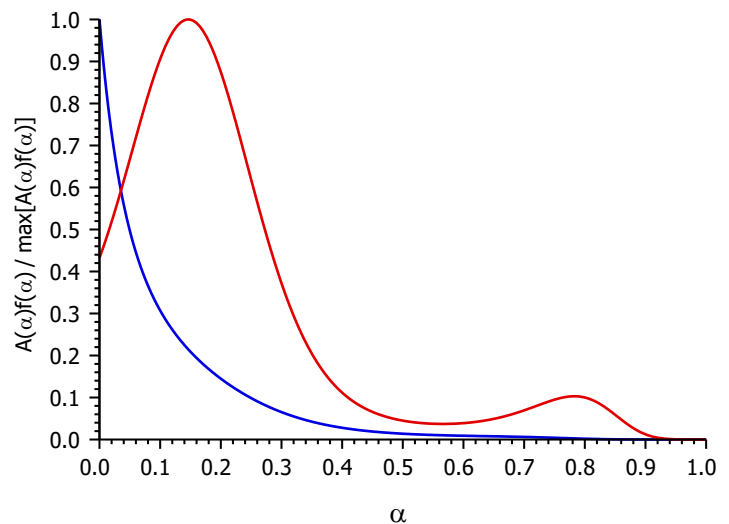
$$\log_{10}\tilde{A}(0)= 15.42 \quad E(0)= 186.6 \quad \log_{10}\tilde{A}(1)= 8.53 \quad E(1)= 186.6$$

$$\text{mean } \log_{10}\tilde{A}= 13.73 \quad \text{mean } E= 186.6$$

Parameter file: S\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 14.31 \quad E(0)= 175.5 \quad \log_{10}\tilde{A}(1)= 10.65 \quad E(1)= 252.1$$

$$\text{mean } \log_{10}\tilde{A}= 14.01 \quad \text{mean } E= 194.4$$



#### Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]

Parameter file: S\_0,5\_oneC.PAR

$$A(0)f(0)= 2.613E+15 \quad E(0)= 186.6 \quad A(1)f(1)= 0.00 \quad E(1)= 186.6$$

$$\text{mean } A(\alpha)f(\alpha)= 2.478E+14 \quad \text{mean } E= 186.6$$

$$\text{max } A(\alpha)f(\alpha)= 2.613E+15 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 186.6$$

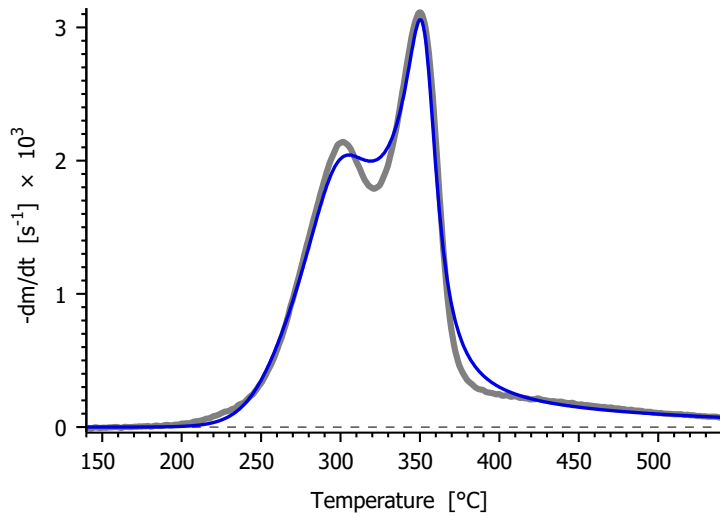
Parameter file: S\_3,5\_oneC.PAR

$$A(0)f(0)= 2.038E+14 \quad E(0)= 175.5 \quad A(1)f(1)= 0.00 \quad E(1)= 252.1$$

$$\text{mean } A(\alpha)f(\alpha)= 1.310E+14 \quad \text{mean } E= 194.4$$

$$\text{max } A(\alpha)f(\alpha)= 4.713E+14 \quad \text{at } \alpha= 0.146 \quad \text{and } E= 186.1$$

Figures illustrating the fit quality (cf. Figure 4 in reference [S4])



**Corncob (ZP Maize Hybrid 505, Serbia), 20°C/min**

Relative deviation: 2.46%, Deviation: 0.39  $\mu\text{g/s}$

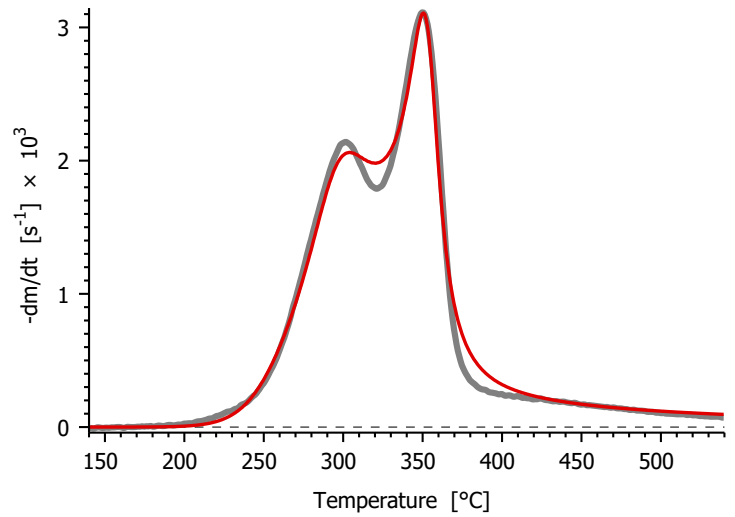
rms rel. dev. of 4 experiments: 2.21%

Model:  $x=2\alpha-1$

$E(x) = 186.57$

$\log_{10} \tilde{A}(x) = 13.381T_0(x) - 2.409T_1(x) - 0.944T_2(x) - 0.849T_3(x) - 0.466T_4(x) - 0.188T_5(x)$

$c = 0.766$



**Corncob (ZP Maize Hybrid 505, Serbia), 20°C/min**

Relative deviation: 2.37%, Deviation: 0.38  $\mu\text{g/s}$

rms rel. dev. of 4 experiments: 2.17%

Model:  $x=2\alpha-1$

$E(x) = 199.26T_0(x) + 28.45T_1(x) + 14.54T_2(x) + 9.89T_3(x)$

$\log_{10} \tilde{A}(x) = 13.773T_0(x) - 1.091T_1(x) - 0.574T_2(x) - 0.498T_3(x) - 0.721T_4(x) - 0.243T_5(x)$

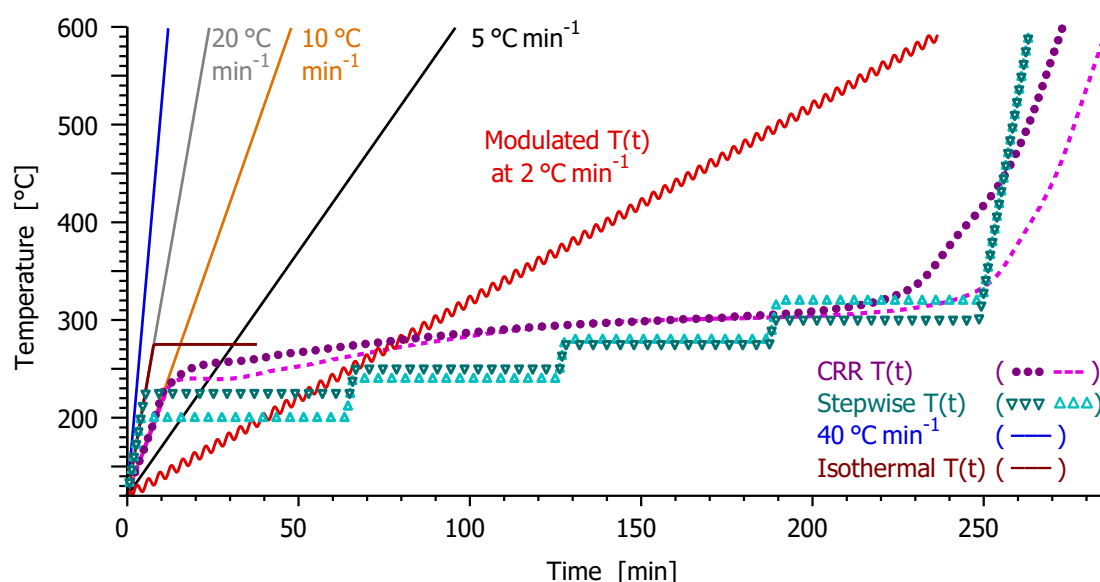
$c = 0.799$

## S5. Birch and Spruce

Source of the data:

[S5] Tapasvi, D.; Khalil, R.; Várhegyi, G.; Tran, K.-Q.; Grønli, M.; Skreiberg, Ø. Thermal decomposition kinetics of woods with an emphasis on torrefaction. *Energy Fuels* **2013**, *27*, 6134-6145. doi: [10.1021/ef4016075](https://doi.org/10.1021/ef4016075)  
[Repository](#)

The birch and spruce samples were taken from standard Norwegian construction boards. Nine TGA experiments were available for each sample: four with linear heating (5, 10, 20 and 40 °C/min); two with stepwise heating; a modulated  $T(t)$ ; a “constant reaction rate” (CRR)  $T(t)$ ; and an isothermal  $T(t)$  at 275°C. (The latter was evaluated together with its heat-up section, as shown in the next pages.) The figure below shows the corresponding temperature programs. It is a redrawn/rearranged version of Figure 1 of the cited paper. Note that the “constant reaction rate” temperature programs are determined by the apparatus and they differ from sample to sample. The dashed line and the dotted line in Figure S5.1 belong to the birch and the wood samples, respectively.



**Figure S5.1:** Temperature programs used for the TGA experiments of this section.

## S5.1. Birch

### Model with constant E:

Input file: "B\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 171.15347$$

$$\log_{10}\tilde{A}(x)= 11.76219 - .555777x + 2.408056x^2 + .40424x^3 - 2.620136x^4 - 1.930992x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 11.983667T_0(x) - 1.459467T_1(x) - .10604T_2(x) - .502375T_3(x) - .327517T_4(x) - .120687T_5(x)$$

### Model with third order E( $\alpha$ ):

Input file: "B\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

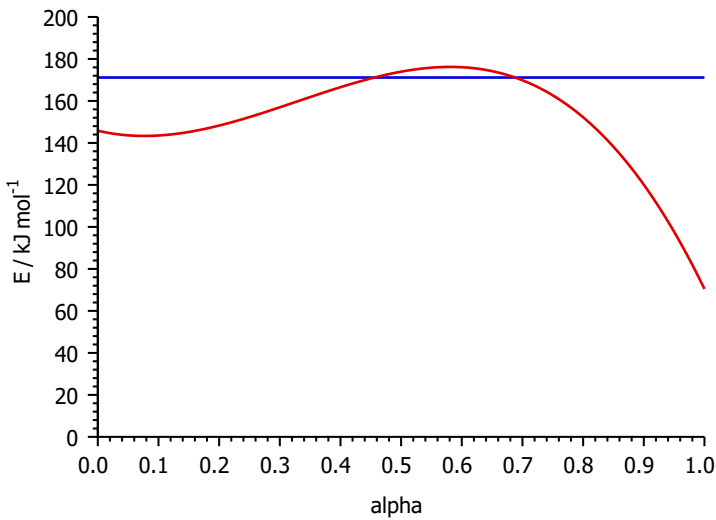
$$E(x)= 173.93757 + 26.34408x - 65.79054x^2 - 64.03504x^3$$

$$\log_{10}\tilde{A}(x)= 12.0004161 + 1.90238x - 3.923592x^2 - 5.51472x^3 - 1.860768x^4 - 1.133216x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 141.0423T_0(x) - 21.6822T_1(x) - 32.89527T_2(x) - 16.00876T_3(x)$$

$$\log_{10}\tilde{A}(x)= 9.3408321T_0(x) - 2.94192T_1(x) - 2.89218T_2(x) - 1.73281T_3(x) - .232596T_4(x) - .070826T_5(x)$$



#### E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)

Parameter file: B\_0,5\_oneC.PAR

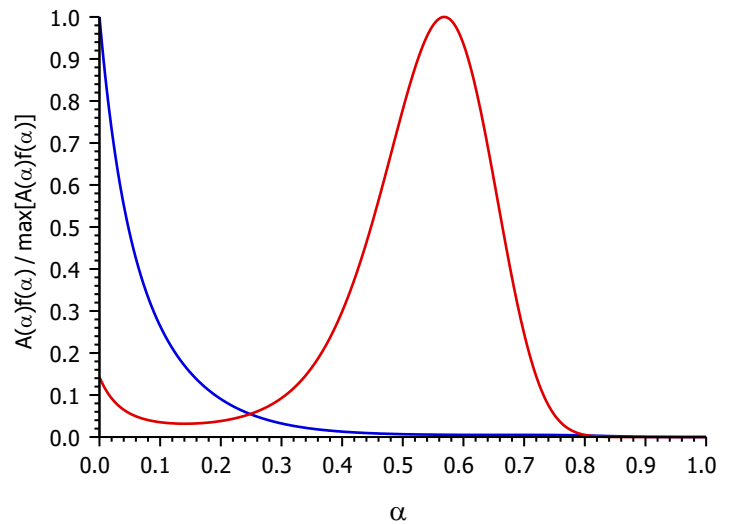
$$\log_{10}\tilde{A}(0)= 13.63 \quad E(0)= 171.2 \quad \log_{10}\tilde{A}(1)= 9.47 \quad E(1)= 171.2$$

$$\text{mean } \log_{10}\tilde{A}= 12.04 \quad \text{mean } E= 171.2$$

Parameter file: B\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 10.96 \quad E(0)= 145.8 \quad \log_{10}\tilde{A}(1)= 1.47 \quad E(1)= 70.5$$

$$\text{mean } \log_{10}\tilde{A}= 10.32 \quad \text{mean } E= 152.0$$



#### Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]

Parameter file: B\_0,5\_oneC.PAR

$$A(0)f(0)= 4.292E+13 \quad E(0)= 171.2 \quad A(1)f(1)= 0.00 \quad E(1)= 171.2$$

$$\text{mean } A(\alpha)f(\alpha)= 3.416E+12 \quad \text{mean } E= 171.2$$

$$\text{max } A(\alpha)f(\alpha)= 4.292E+13 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 171.2$$

Parameter file: B\_3,5\_oneC.PAR

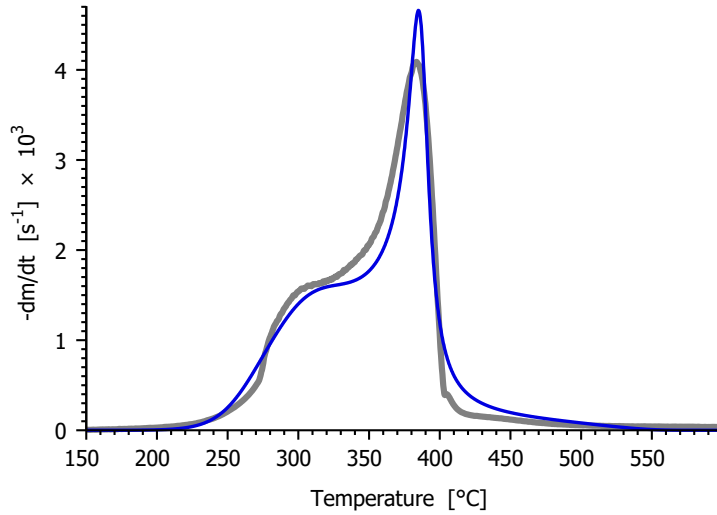
$$A(0)f(0)= 9.154E+10 \quad E(0)= 145.8 \quad A(1)f(1)= 0.00 \quad E(1)= 70.5$$

$$\text{mean } A(\alpha)f(\alpha)= 1.591E+11 \quad \text{mean } E= 152.0$$

$$\text{max } A(\alpha)f(\alpha)= 6.419E+11 \quad \text{at } \alpha= 0.568 \quad \text{and } E= 176.1$$



Figures illustrating the fit quality (cf. Figure 5 in reference [S5])



**Birch, 20°C/min, 3mg**

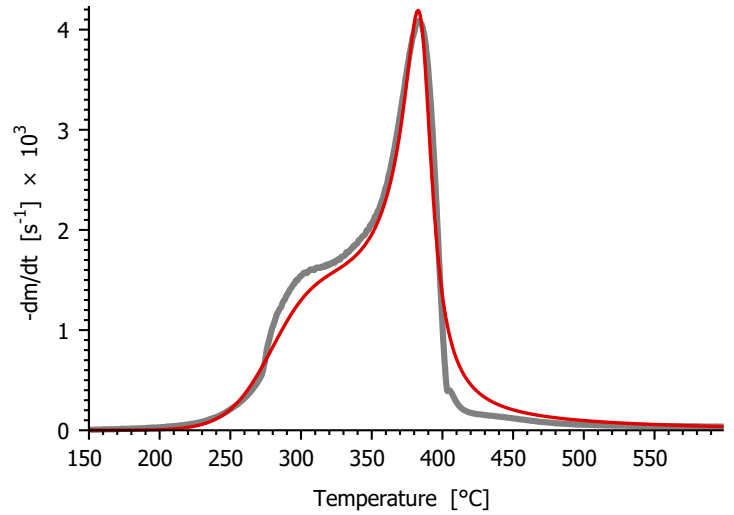
Relative deviation: 4.32%, Deviation: 0.53 µg/s  
rms rel. dev. of 9 experiments: 5.17%

Model:  $x=2\alpha-1$

$E(x) = 171.15$

$\log_{10} \tilde{A}(x) = 11.984T_0(x) - 1.459T_1(x) - .106T_2(x) - .502T_3(x) - .328T_4(x) - .121T_5(x)$

$c = 0.876$



**Birch, 20°C/min, 3mg**

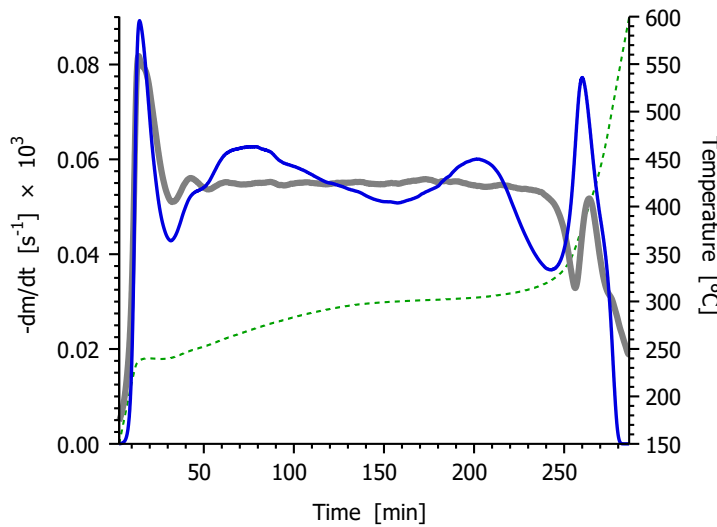
Relative deviation: 3.64%, Deviation: 0.45 µg/s  
rms rel. dev. of 9 experiments: 3.43%

Model:  $x=2\alpha-1$

$E(x) = 141.04T_0(x) - 21.68T_1(x) - 32.9T_2(x) - 16.01T_3(x)$

$\log_{10} \tilde{A}(x) = 9.341T_0(x) - 2.942T_1(x) - 2.892T_2(x) - 1.733T_3(x) - .233T_4(x) - .071T_5(x)$

$c = 0.906$



**Birch, CRR T(t) (10°C/min), 10mg**

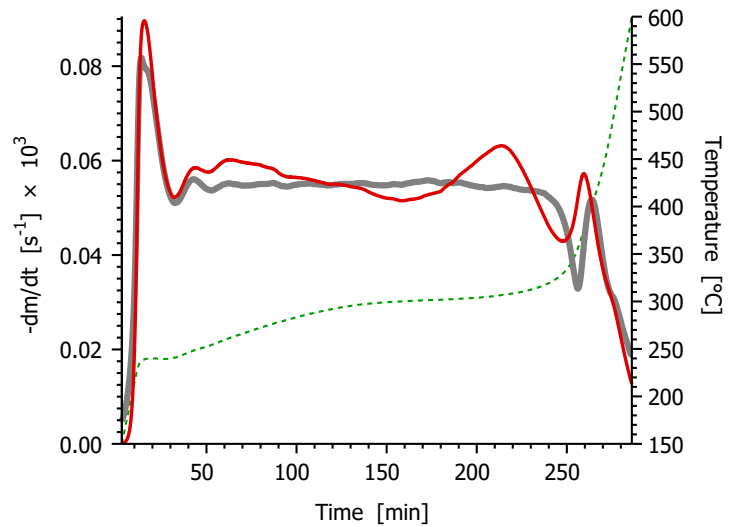
Relative deviation: 11.09%, Deviation: 0.090 µg/s  
rms rel. dev. of 9 experiments: 5.17%

Model:  $x=2\alpha-1$

$E(x) = 171.15$

$\log_{10} \tilde{A}(x) = 11.984T_0(x) - 1.459T_1(x) - .106T_2(x) - .502T_3(x) - .328T_4(x) - .121T_5(x)$

$c = 0.876$



**Birch, CRR T(t) (10°C/min), 10mg**

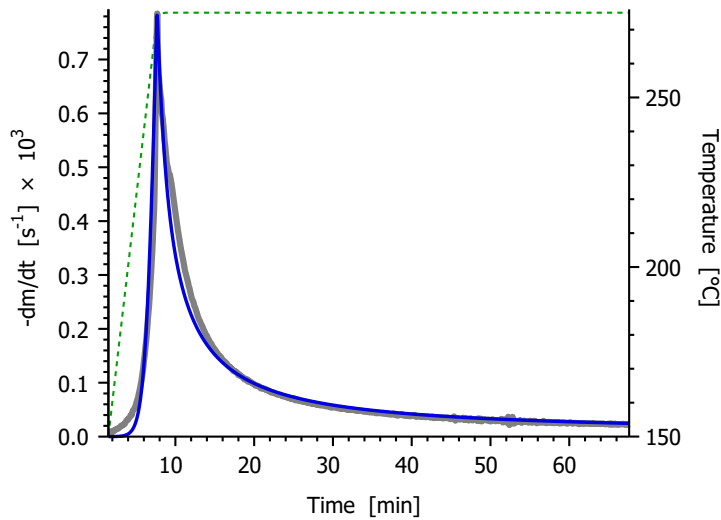
Relative deviation: 6.09%, Deviation: 0.049 µg/s  
rms rel. dev. of 9 experiments: 3.43%

Model:  $x=2\alpha-1$

$E(x) = 141.04T_0(x) - 21.68T_1(x) - 32.9T_2(x) - 16.01T_3(x)$

$\log_{10} \tilde{A}(x) = 9.341T_0(x) - 2.942T_1(x) - 2.892T_2(x) - 1.733T_3(x) - .233T_4(x) - .071T_5(x)$

$c = 0.906$



**Birch, isothermal: 20°C/min till 275°C (60min), 4mg**

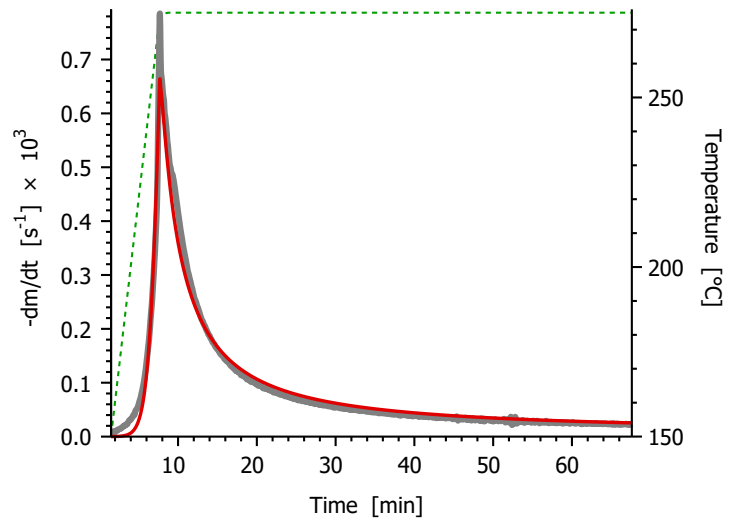
Relative deviation: 2.89%, Deviation: 0.088 µg/s  
rms rel. dev. of 9 experiments: 5.17%

Model:  $x=2\alpha-1$

$E(x) = 171.15$

$\log_{10} \tilde{A}(x) = 11.984T_0(x) - 1.459T_1(x) - .106T_2(x) - .502T_3(x) - .328T_4(x) - .121T_5(x)$

$c = 0.876$



**Birch, isothermal: 20°C/min till 275°C (60min), 4mg**

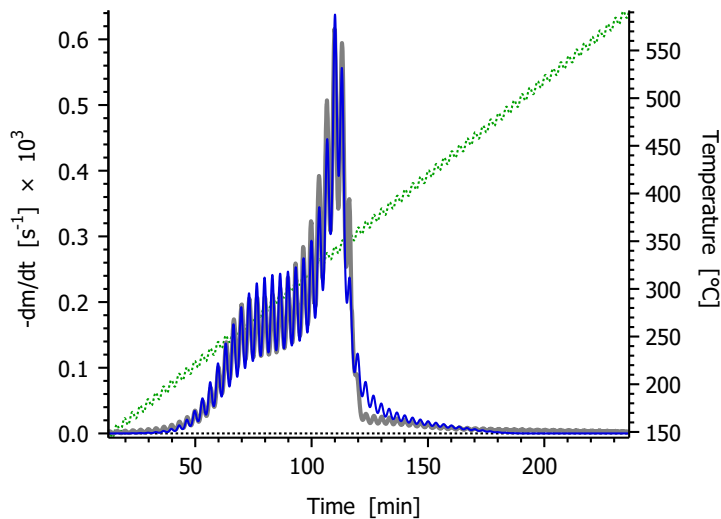
Relative deviation: 1.97%, Deviation: 0.060 µg/s  
rms rel. dev. of 9 experiments: 3.43%

Model:  $x=2\alpha-1$

$E(x) = 141.04T_0(x) - 21.68T_1(x) - 32.9T_2(x) - 16.01T_3(x)$

$\log_{10} \tilde{A}(x) = 9.341T_0(x) - 2.942T_1(x) - 2.892T_2(x) - 1.733T_3(x) - .233T_4(x) - .071T_5(x)$

$c = 0.906$



**Birch, modulated T(t) (2°C/min), 10mg**

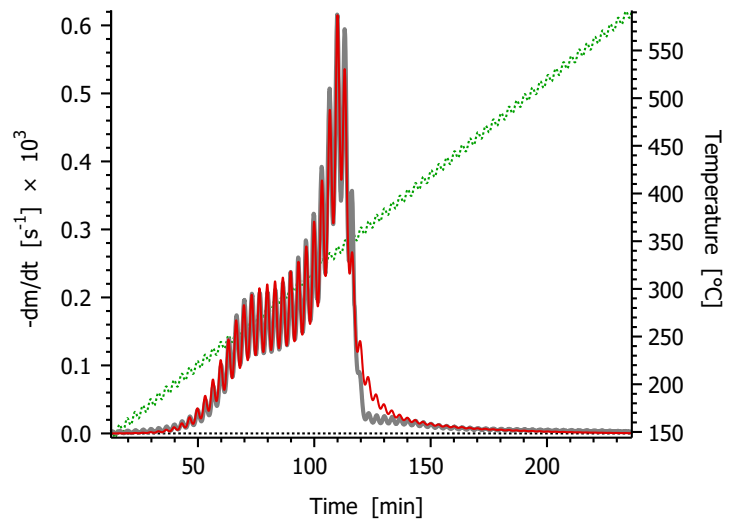
Relative deviation: 2.81%, Deviation: 0.16 µg/s  
rms rel. dev. of 9 experiments: 5.17%

Model:  $x=2\alpha-1$

$E(x) = 171.15$

$\log_{10} \tilde{A}(x) = 11.984T_0(x) - 1.459T_1(x) - .106T_2(x) - .502T_3(x) - .328T_4(x) - .121T_5(x)$

$c = 0.876$



**Birch, modulated T(t) (2°C/min), 10mg**

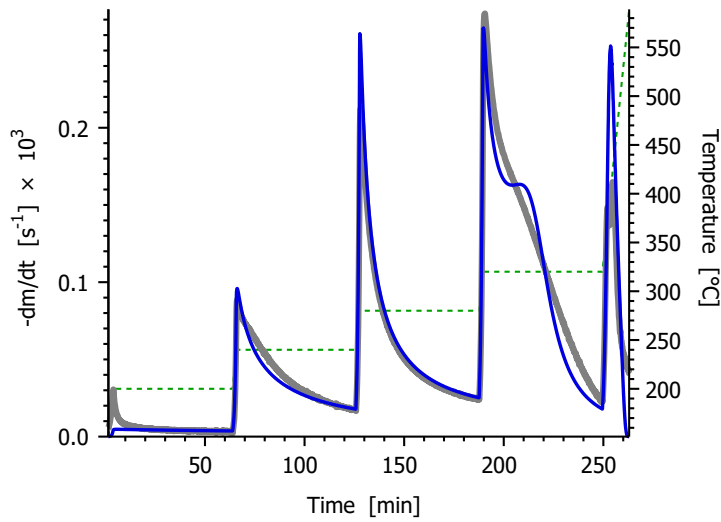
Relative deviation: 2.31%, Deviation: 0.13 µg/s  
rms rel. dev. of 9 experiments: 3.43%

Model:  $x=2\alpha-1$

$E(x) = 141.04T_0(x) - 21.68T_1(x) - 32.9T_2(x) - 16.01T_3(x)$

$\log_{10} \tilde{A}(x) = 9.341T_0(x) - 2.942T_1(x) - 2.892T_2(x) - 1.733T_3(x) - .233T_4(x) - .071T_5(x)$

$c = 0.906$



**Birch, stepwise T(t) 200-320°C, 5mg**

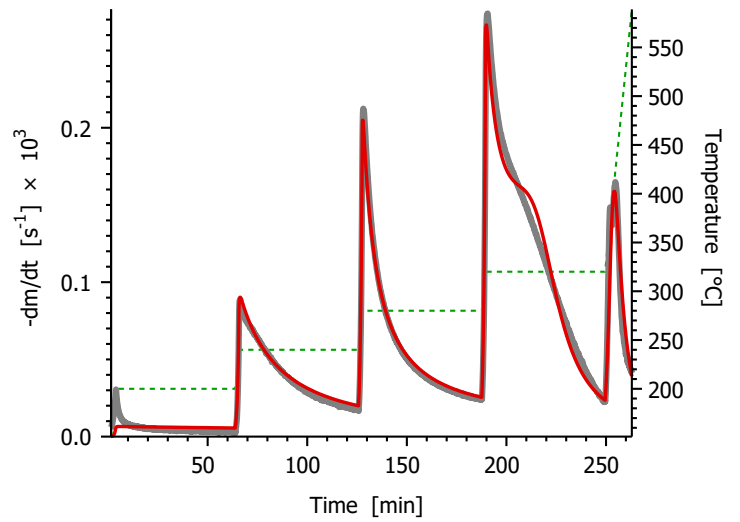
Relative deviation: 5.23%, Deviation: 0.075 µg/s  
rms rel. dev. of 9 experiments: 5.17%

Model:  $x=2\alpha-1$

$E(x) = 171.15$

$\log_{10} \tilde{A}(x) = 11.984T_0(x) - 1.459T_1(x) - .106T_2(x) - .502T_3(x) - .328T_4(x) - .121T_5(x)$

$c = 0.876$



**Birch, stepwise T(t) 200-320°C, 5mg**

Relative deviation: 2.51%, Deviation: 0.036 µg/s  
rms rel. dev. of 9 experiments: 3.43%

Model:  $x=2\alpha-1$

$E(x) = 141.04T_0(x) - 21.68T_1(x) - 32.9T_2(x) - 16.01T_3(x)$

$\log_{10} \tilde{A}(x) = 9.341T_0(x) - 2.942T_1(x) - 2.892T_2(x) - 1.733T_3(x) - .233T_4(x) - .071T_5(x)$

$c = 0.906$

## S5.2. Spruce

### Model with constant E:

Input file: "S\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 168.22096$$

$$\log_{10}\tilde{A}(x)= 11.535869 - .420241x + 1.585322x^2 + .849588x^3 - 2.744856x^4 - 3.429088x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 11.299209T_0(x) - 1.92623T_1(x) - .579767T_2(x) - .859193T_3(x) - .343107T_4(x) - .214318T_5(x)$$

### Model with third order E( $\alpha$ ):

Input file: "S\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

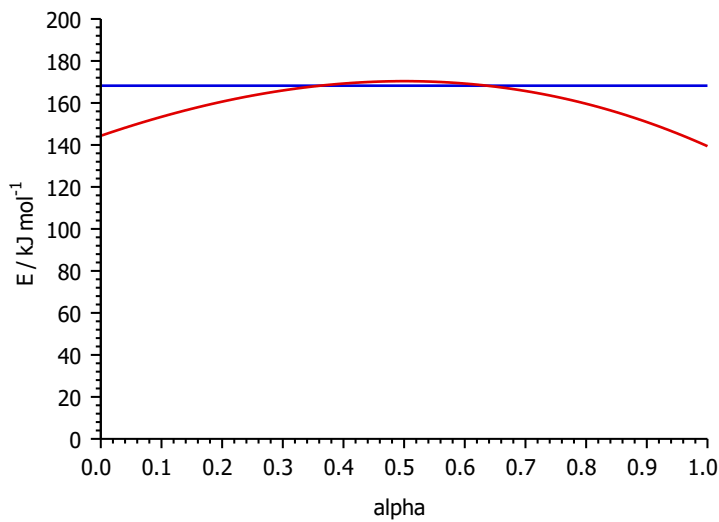
$$E(x)= 170.37188 + .090612x - 28.48678x^2 - 2.571172x^3$$

$$\log_{10}\tilde{A}(x)= 11.715329 - .385387x - .952078x^2 + .50058x^3 - 2.814936x^4 - 3.108848x^5$$

Expressed by Chebyshev polynomials of the first kind:

$$E(x)= 156.12849T_0(x) - 1.837767T_1(x) - 14.24339T_2(x) - .642793T_3(x)$$

$$\log_{10}\tilde{A}(x)= 10.183689T_0(x) - 1.952982T_1(x) - 1.883507T_2(x) - .84637T_3(x) - .351867T_4(x) - .194303T_5(x)$$



#### E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)

Parameter file: S\_0,5\_oneC.PAR

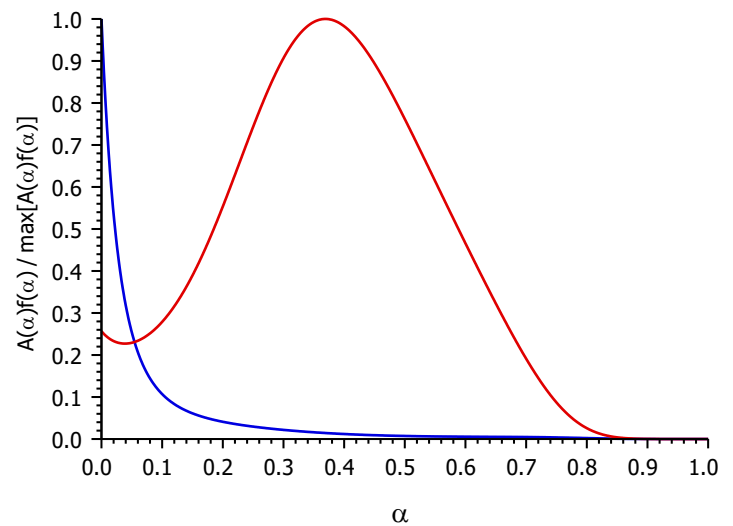
$$\log_{10}\tilde{A}(0)= 13.38 \quad E(0)= 168.2 \quad \log_{10}\tilde{A}(1)= 7.38 \quad E(1)= 168.2$$

$$\text{mean } \log_{10}\tilde{A}= 11.52 \quad \text{mean } E= 168.2$$

Parameter file: S\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 10.94 \quad E(0)= 144.4 \quad \log_{10}\tilde{A}(1)= 4.95 \quad E(1)= 139.4$$

$$\text{mean } \log_{10}\tilde{A}= 10.83 \quad \text{mean } E= 160.9$$



#### Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]

Parameter file: S\_0,5\_oneC.PAR

$$A(0)f(0)= 2.377E+13 \quad E(0)= 168.2 \quad A(1)f(1)= 0.00 \quad E(1)= 168.2$$

$$\text{mean } A(\alpha)f(\alpha)= 1.136E+12 \quad \text{mean } E= 168.2$$

$$\text{max } A(\alpha)f(\alpha)= 2.377E+13 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 168.2$$

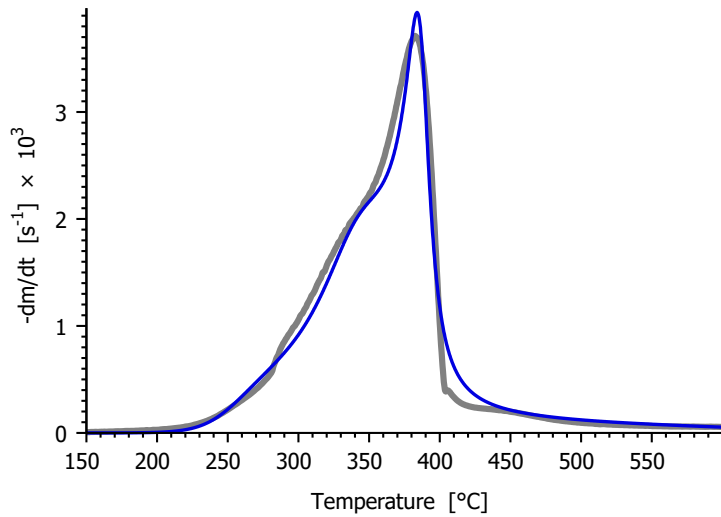
Parameter file: S\_3,5\_oneC.PAR

$$A(0)f(0)= 8.749E+10 \quad E(0)= 144.4 \quad A(1)f(1)= 0.00 \quad E(1)= 139.4$$

$$\text{mean } A(\alpha)f(\alpha)= 1.459E+11 \quad \text{mean } E= 160.9$$

$$\text{max } A(\alpha)f(\alpha)= 3.408E+11 \quad \text{at } \alpha= 0.369 \quad \text{and } E= 168.4$$

Figures illustrating the fit quality (cf. Figure 6 in reference [S5])



**Spruce, 20°C/min, 3mg**

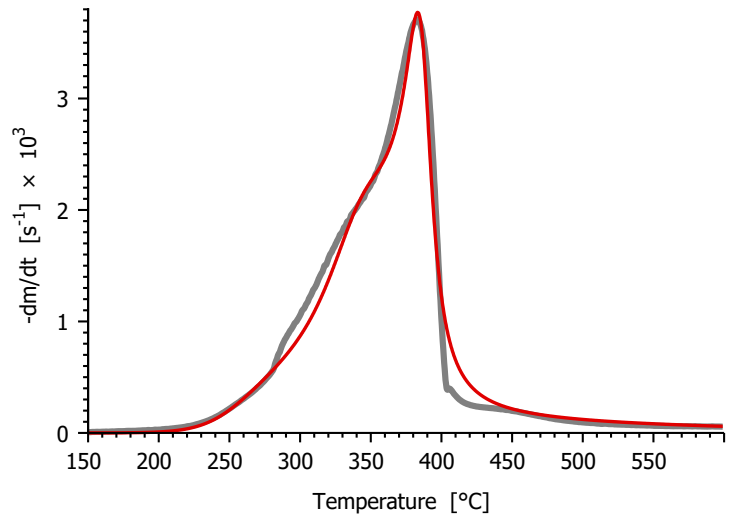
Relative deviation: 3.18%, Deviation: 0.38 µg/s  
rms rel. dev. of 9 experiments: 3.51%

Model:  $x=2\alpha-1$

$E(x) = 168.22$

$\log_{10} \tilde{A}(x) = 11.299T_0(x) - 1.926T_1(x) - .58T_2(x) - .859T_3(x) - .343T_4(x) - .214T_5(x)$

$c = 0.856$



**Spruce, 20°C/min, 3mg**

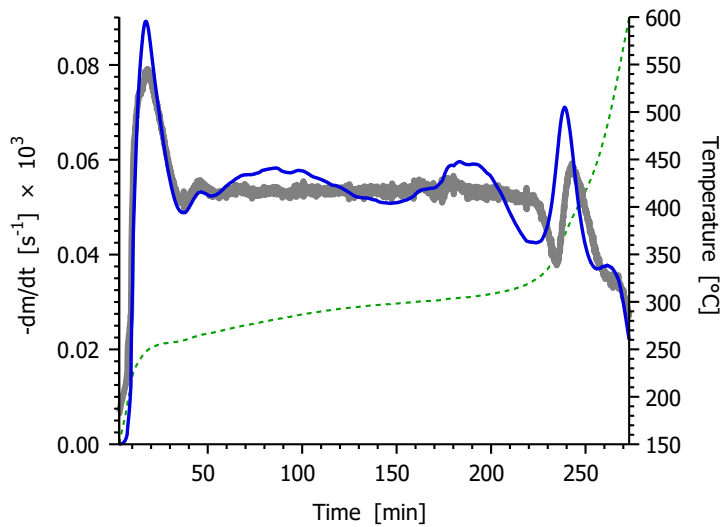
Relative deviation: 3.14%, Deviation: 0.38 µg/s  
rms rel. dev. of 9 experiments: 3.30%

Model:  $x=2\alpha-1$

$E(x) = 156.13T_0(x) - 1.84T_1(x) - 14.24T_2(x) - .64T_3(x)$

$\log_{10} \tilde{A}(x) = 10.184T_0(x) - 1.953T_1(x) - 1.884T_2(x) - .846T_3(x) - .352T_4(x) - .194T_5(x)$

$c = 0.866$



**Spruce, CRR T(t) (10°C/min), 9mg**

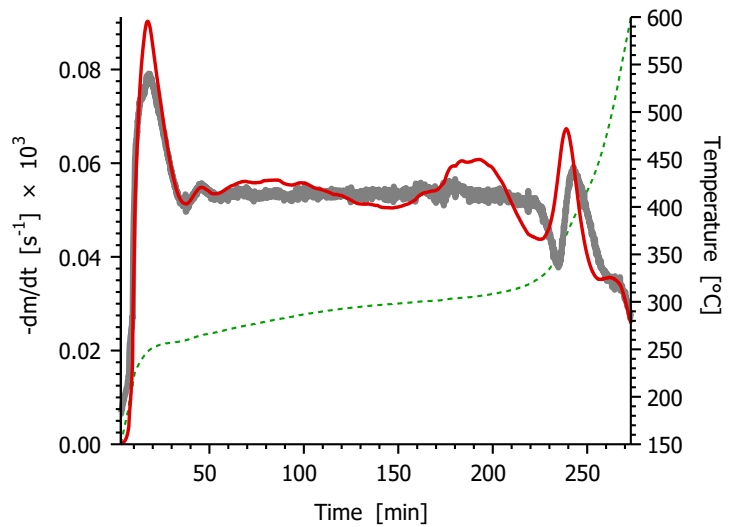
Relative deviation: 7.28%, Deviation: 0.053 µg/s  
rms rel. dev. of 9 experiments: 3.51%

Model:  $x=2\alpha-1$

$E(x) = 168.22$

$\log_{10} \tilde{A}(x) = 11.299T_0(x) - 1.926T_1(x) - .58T_2(x) - .859T_3(x) - .343T_4(x) - .214T_5(x)$

$c = 0.856$



**Spruce, CRR T(t) (10°C/min), 9mg**

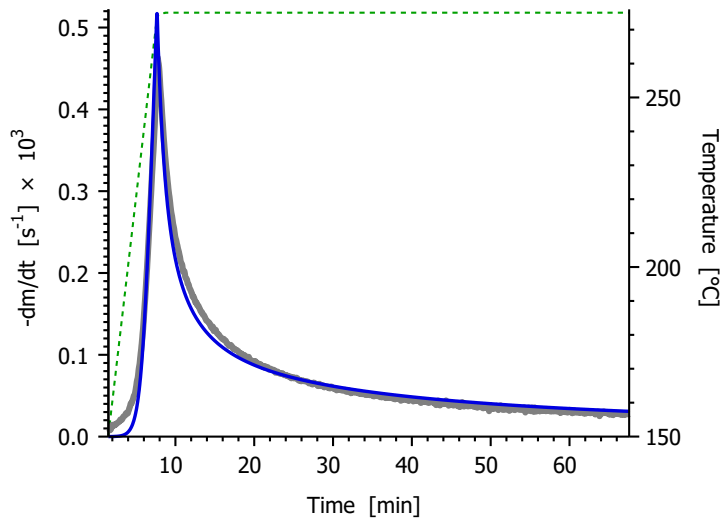
Relative deviation: 6.62%, Deviation: 0.048 µg/s  
rms rel. dev. of 9 experiments: 3.30%

Model:  $x=2\alpha-1$

$E(x) = 156.13T_0(x) - 1.84T_1(x) - 14.24T_2(x) - .64T_3(x)$

$\log_{10} \tilde{A}(x) = 10.184T_0(x) - 1.953T_1(x) - 1.884T_2(x) - .846T_3(x) - .352T_4(x) - .194T_5(x)$

$c = 0.866$



**Spruce, isothermal: 20°C/min till 275°C (60min), 3mg**

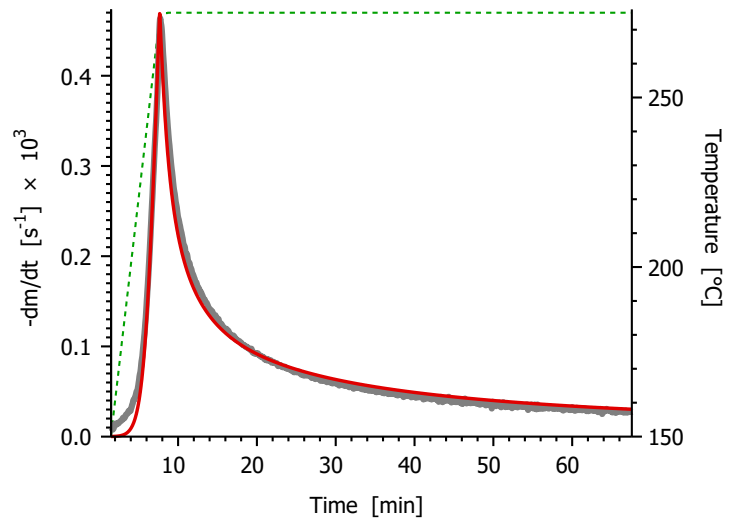
Relative deviation: 2.56%, Deviation: 0.037 µg/s  
rms rel. dev. of 9 experiments: 3.51%

Model:  $x=2\alpha-1$

$E(x) = 168.22$

$\log_{10} \tilde{A}(x) = 11.299T_0(x) - 1.926T_1(x) - .58T_2(x) - .859T_3(x) - .343T_4(x) - .214T_5(x)$

$c = 0.856$



**Spruce, isothermal: 20°C/min till 275°C (60min), 3mg**

3mg 2012-02-19

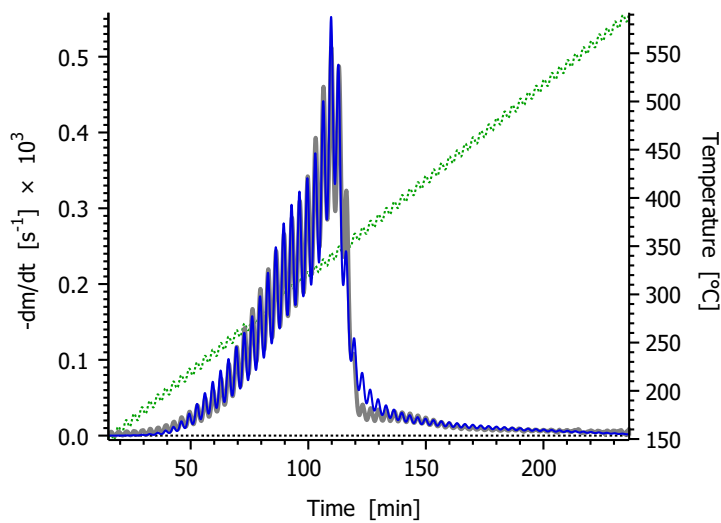
Relative deviation: 1.95%, Deviation: 0.028 µg/s  
rms rel. dev. of 9 experiments: 3.30%

Model:  $x=2\alpha-1$

$E(x) = 156.13T_0(x) - 1.84T_1(x) - 14.24T_2(x) - .64T_3(x)$

$\log_{10} \tilde{A}(x) = 10.184T_0(x) - 1.953T_1(x) - 1.884T_2(x) - .846T_3(x) - .352T_4(x) - .194T_5(x)$

$c = 0.866$



**Spruce, modulated T(t) (2°C/min), 3mg**

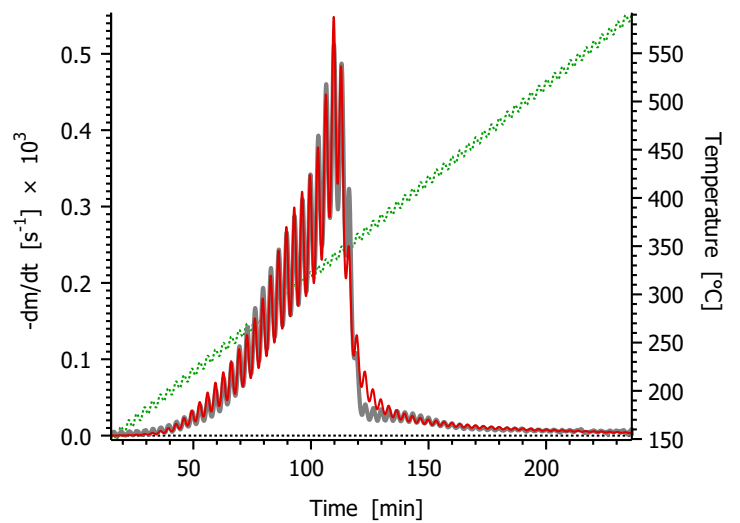
Relative deviation: 2.71%, Deviation: 0.046 µg/s  
rms rel. dev. of 9 experiments: 3.51%

Model:  $x=2\alpha-1$

$E(x) = 168.22$

$\log_{10} \tilde{A}(x) = 11.299T_0(x) - 1.926T_1(x) - .58T_2(x) - .859T_3(x) - .343T_4(x) - .214T_5(x)$

$c = 0.856$



**Spruce, modulated T(t) (2°C/min), 3mg**

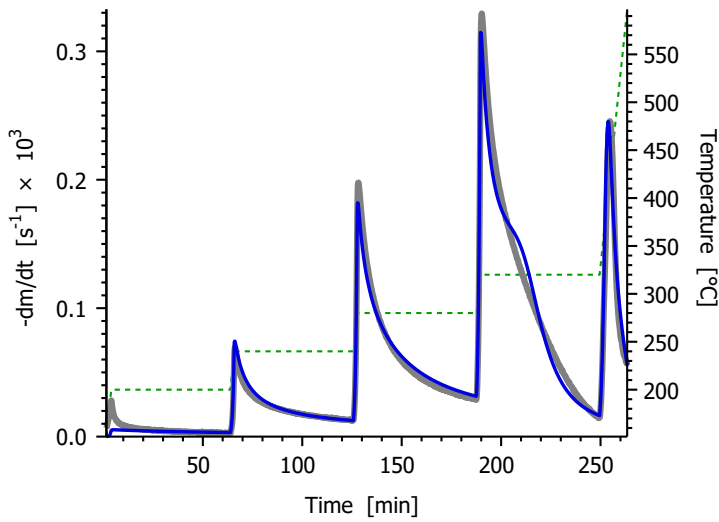
Relative deviation: 2.59%, Deviation: 0.044 µg/s  
rms rel. dev. of 9 experiments: 3.30%

Model:  $x=2\alpha-1$

$E(x) = 156.13T_0(x) - 1.84T_1(x) - 14.24T_2(x) - .64T_3(x)$

$\log_{10} \tilde{A}(x) = 10.184T_0(x) - 1.953T_1(x) - 1.884T_2(x) - .846T_3(x) - .352T_4(x) - .194T_5(x)$

$c = 0.866$



**Spruce, stepwise T(t) 200-320°C, 4mg**

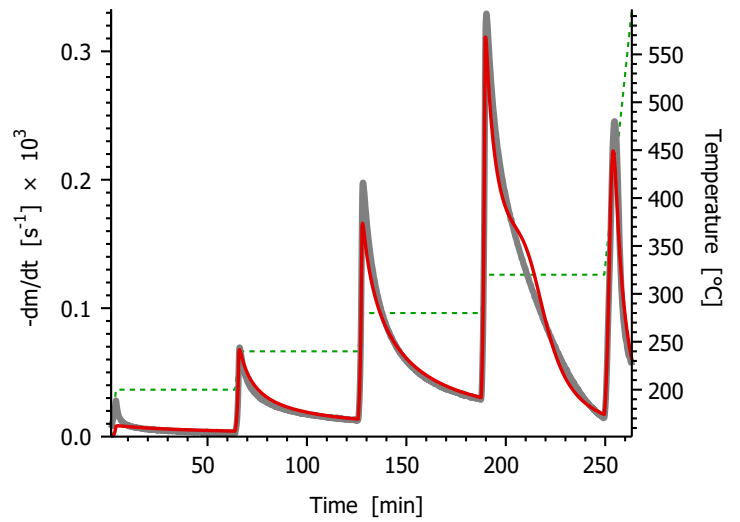
Relative deviation: 2.64%, Deviation: 0.033 µg/s  
rms rel. dev. of 9 experiments: 3.51%

Model:  $x=2\alpha-1$

$E(x) = 168.22$

$\log_{10} \tilde{A}(x) = 11.299T_0(x) - 1.926T_1(x) - .58T_2(x) - .859T_3(x) - .343T_4(x) - .214T_5(x)$

$c = 0.856$



**Spruce, stepwise T(t) 200-320°C, 4mg**

Relative deviation: 2.66%, Deviation: 0.033 µg/s  
rms rel. dev. of 9 experiments: 3.30%

Model:  $x=2\alpha-1$

$E(x) = 156.13T_0(x) - 1.84T_1(x) - 14.24T_2(x) - .64T_3(x)$

$\log_{10} \tilde{A}(x) = 10.184T_0(x) - 1.953T_1(x) - 1.884T_2(x) - .846T_3(x) - .352T_4(x) - .194T_5(x)$

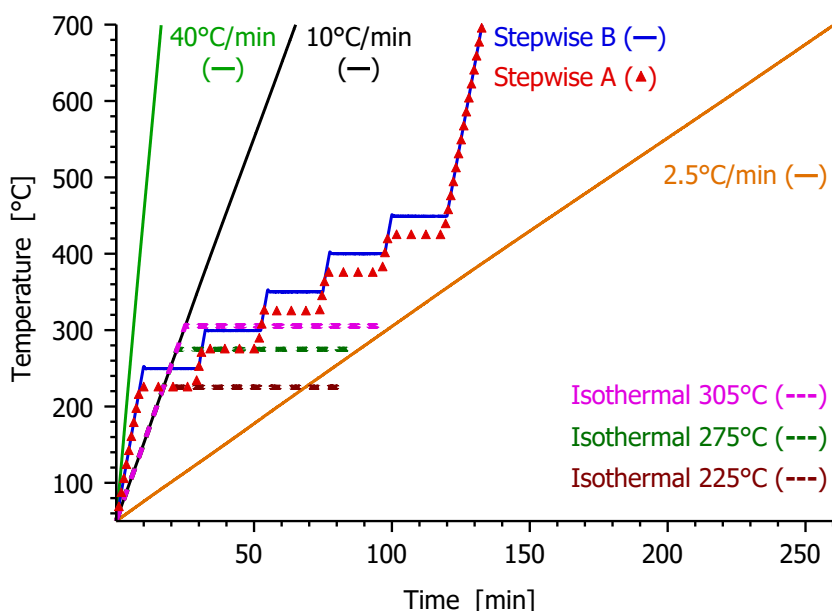
$c = 0.866$

## S6. Bark and Wood

Source of the data:

[S6] Barta-Rajnai, E.; Várhegyi, G.; Wang, L.; Skreiberg, Ø.; Grønli, M.; Czégény, Zs. Thermal decomposition kinetics of wood and bark and their torrefied products. *Energy Fuels* **2017**, *31*, 4024-4034. doi: [10.1021/acs.energyfuels.6b03419](https://doi.org/10.1021/acs.energyfuels.6b03419) [Supporting info](#) [Repository](#)

Spruce (Norway spruce) and its bark were examined. The samples were obtained from a forest in South Norway. Eight TGA experiments were available for each sample: three with linear heating (2.5, 10 and 40 °C/min), two with stepwise heating, and isothermal experiments at 225, 275 and 325°C. (The isothermal experiments were evaluated together with the heat-up sections, as shown in the next pages.) The figure below shows the corresponding temperature programs. It is a redrawn/rearranged version of Figure 1 of the cited paper.



**Figure S6.1:** Temperature programs used for the TGA experiments of this section.



## S6.1. Bark

### Model with constant E:

Input file: "B\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 183.7358$$

$$\log_{10}\tilde{A}(x)= 12.815827 - .505444x + .87104x^2 - 3.110812x^3 - 5.027752x^4 - 3.535776x^5$$

Expressed with Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 11.36594T_0(x) - 5.048413T_1(x) - 2.078356T_2(x) - 1.882633T_3(x) - .628469T_4(x) - .220986T_5(x)$$

### Model with third order E( $\alpha$ ):

Input file: "B\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

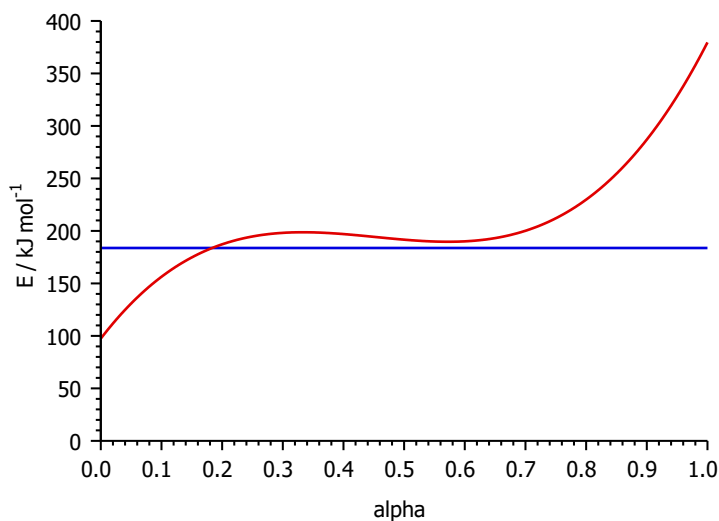
$$E(x)= 191.660298 - 23.91577x + 46.847964x^2 + 164.984172x^3$$

$$\log_{10}\tilde{A}(x)= 13.514137 - 2.5125887x + 5.545716x^2 + 10.0581952x^3 - 6.413064x^4 - 1.645296x^5$$

Expressed with Chebyshev polynomials of the first kind:

$$E(x)= 215.08428T_0(x) + 99.822359T_1(x) + 23.423982T_2(x) + 41.246043T_3(x)$$

$$\log_{10}\tilde{A}(x)= 13.882096T_0(x) + 4.0027477T_1(x) - .433674T_2(x) + 2.0003938T_3(x) - .801633T_4(x) - .102831T_5(x)$$



#### E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)

Parameter file: B\_0,5\_oneC.PAR

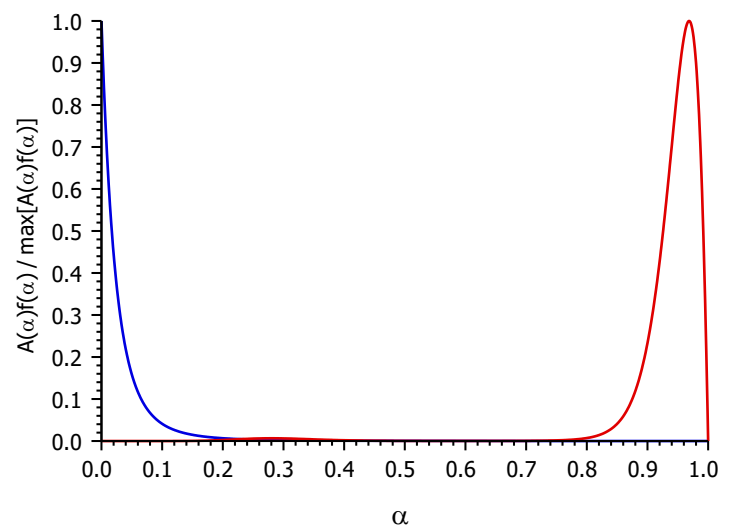
$$\log_{10}\tilde{A}(0)= 15.81 \quad E(0)= 183.7 \quad \log_{10}\tilde{A}(1)= 1.51 \quad E(1)= 183.7$$

$$\text{mean } \log_{10}\tilde{A}= 12.10 \quad \text{mean } E= 183.7$$

Parameter file: B\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 6.75 \quad E(0)= 97.4 \quad \log_{10}\tilde{A}(1)= 18.55 \quad E(1)= 379.6$$

$$\text{mean } \log_{10}\tilde{A}= 14.08 \quad \text{mean } E= 207.3$$



#### Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]

Parameter file: B\_0,5\_oneC.PAR

$$A(0)f(0)= 6.474E+15 \quad E(0)= 183.7 \quad A(1)f(1)= 0.00 \quad E(1)= 183.7$$

$$\text{mean } A(\alpha)f(\alpha)= 1.841E+14 \quad \text{mean } E= 183.7$$

$$\text{max } A(\alpha)f(\alpha)= 6.474E+15 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 183.7$$

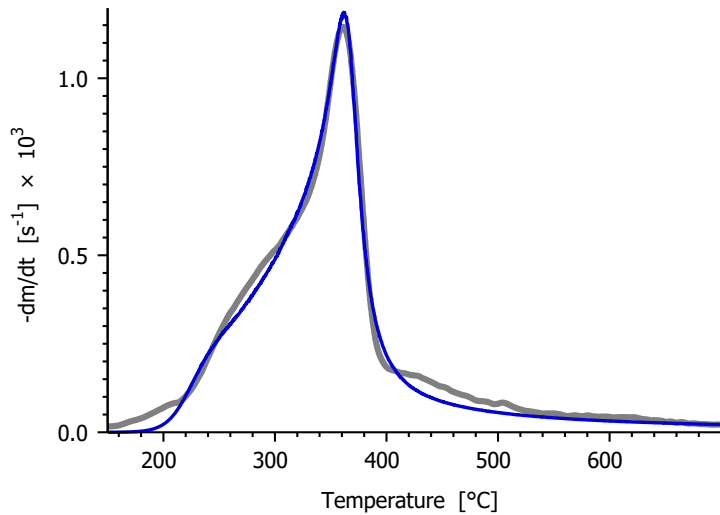
Parameter file: B\_3,5\_oneC.PAR

$$A(0)f(0)= 5.578E+06 \quad E(0)= 97.4 \quad A(1)f(1)= 0.00 \quad E(1)= 379.6$$

$$\text{mean } A(\alpha)f(\alpha)= 3.402E+15 \quad \text{mean } E= 207.3$$

$$\text{max } A(\alpha)f(\alpha)= 4.676E+16 \quad \text{at } \alpha= 0.969 \quad \text{and } E= 346.2$$

Figures illustrating the fit quality (cf. Figure S1 in the Supporting Information of reference [S6])



**Bark, 10°C/min, 2mg**

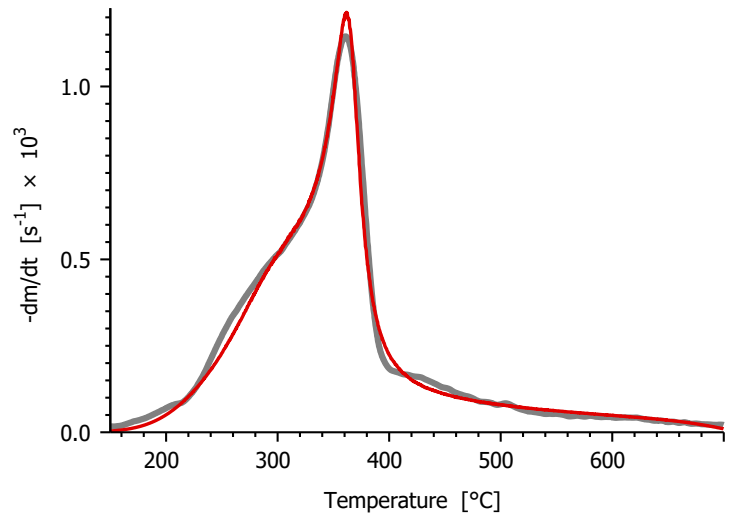
Relative deviation: 2.33%, Deviation: 0.058 µg/s  
rms rel. dev. of 8 experiments: 3.33%

Model:  $x=2\alpha-1$

$E(x) = 183.74$

$\log_{10} \tilde{A}(x) = 11.366T_0(x) - 5.048T_1(x) - 2.078T_2(x) - 1.883T_3(x) - 0.628T_4(x) - 0.221T_5(x)$

$c = 0.723$



**Bark, 10°C/min, 2mg**

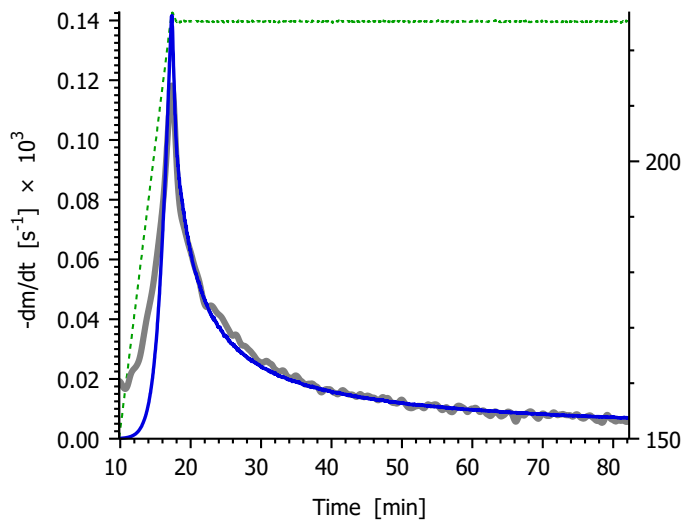
Relative deviation: 2.05%, Deviation: 0.051 µg/s  
rms rel. dev. of 8 experiments: 2.18%

Model:  $x=2\alpha-1$

$E(x) = 215.08T_0(x) + 99.82T_1(x) + 23.42T_2(x) + 41.25T_3(x)$

$\log_{10} \tilde{A}(x) = 13.882T_0(x) + 4.003T_1(x) - 0.434T_2(x) + 2.0T_3(x) - 0.802T_4(x) - 0.103T_5(x)$

$c = 0.702$



**Bark, 65min at 225°C (10°C/min), 4mg**

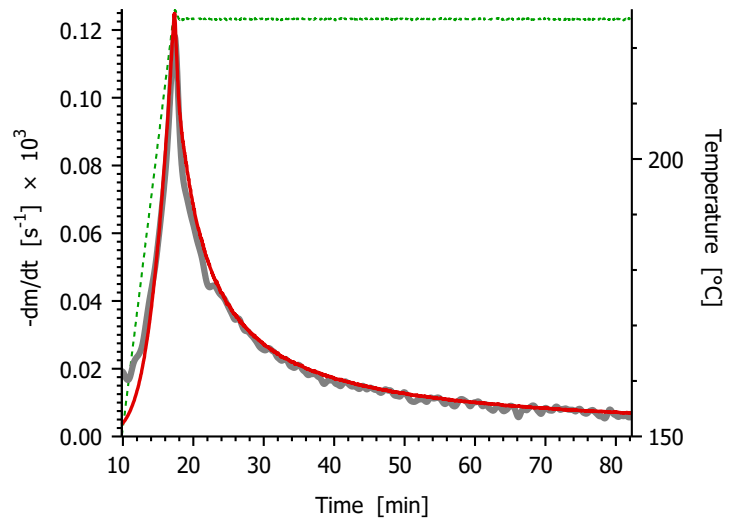
Relative deviation: 6.25%, Deviation: 0.029 µg/s  
rms rel. dev. of 8 experiments: 3.33%

Model:  $x=2\alpha-1$

$E(x) = 183.74$

$\log_{10} \tilde{A}(x) = 11.366T_0(x) - 5.048T_1(x) - 2.078T_2(x) - 1.883T_3(x) - 0.628T_4(x) - 0.221T_5(x)$

$c = 0.723$



**Bark, 65min at 225°C (10°C/min), 4mg**

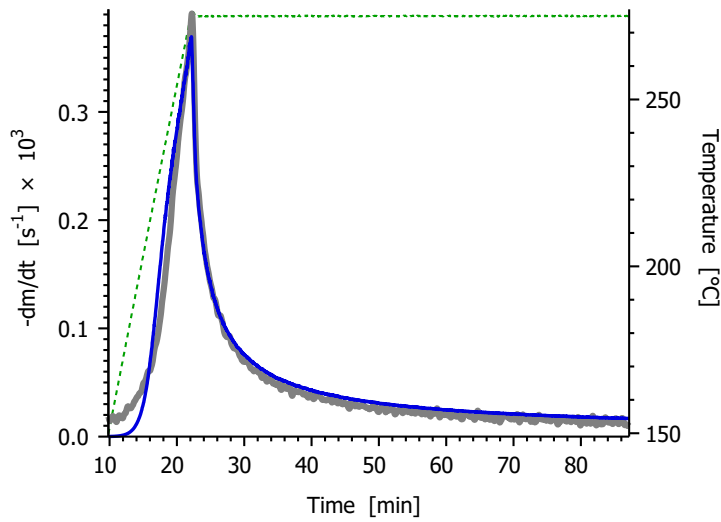
Relative deviation: 2.77%, Deviation: 0.013 µg/s  
rms rel. dev. of 8 experiments: 2.18%

Model:  $x=2\alpha-1$

$E(x) = 215.08T_0(x) + 99.82T_1(x) + 23.42T_2(x) + 41.25T_3(x)$

$\log_{10} \tilde{A}(x) = 13.882T_0(x) + 4.003T_1(x) - 0.434T_2(x) + 2.0T_3(x) - 0.802T_4(x) - 0.103T_5(x)$

$c = 0.702$



**Bark, 65min at 275°C (10°C/min), 4mg**

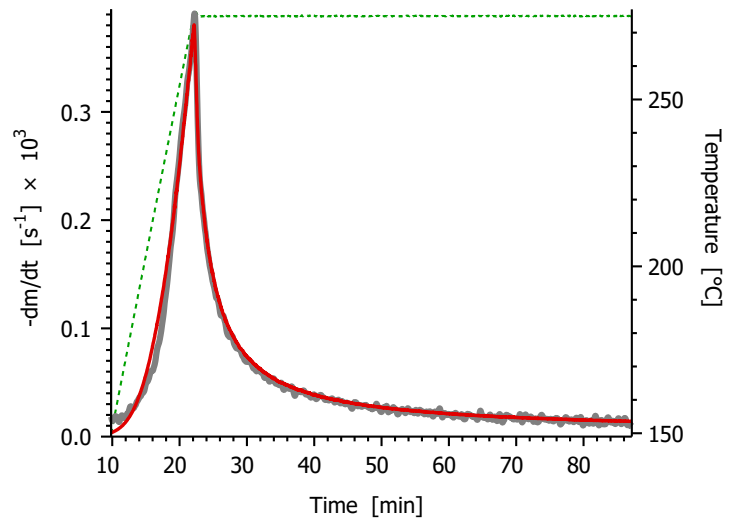
Relative deviation: 3.13%, Deviation: 0.049 µg/s  
rms rel. dev. of 8 experiments: 3.33%

Model:  $x=2\alpha-1$

$E(x) = 183.74$

$\log_{10} \tilde{A}(x) = 11.366T_0(x) - 5.048T_1(x) - 2.078T_2(x) - 1.883T_3(x) - 0.628T_4(x) - 0.221T_5(x)$

$c = 0.723$



**Bark, 65min at 275°C (10°C/min), 4mg**

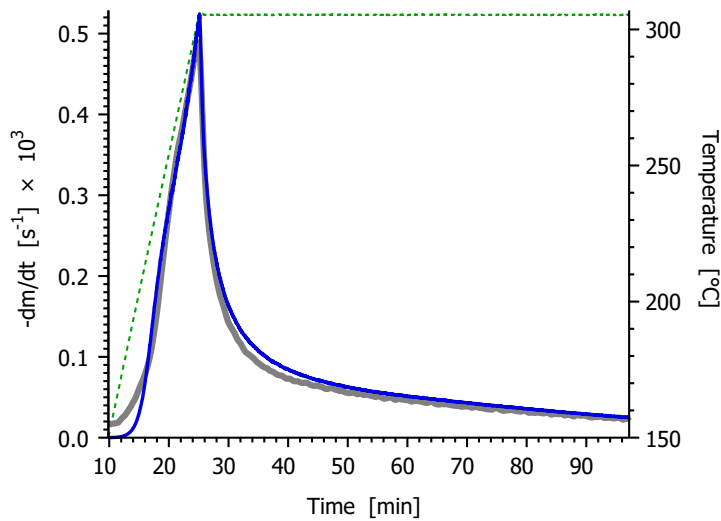
Relative deviation: 1.57%, Deviation: 0.024 µg/s  
rms rel. dev. of 8 experiments: 2.18%

Model:  $x=2\alpha-1$

$E(x) = 215.08T_0(x) + 99.82T_1(x) + 23.42T_2(x) + 41.25T_3(x)$

$\log_{10} \tilde{A}(x) = 13.882T_0(x) + 4.003T_1(x) - 0.434T_2(x) + 2.0T_3(x) - 0.802T_4(x) - 0.103T_5(x)$

$c = 0.702$



**Bark, 65min at 305°C (10°C/min), 4mg**

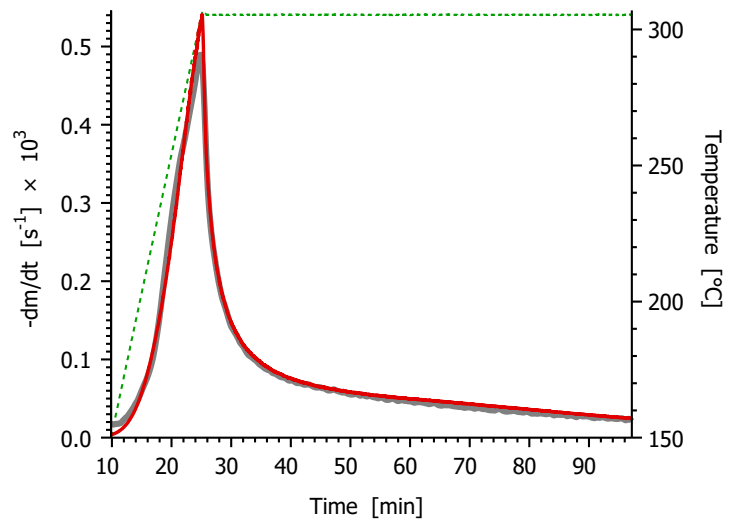
Relative deviation: 2.43%, Deviation: 0.044 µg/s  
rms rel. dev. of 8 experiments: 3.33%

Model:  $x=2\alpha-1$

$E(x) = 183.74$

$\log_{10} \tilde{A}(x) = 11.366T_0(x) - 5.048T_1(x) - 2.078T_2(x) - 1.883T_3(x) - 0.628T_4(x) - 0.221T_5(x)$

$c = 0.723$



**Bark, 65min at 305°C (10°C/min), 4mg**

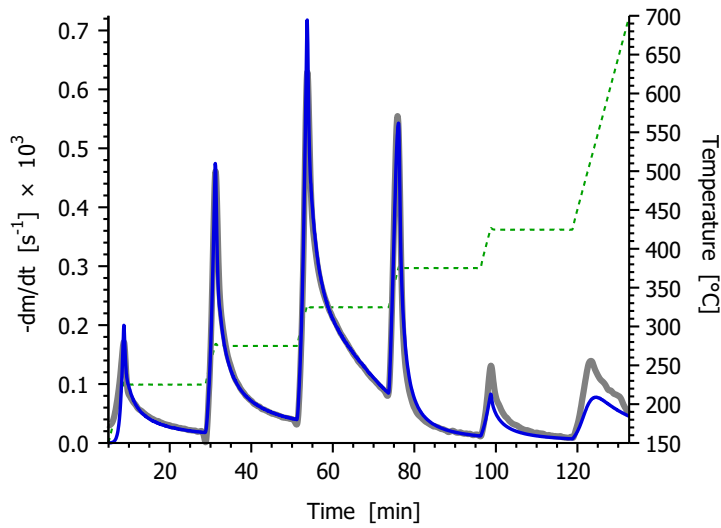
Relative deviation: 1.76%, Deviation: 0.032 µg/s  
rms rel. dev. of 8 experiments: 2.18%

Model:  $x=2\alpha-1$

$E(x) = 215.08T_0(x) + 99.82T_1(x) + 23.42T_2(x) + 41.25T_3(x)$

$\log_{10} \tilde{A}(x) = 13.882T_0(x) + 4.003T_1(x) - 0.434T_2(x) + 2.0T_3(x) - 0.802T_4(x) - 0.103T_5(x)$

$c = 0.702$



**Bark, stepwise T(t) "A" (20°C/min), 4mg**

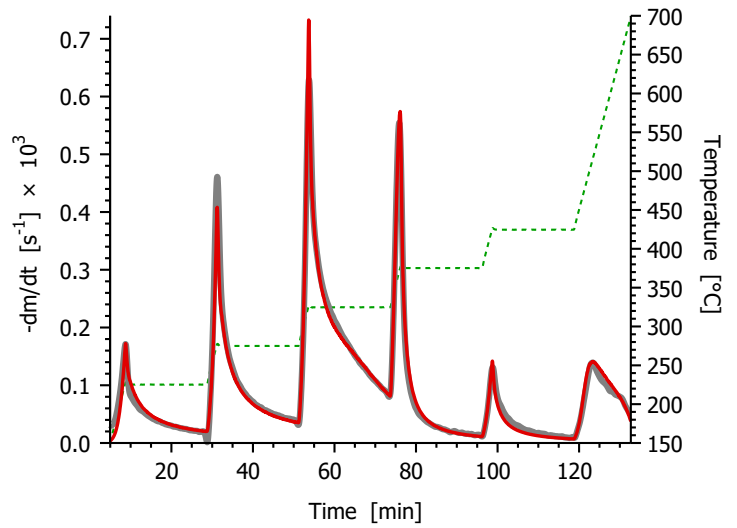
Relative deviation: 2.88%, Deviation: 0.073 µg/s  
rms rel. dev. of 8 experiments: 3.33%

Model:  $x=2\alpha-1$

$E(x) = 183.74$

$\log_{10} \tilde{A}(x) = 11.366T_0(x) - 5.048T_1(x) - 2.078T_2(x) - 1.883T_3(x) - 0.628T_4(x) - 0.221T_5(x)$

$c = 0.723$



**Bark, stepwise T(t) "A" (20°C/min), 4mg**

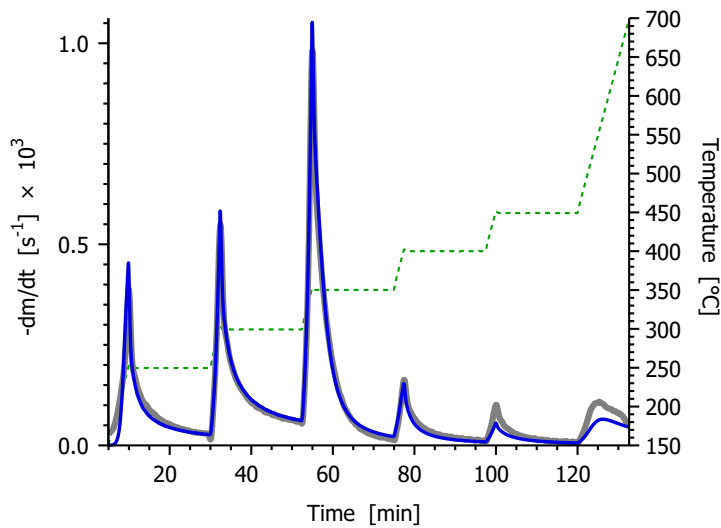
Relative deviation: 2.21%, Deviation: 0.056 µg/s  
rms rel. dev. of 8 experiments: 2.18%

Model:  $x=2\alpha-1$

$E(x) = 215.08T_0(x) + 99.82T_1(x) + 23.42T_2(x) + 41.25T_3(x)$

$\log_{10} \tilde{A}(x) = 13.882T_0(x) + 4.003T_1(x) - 0.434T_2(x) + 2.0T_3(x) - 0.802T_4(x) - 0.103T_5(x)$

$c = 0.702$



**Bark, stepwise T(t) "B" (20°C/min), 4mg**

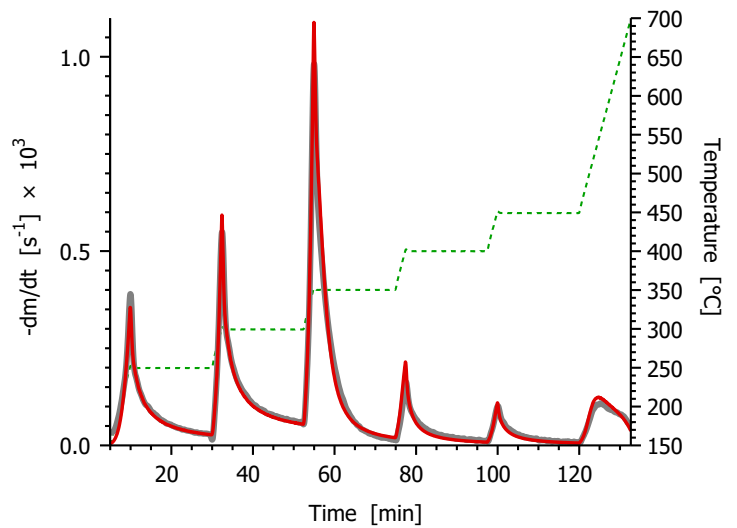
Relative deviation: 1.86%, Deviation: 0.074 µg/s  
rms rel. dev. of 8 experiments: 3.33%

Model:  $x=2\alpha-1$

$E(x) = 183.74$

$\log_{10} \tilde{A}(x) = 11.366T_0(x) - 5.048T_1(x) - 2.078T_2(x) - 1.883T_3(x) - 0.628T_4(x) - 0.221T_5(x)$

$c = 0.723$



**Bark, stepwise T(t) "B" (20°C/min), 4mg**

Relative deviation: 1.48%, Deviation: 0.059 µg/s  
rms rel. dev. of 8 experiments: 2.18%

Model:  $x=2\alpha-1$

$E(x) = 215.08T_0(x) + 99.82T_1(x) + 23.42T_2(x) + 41.25T_3(x)$

$\log_{10} \tilde{A}(x) = 13.882T_0(x) + 4.003T_1(x) - 0.434T_2(x) + 2.0T_3(x) - 0.802T_4(x) - 0.103T_5(x)$

$c = 0.702$

## S6.2. Wood

### Model with constant E:

Input file: "W\_0,5\_oneC.PAR"

$$x=2\alpha-1$$

$$E= 173.51359$$

$$\log_{10}\tilde{A}(x)= 11.638268 - .41031x + 2.179856x^2 + .7517x^3 - 6.469424x^4 - 6.64784x^5$$

Expressed with Chebyshev polynomials of the first kind:

$$\log_{10}\tilde{A}(x)= 10.302162T_0(x) - 4.001435T_1(x) - 2.144784T_2(x) - 1.889525T_3(x) - .808678T_4(x) - .41549T_5(x)$$

### Model with third order E( $\alpha$ ):

Input file: "W\_3,5\_oneC.PAR"

$$x=2\alpha-1$$

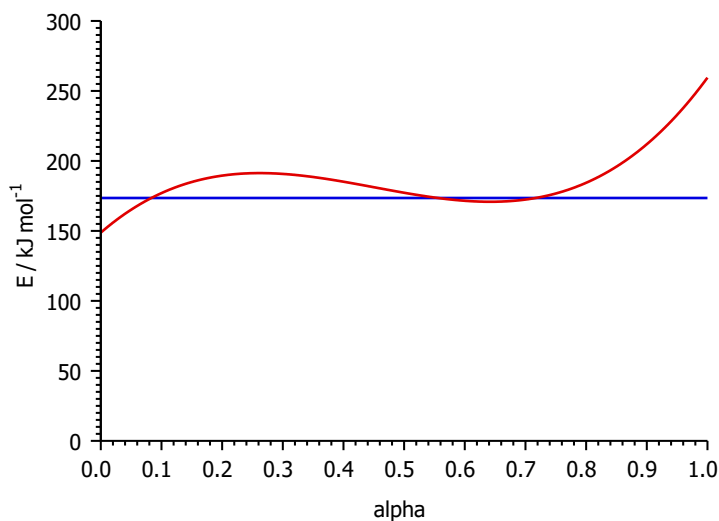
$$E(x)= 177.269618 - 37.801456x + 26.878364x^2 + 93.1628x^3$$

$$\log_{10}\tilde{A}(x)= 12.0739416 - 3.7579116x + 4.1196608x^2 + 9.0435888x^3 - 3.131296x^4 - 3.355152x^5$$

Expressed with Chebyshev polynomials of the first kind:

$$E(x)= 190.7088T_0(x) + 32.070644T_1(x) + 13.439182T_2(x) + 23.2907T_3(x)$$

$$\log_{10}\tilde{A}(x)= 12.959536T_0(x) + .92781T_1(x) + .4941824T_2(x) + 1.2124122T_3(x) - .391412T_4(x) - .209697T_5(x)$$



#### E( $\alpha$ ) = polynomial of (2 $\alpha$ -1)

Parameter file: W\_0,5\_oneC.PAR

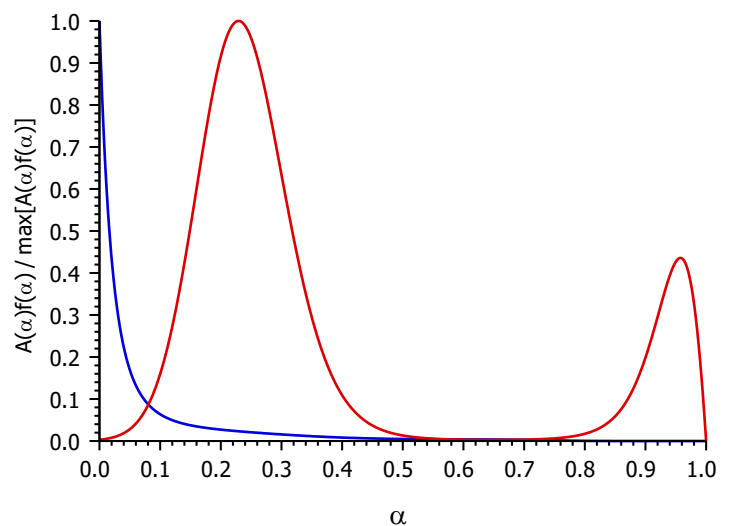
$$\log_{10}\tilde{A}(0)= 13.66 \quad E(0)= 173.5 \quad \log_{10}\tilde{A}(1)= 1.04 \quad E(1)= 173.5$$

$$\text{mean } \log_{10}\tilde{A}= 11.07 \quad \text{mean } E= 173.5$$

Parameter file: W\_3,5\_oneC.PAR

$$\log_{10}\tilde{A}(0)= 11.13 \quad E(0)= 148.8 \quad \log_{10}\tilde{A}(1)= 14.99 \quad E(1)= 259.5$$

$$\text{mean } \log_{10}\tilde{A}= 12.82 \quad \text{mean } E= 186.2$$



#### Plot of A( $\alpha$ )f( $\alpha$ ) / max[A( $\alpha$ )f( $\alpha$ )]

Parameter file: W\_0,5\_oneC.PAR

$$A(0)f(0)= 4.520E+13 \quad E(0)= 173.5 \quad A(1)f(1)= 0.00 \quad E(1)= 173.5$$

$$\text{mean } A(\alpha)f(\alpha)= 1.608E+12 \quad \text{mean } E= 173.5$$

$$\text{max } A(\alpha)f(\alpha)= 4.520E+13 \quad \text{at } \alpha= 0.000 \quad \text{and } E= 173.5$$

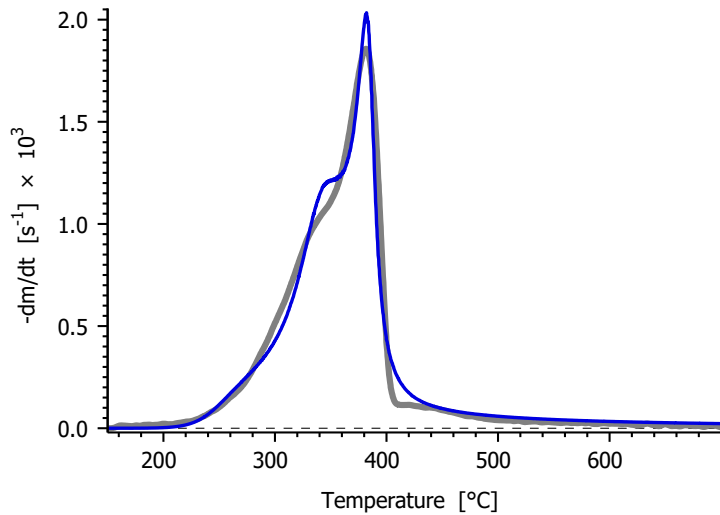
Parameter file: W\_3,5\_oneC.PAR

$$A(0)f(0)= 1.355E+11 \quad E(0)= 148.8 \quad A(1)f(1)= 0.00 \quad E(1)= 259.5$$

$$\text{mean } A(\alpha)f(\alpha)= 1.011E+13 \quad \text{mean } E= 186.2$$

$$\text{max } A(\alpha)f(\alpha)= 4.516E+13 \quad \text{at } \alpha= 0.229 \quad \text{and } E= 190.8$$

Figures illustrating the fit quality (cf. Figure S1 in the Supporting Information of reference [S6])



**Wood, 10°C/min, 2mg**

Relative deviation: 3.29%, Deviation: 0.12 µg/s

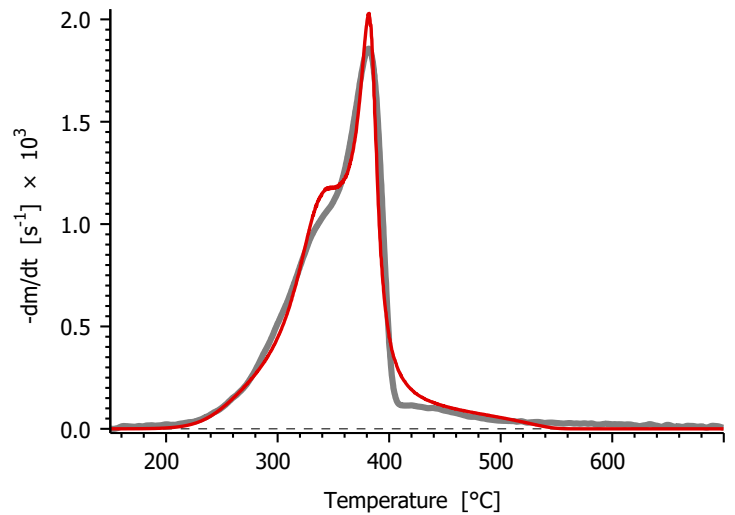
rms rel. dev. of 8 experiments: 4.43%

Model:  $x=2\alpha-1$

$E(x) = 173.51$

$\log_{10} \tilde{A}(x) = 10.302T_0(x) - 4.001T_1(x) - 2.145T_2(x) - 1.89T_3(x) - 0.809T_4(x) - 0.415T_5(x)$

$c = 0.912$



**Wood, 10°C/min, 2mg**

Relative deviation: 3.33%, Deviation: 0.12 µg/s

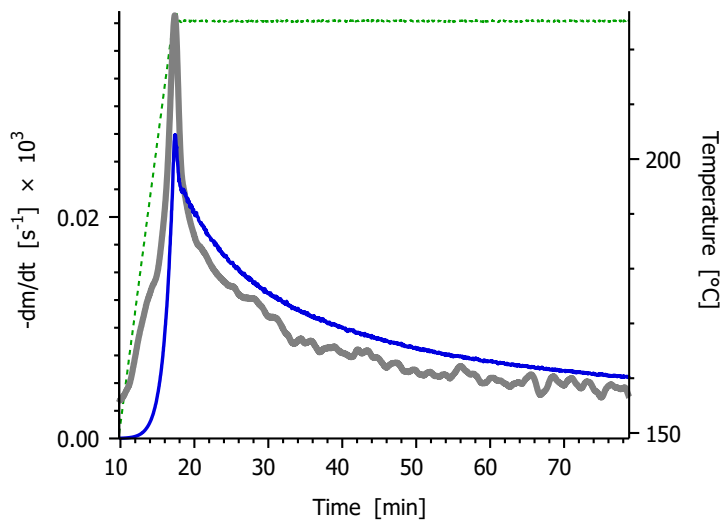
rms rel. dev. of 8 experiments: 4.26%

Model:  $x=2\alpha-1$

$E(x) = 190.71T_0(x) + 32.07T_1(x) + 13.44T_2(x) + 23.29T_3(x)$

$\log_{10} \tilde{A}(x) = 12.96T_0(x) + 0.928T_1(x) + 0.494T_2(x) + 1.212T_3(x) - 0.391T_4(x) - 0.21T_5(x)$

$c = 0.835$



**Wood, 65min at 225°C (10°C/min), 4mg**

Relative deviation: 9.83%, Deviation: 0.015 µg/s

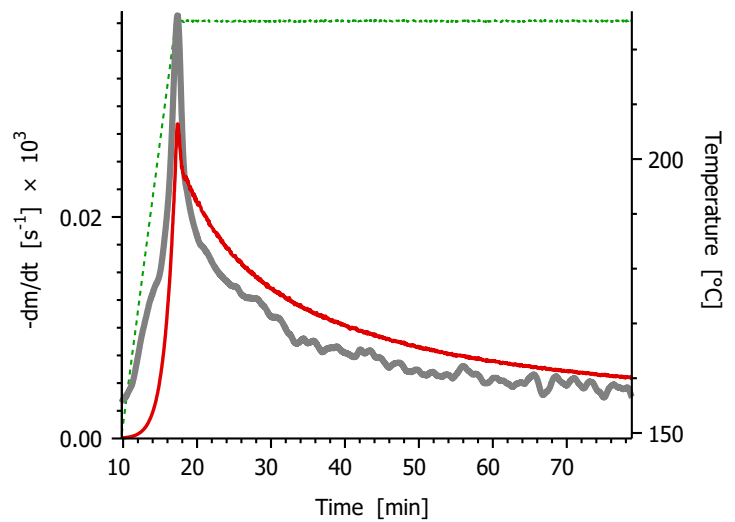
rms rel. dev. of 8 experiments: 4.43%

Model:  $x=2\alpha-1$

$E(x) = 173.51$

$\log_{10} \tilde{A}(x) = 10.302T_0(x) - 4.001T_1(x) - 2.145T_2(x) - 1.89T_3(x) - 0.809T_4(x) - 0.415T_5(x)$

$c = 0.912$



**Wood, 65min at 225°C (10°C/min), 4mg**

Relative deviation: 9.35%, Deviation: 0.015 µg/s

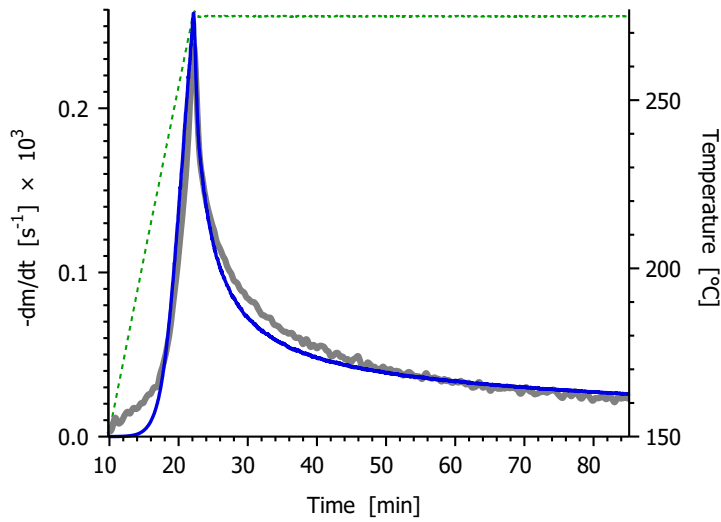
rms rel. dev. of 8 experiments: 4.26%

Model:  $x=2\alpha-1$

$E(x) = 190.71T_0(x) + 32.07T_1(x) + 13.44T_2(x) + 23.29T_3(x)$

$\log_{10} \tilde{A}(x) = 12.96T_0(x) + 0.928T_1(x) + 0.494T_2(x) + 1.212T_3(x) - 0.391T_4(x) - 0.21T_5(x)$

$c = 0.835$



**Wood, 65min at 275°C (10°C/min), 4mg**

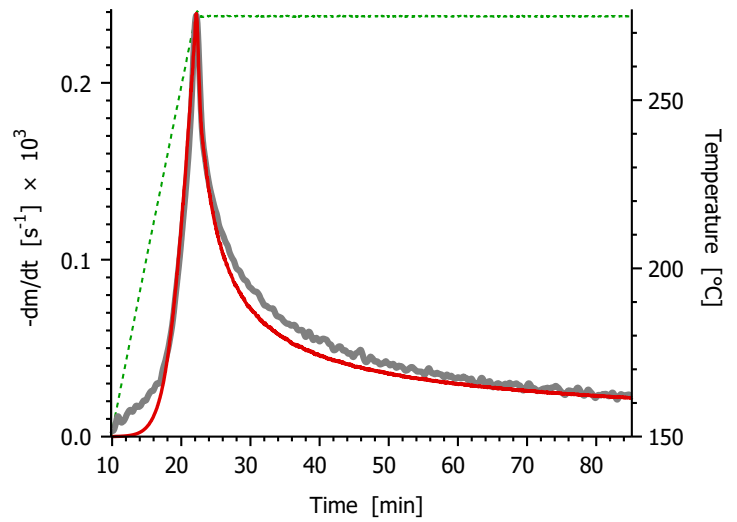
Relative deviation: 3.76%, Deviation: 0.030 µg/s  
rms rel. dev. of 8 experiments: 4.43%

Model:  $x=2\alpha-1$

$E(x) = 173.51$

$\log_{10} \tilde{A}(x) = 10.302T_0(x) - 4.001T_1(x) - 2.145T_2(x) - 1.89T_3(x) - 0.809T_4(x) - 0.415T_5(x)$

$c = 0.912$



**Wood, 65min at 275°C (10°C/min), 4mg**

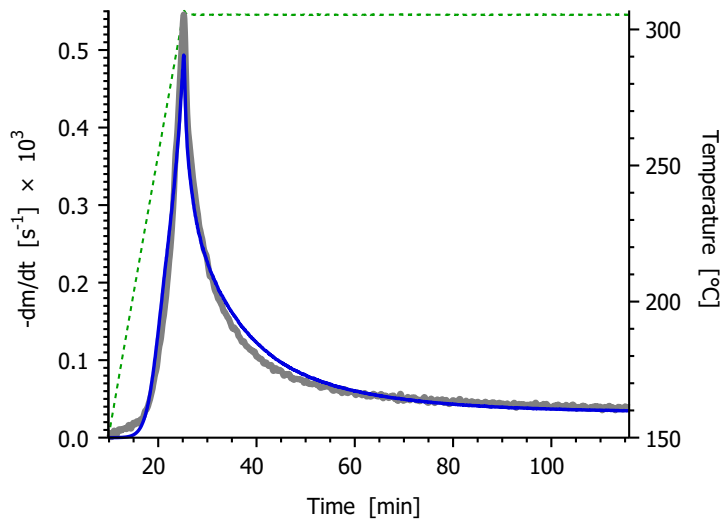
Relative deviation: 3.14%, Deviation: 0.025 µg/s  
rms rel. dev. of 8 experiments: 4.26%

Model:  $x=2\alpha-1$

$E(x) = 190.71T_0(x) + 32.07T_1(x) + 13.44T_2(x) + 23.29T_3(x)$

$\log_{10} \tilde{A}(x) = 12.96T_0(x) + 0.928T_1(x) + 0.494T_2(x) + 1.212T_3(x) - 0.391T_4(x) - 0.21T_5(x)$

$c = 0.835$



**Wood, 90min at 305°C (10°C/min), 4mg**

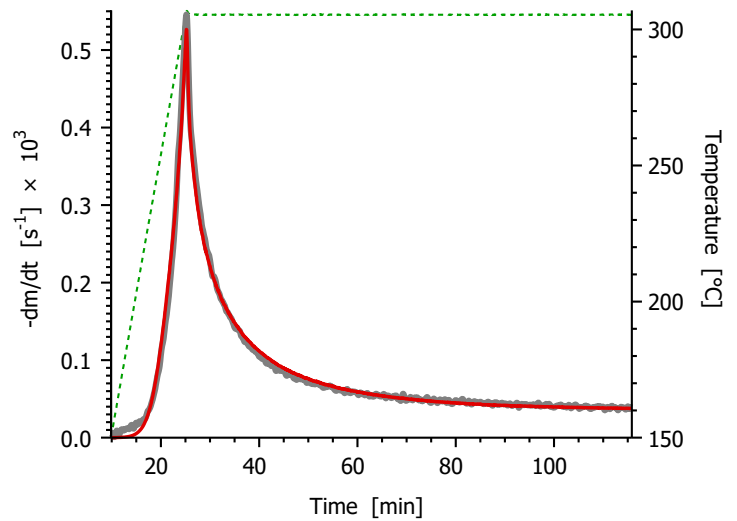
Relative deviation: 2.42%, Deviation: 0.052 µg/s  
rms rel. dev. of 8 experiments: 4.43%

Model:  $x=2\alpha-1$

$E(x) = 173.51$

$\log_{10} \tilde{A}(x) = 10.302T_0(x) - 4.001T_1(x) - 2.145T_2(x) - 1.89T_3(x) - 0.809T_4(x) - 0.415T_5(x)$

$c = 0.912$



**Wood, 90min at 305°C (10°C/min), 4mg**

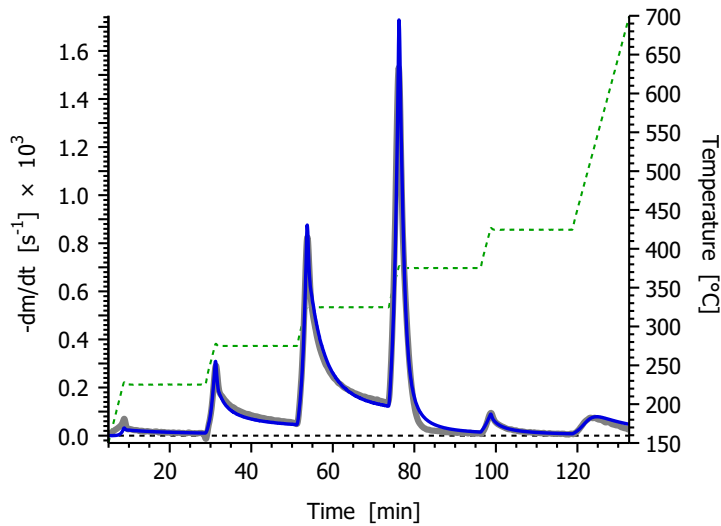
Relative deviation: 1.29%, Deviation: 0.028 µg/s  
rms rel. dev. of 8 experiments: 4.26%

Model:  $x=2\alpha-1$

$E(x) = 190.71T_0(x) + 32.07T_1(x) + 13.44T_2(x) + 23.29T_3(x)$

$\log_{10} \tilde{A}(x) = 12.96T_0(x) + 0.928T_1(x) + 0.494T_2(x) + 1.212T_3(x) - 0.391T_4(x) - 0.21T_5(x)$

$c = 0.835$


**Wood, stepwise T(t) "A" (20°C/min), 4mg**

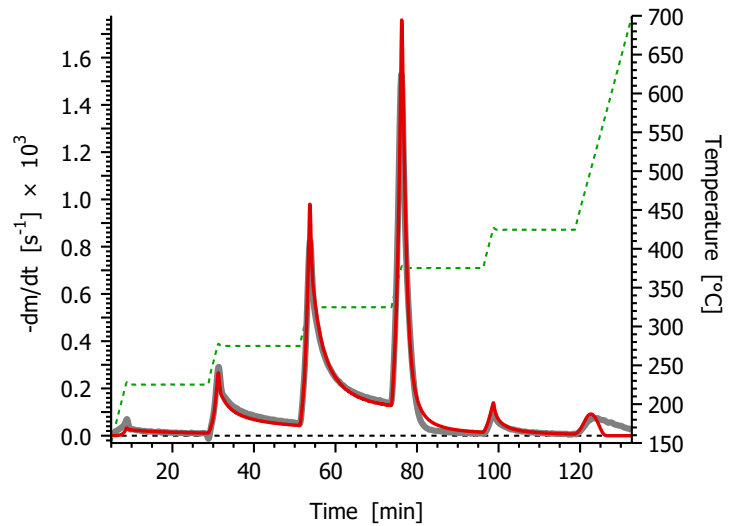
Relative deviation: 1.65%, Deviation: 0.097 µg/s  
rms rel. dev. of 8 experiments: 4.43%

Model:  $x=2\alpha-1$

$E(x) = 173.51$

$\log_{10} \tilde{A}(x) = 10.302T_0(x) - 4.001T_1(x) - 2.145T_2(x) - 1.89T_3(x) - 0.809T_4(x) - 0.415T_5(x)$

$c = 0.912$


**Wood, stepwise T(t) "A" (20°C/min), 4mg**

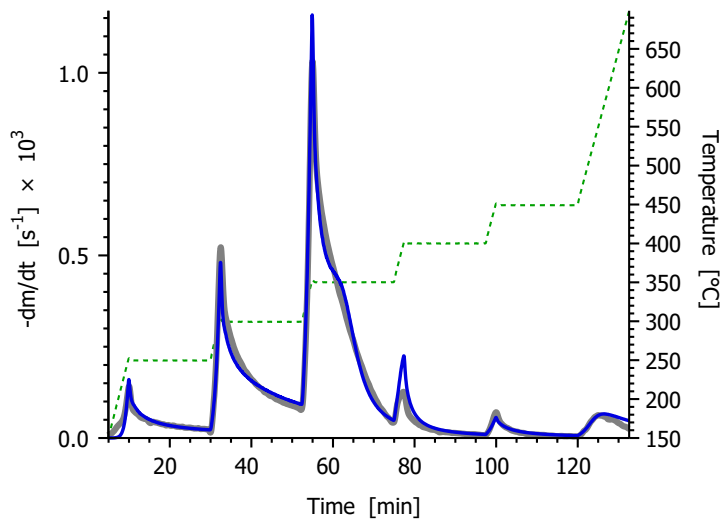
Relative deviation: 1.86%, Deviation: 0.11 µg/s  
rms rel. dev. of 8 experiments: 4.26%

Model:  $x=2\alpha-1$

$E(x) = 190.71T_0(x) + 32.07T_1(x) + 13.44T_2(x) + 23.29T_3(x)$

$\log_{10} \tilde{A}(x) = 12.96T_0(x) + 0.928T_1(x) + 0.494T_2(x) + 1.212T_3(x) - 0.391T_4(x) - 0.21T_5(x)$

$c = 0.835$


**Wood, stepwise T(t) "B" (20°C/min), 4mg**

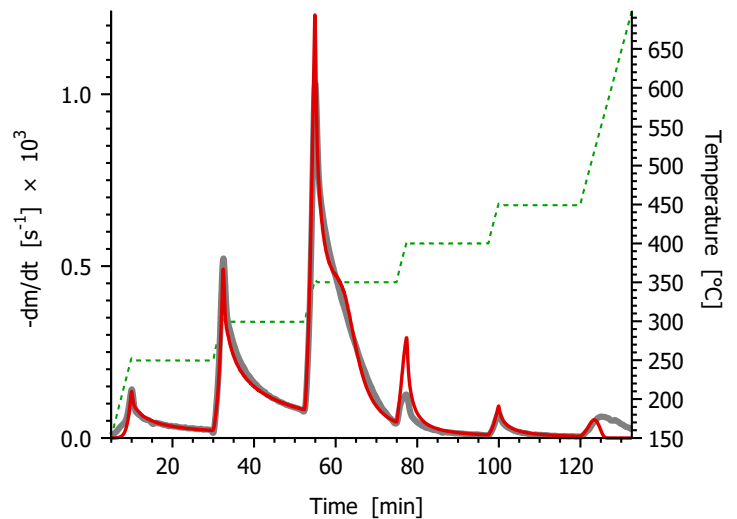
Relative deviation: 2.14%, Deviation: 0.096 µg/s  
rms rel. dev. of 8 experiments: 4.43%

Model:  $x=2\alpha-1$

$E(x) = 173.51$

$\log_{10} \tilde{A}(x) = 10.302T_0(x) - 4.001T_1(x) - 2.145T_2(x) - 1.89T_3(x) - 0.809T_4(x) - 0.415T_5(x)$

$c = 0.912$


**Wood, stepwise T(t) "B" (20°C/min), 4mg**

Relative deviation: 2.85%, Deviation: 0.13 µg/s  
rms rel. dev. of 8 experiments: 4.26%

Model:  $x=2\alpha-1$

$E(x) = 190.71T_0(x) + 32.07T_1(x) + 13.44T_2(x) + 23.29T_3(x)$

$\log_{10} \tilde{A}(x) = 12.96T_0(x) + 0.928T_1(x) + 0.494T_2(x) + 1.212T_3(x) - 0.391T_4(x) - 0.21T_5(x)$

$c = 0.835$